



A T M E
College of Engineering



APPLIED THERMODYNAMICS BME401

Introduction

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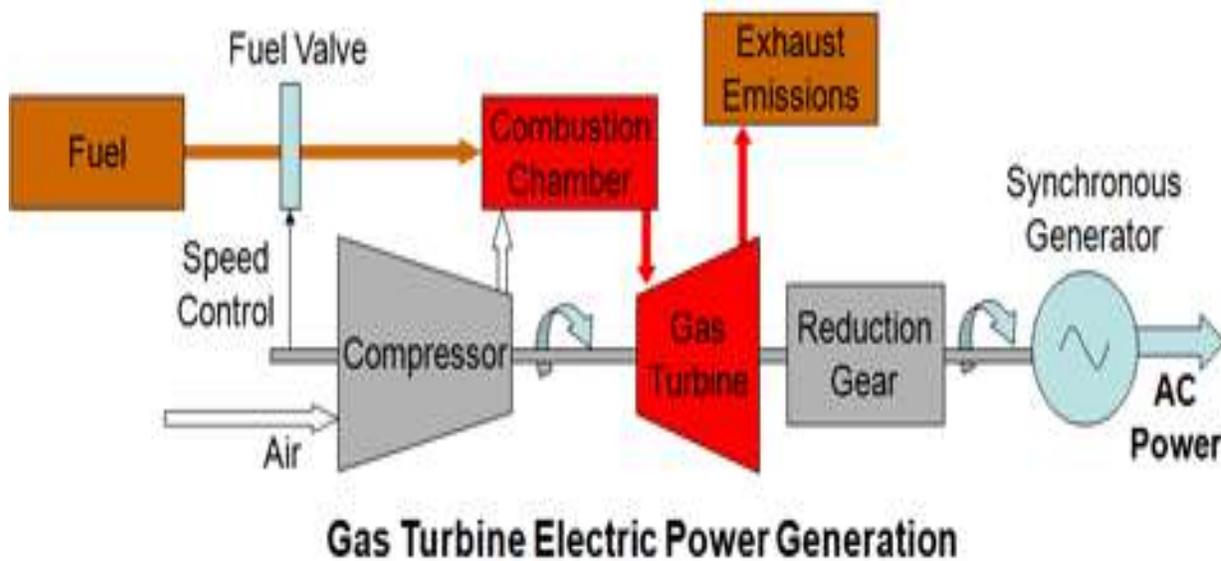


Syllabus

- **Module – 1: Air standard cycles, I.C. Engines**
- **Module – 2: Gas power Cycles**
- **Module – 3: Vapour Power Cycles**
- **Module – 4: Refrigeration Cycles, Psychometrics and Air-conditioning Systems**
- **Module – 5: Reciprocating Compressors, Steam nozzles**

Importance of studying the subject (Applications of Applied Thermodynamics)

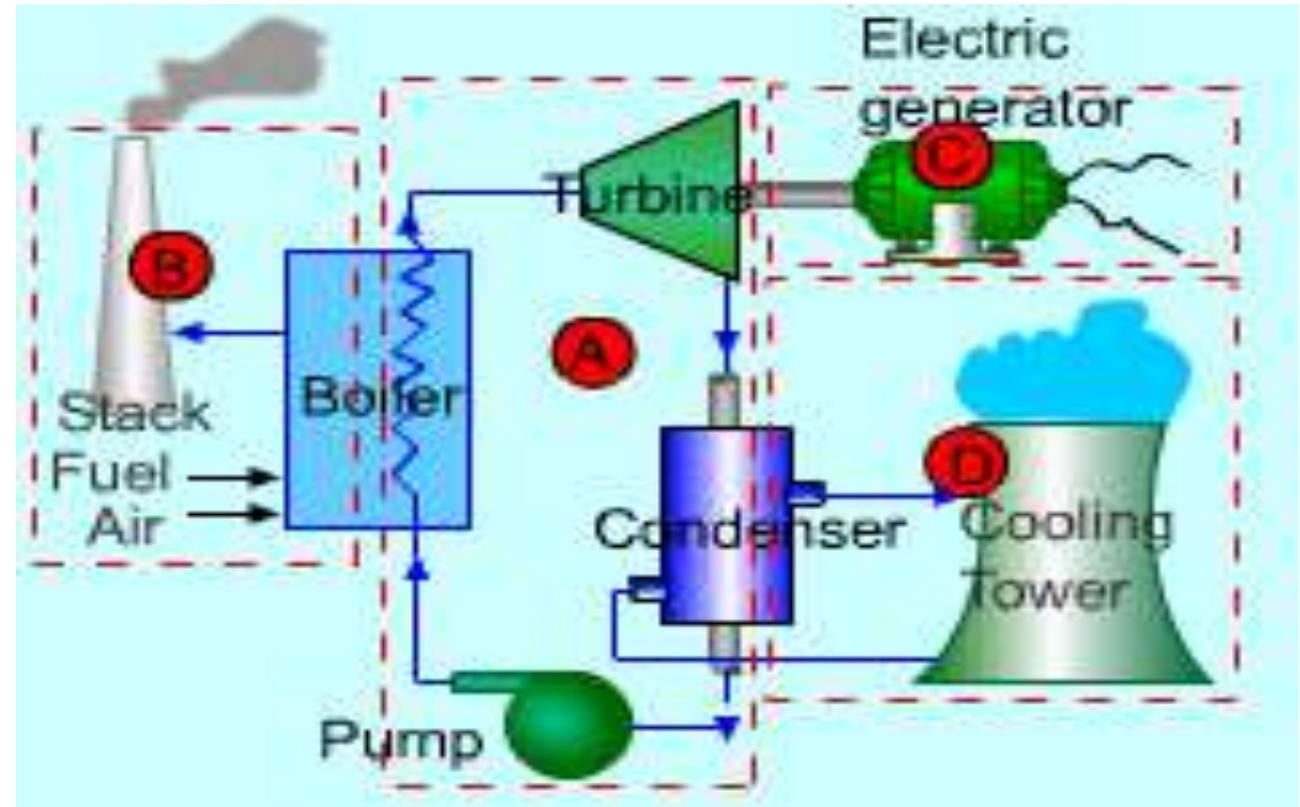
Gas turbine used in rocket



Importance of studying the subject (Applications of Applied Thermodynamics)

Vapour Power Cycle in Thermal power plant

- Coal: 204,724.5 MW (55.6%)**
- Large Hydro: 45,399.22 MW (12.3%)**
- Small Hydro: 4,671.56 MW (1.3%)**
- Wind Power: 37,505.18 MW (10.2%)**
- Solar Power: 33,730.56 MW (9.2%)**
- Biomass: 10,001.11 MW (2.7%)**
- Nuclear: 6,780 MW (1.8%)**
- Gas: 24,955.36 MW (6.8%)**
- Diesel: 509.71 MW (0.1%)**



Importance of studying the subject (Applications of Applied Thermodynamics)

Refrigeration Cycles, Psychometrics and Air-conditioning Systems



Importance of studying the subject (Applications of Applied Thermodynamics)

Reciprocating Compressors



References

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- Thermodynamics, Yunus A, Cengel, Michael A Boles, Tata McGraw Hill, 7th Edition
- Thermodynamics for engineers, Kenneth A. Kroos and Merle C. Potter, Cengage Learning 2016
- Thermodynamics, Radhakrishnan, PHI 2nd revised Edition
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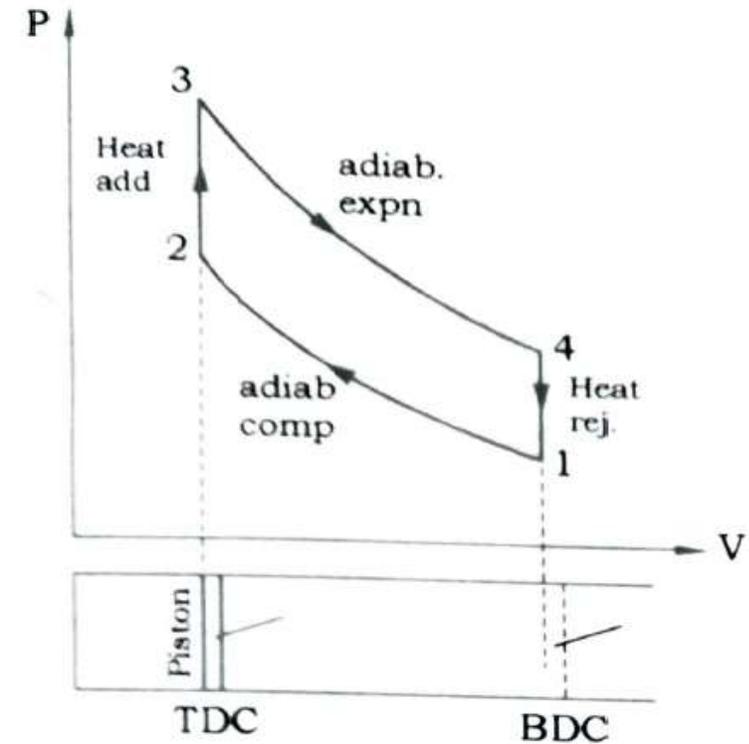
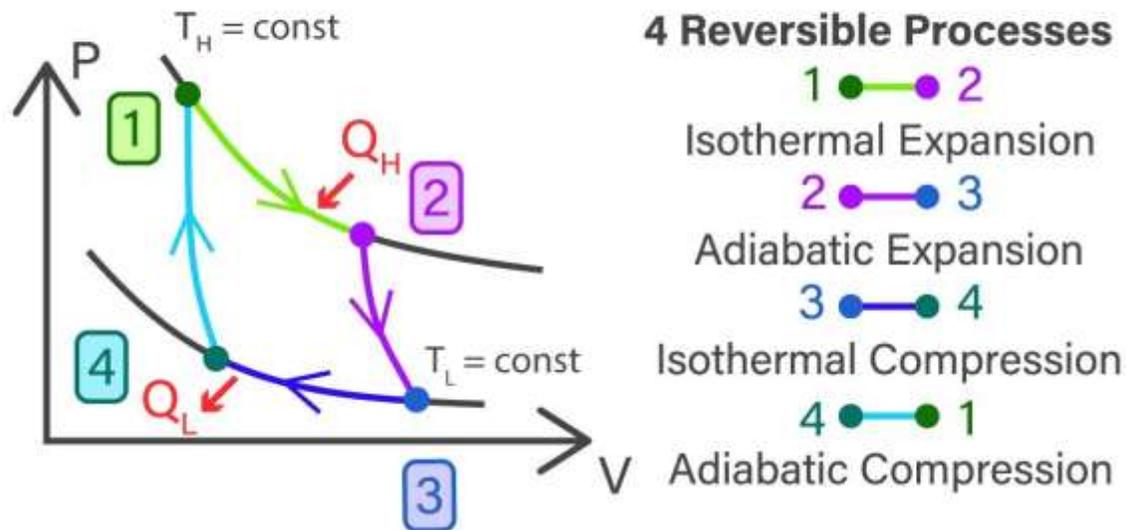


Module – 1: Air standard cycles

- **Air standard cycles:** Carnot, Otto, Diesel, Dual and Stirling cycles, p-v and T -S diagrams, description, efficiencies and mean effective pressures. Comparison of Otto and Diesel cycles.
- **I.C.Engines:** Classification of IC engines, Combustion of SI engine and CI engine, Detonation and factors affecting detonation, Performance analysis of I.C Engines, Heat balance, Morse test.

Air standard cycles

CARNOT HEAT ENGINE



Carnot cycle

Expression for air standard efficiency in Carnot cycle

Process 1-2: Isothermal Expansion

∴ Heat absorbed or heat added or heat supplied = $Q_s = P_1 V_1 \ln \left(\frac{V_2}{V_1} \right)$

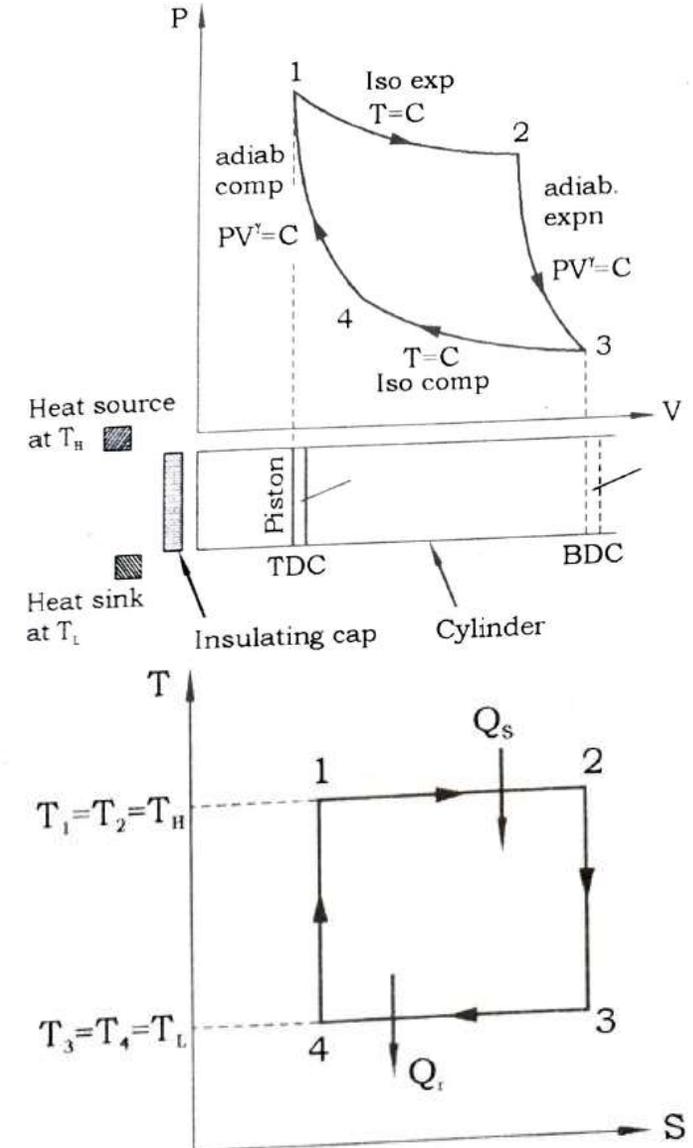
under ideal conditions, we have $PV = mRT$ i.e., $P_1 V_1 = mRT_1$

$$\therefore Q_s = mRT_1 \ln \left(\frac{V_2}{V_1} \right) \quad \text{-----(1)}$$

Process 2-3: Adiabatic Expansion

w.k.t. from adiabatic process, heat transfer $Q = 0$

$$\frac{T_2}{T_3} = \left(\frac{V_3}{V_2} \right)^{\gamma-1} \quad \text{-----(2)}$$



Carnot cycle

Process 3-4: Isothermal compression

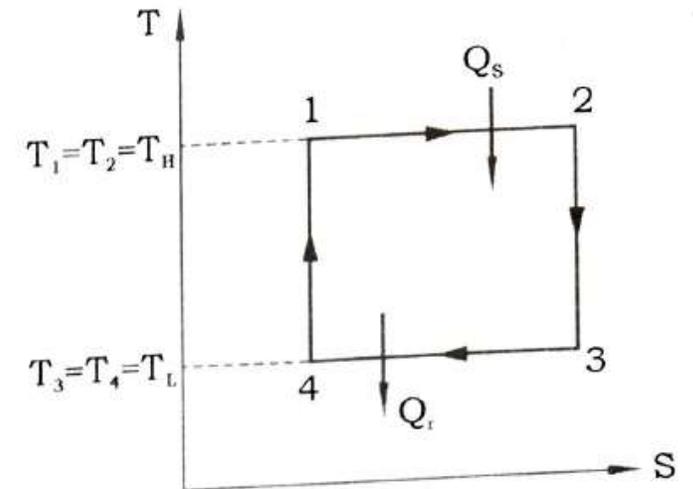
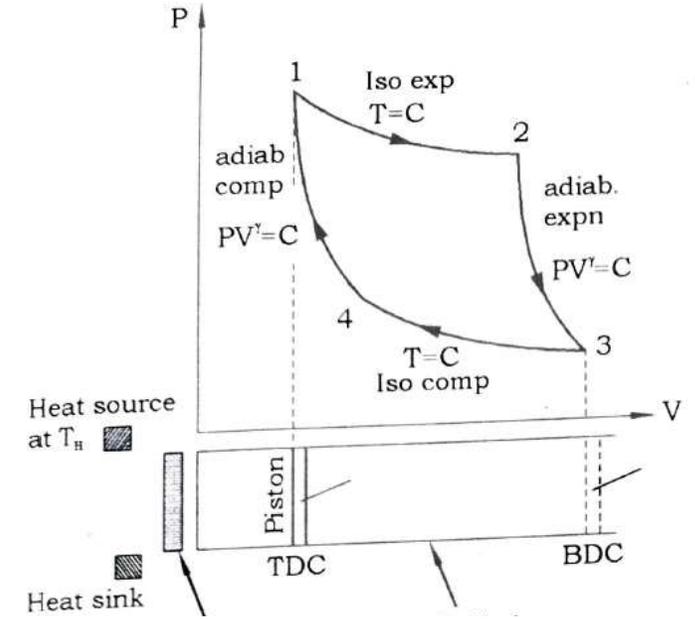
$$\text{Heat rejected} = Q_r = P_3 V_3 \ln \left(\frac{V_3}{V_4} \right)$$

$$= mRT_3 \ln \left(\frac{V_3}{V_4} \right) \quad \text{---(3)}$$

Process 4-1: Adiabatic compression

w.k.t. for adiabatic process, heat transfer $Q = 0$

$$\frac{T_4}{T_1} = \left(\frac{V_1}{V_4} \right)^{\gamma-1} \quad \text{---(4)}$$

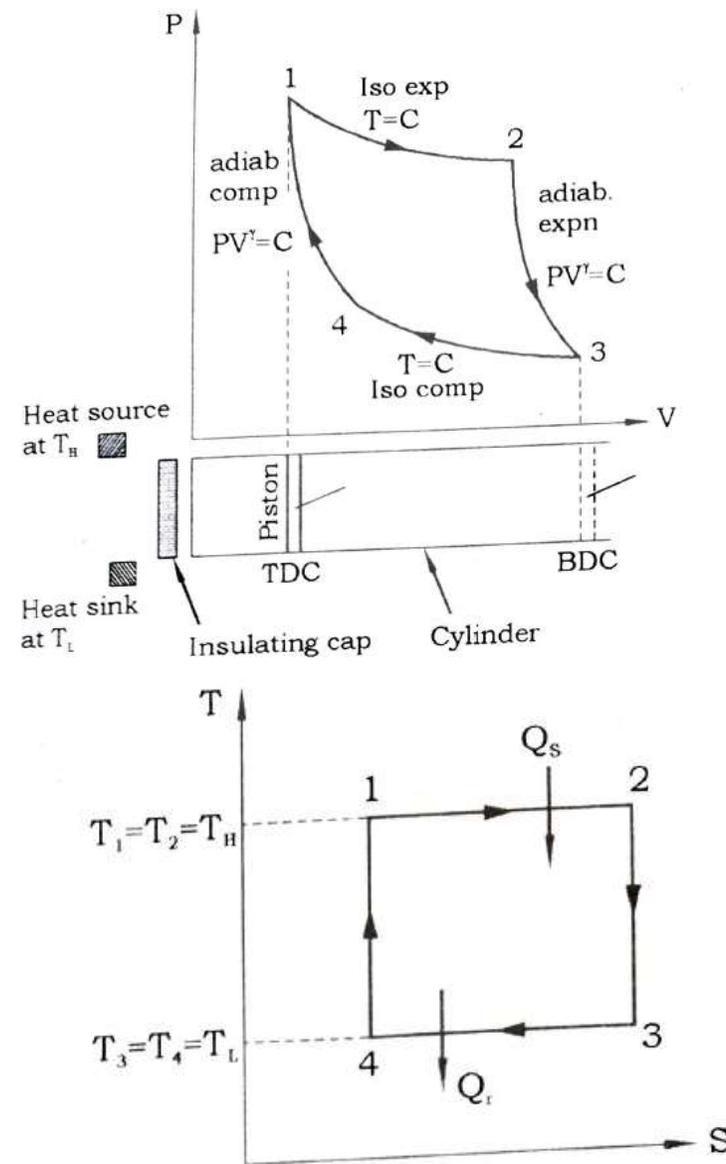


Carnot cycle

To find air standard efficiency:

$$\begin{aligned} \text{w.k.t. efficiency } \eta_{\text{air}} &= \frac{\text{Work done (WD)}}{\text{Heat supplied (} Q_s \text{)}} \\ &= \frac{\text{Heat supplied} - \text{Heat rejected}}{\text{Heat supplied}} \end{aligned}$$

$$\begin{aligned} &= \frac{Q_s - Q_r}{Q_s} \\ \eta_{\text{air}} &= 1 - \frac{Q_r}{Q_s} = 1 - \frac{m \cdot R T_3 \ln\left(\frac{V_3}{V_4}\right)}{m \cdot R T_1 \ln\left(\frac{V_2}{V_1}\right)} \end{aligned}$$



Carnot cycle

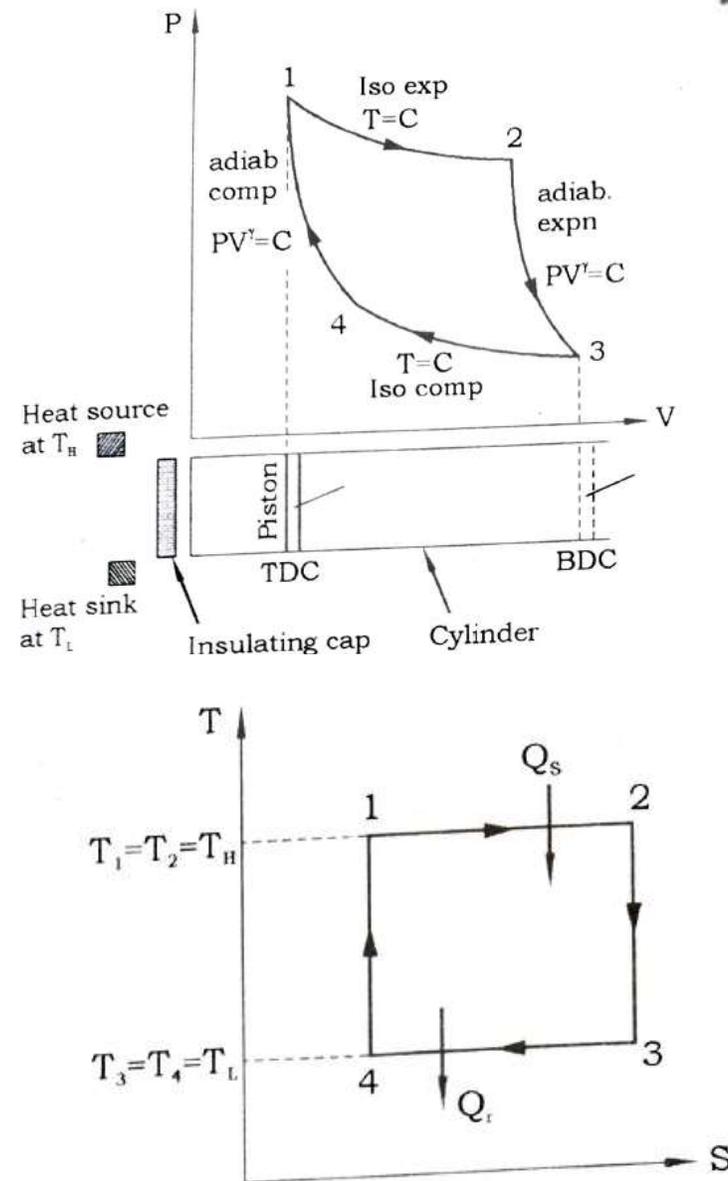
Consider equation (2) $\frac{T_2}{T_3} = \left(\frac{V_3}{V_2}\right)^{\gamma-1}$

But, from t-s diagram, $T_2 = T_1$ and $T_3 = T_4$

$$\therefore \frac{T_1}{T_4} = \left(\frac{V_3}{V_2}\right)^{\gamma-1}$$

we have $\left(\frac{V_1}{V_4}\right)^{\gamma-1} = \left(\frac{V_2}{V_3}\right)^{\gamma-1}$

$$\frac{V_1}{V_4} = \frac{V_2}{V_3} \quad \text{or} \quad \frac{V_3}{V_4} = \frac{V_2}{V_1}$$

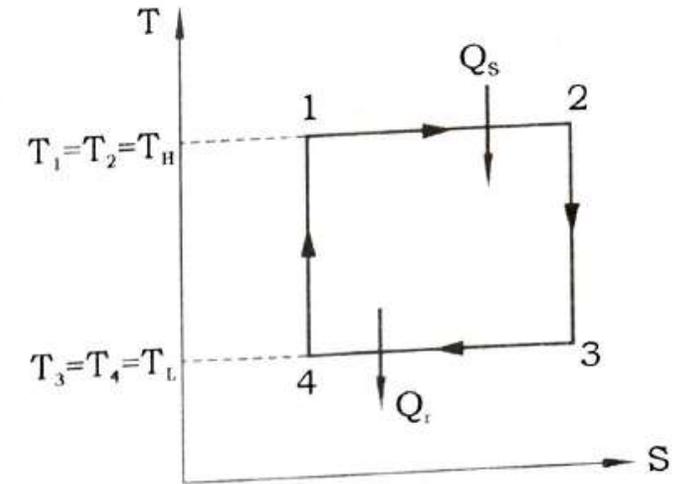


Carnot cycle

, we get
$$\eta_{\text{air}} = 1 - \frac{m \cdot R T_3 \ln\left(\frac{V_2}{V_1}\right)}{m \cdot R T_1 \ln\left(\frac{V_2}{V_1}\right)} = 1 - \frac{T_3}{T_1}$$

$$\eta_{\text{air}} = 1 - \frac{T_L}{T_H} \quad \text{for Carnot cycle}$$

where $T_L = T_3 = T_4 =$ Lowest temperature of the cycle, and
 $T_H = T_1 = T_2 =$ highest temperature of the cycle



Otto cycle (constant volume cycle)

Expression for air standard efficiency in Otto cycle

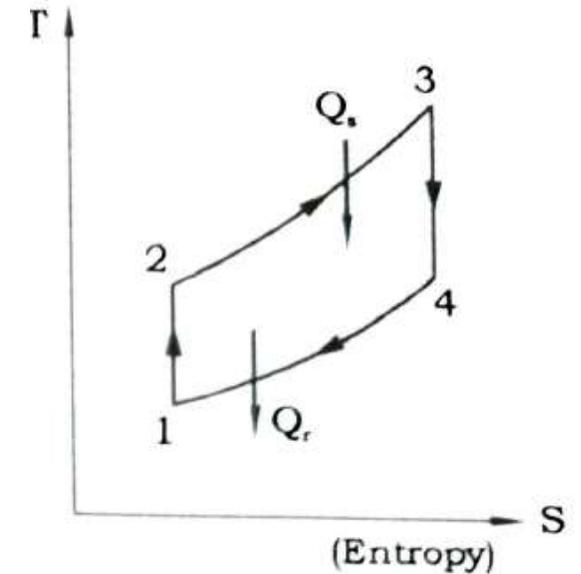
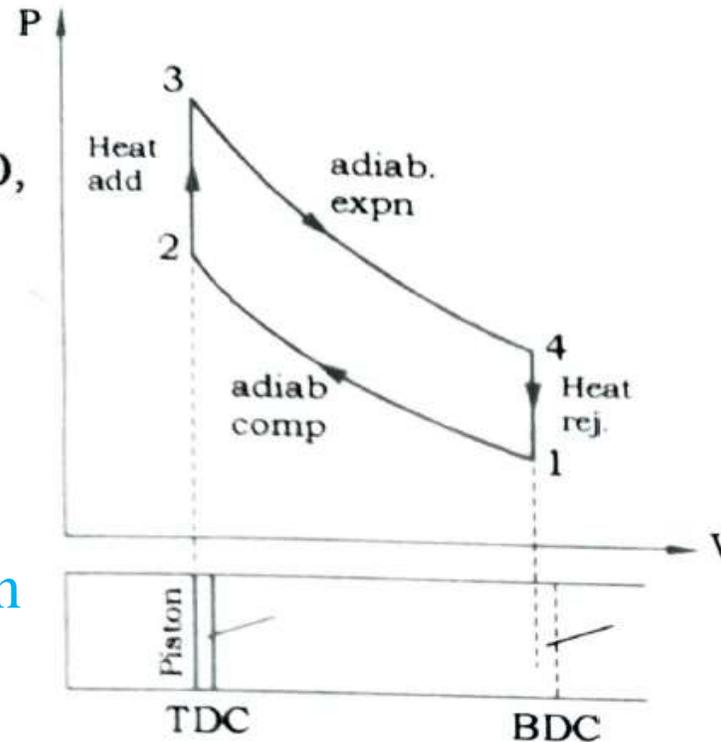
Process 1-2: Adiabatic compression

w.k.t. for adiabatic process, heat transfer $Q = 0$,

$$\frac{T_1}{T_2} = \left(\frac{V_2}{V_1}\right)^{\gamma-1} \quad \text{-----(1)}$$

Process 2-3: constant volume heat addition

$$\text{Heat supplied } Q_s = mC_v (T_3 - T_2) \quad \text{-----(2)}$$



Otto cycle (constant volume cycle)

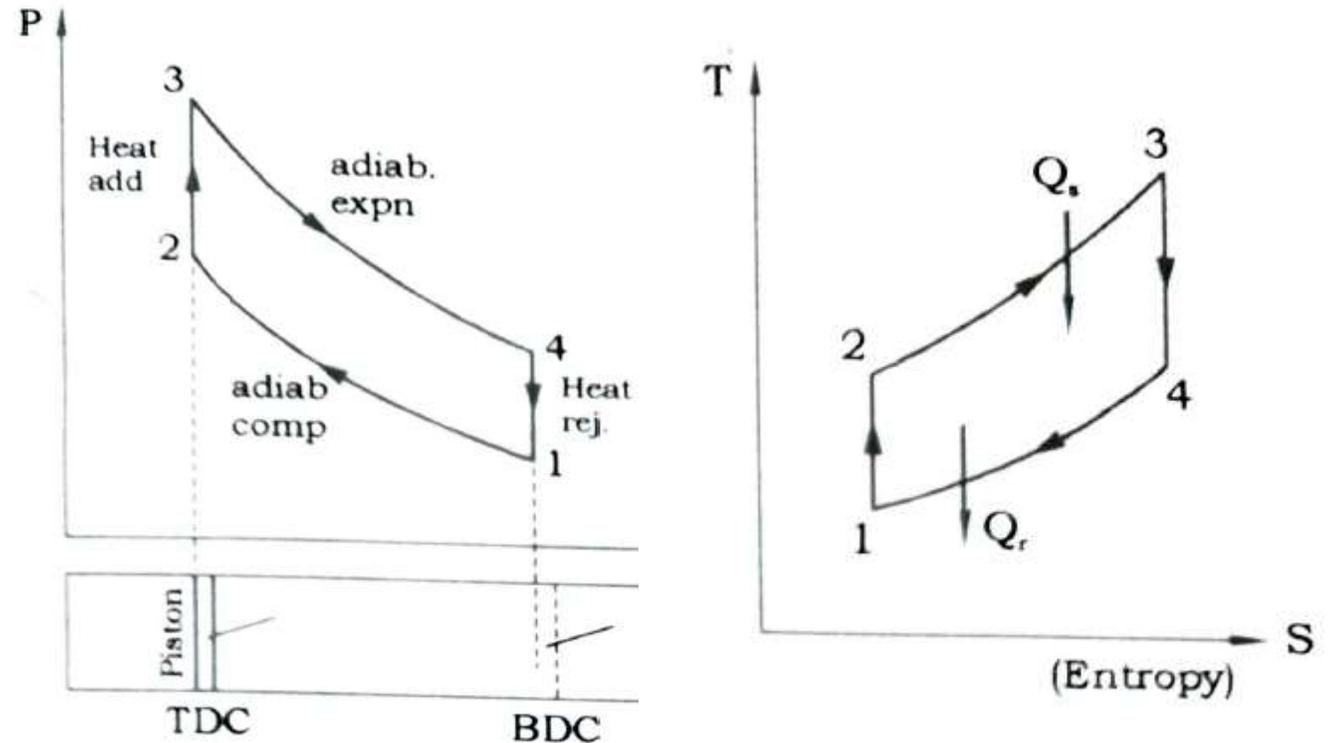
Process 3-4: Adiabatic Expansion

w.k.t. for adiabatic process, heat transfer $Q = 0$,

$$\frac{T_3}{T_4} = \left(\frac{V_4}{V_3} \right)^{\gamma-1} \quad \text{-----(3)}$$

Process 4-1: constant volume heat rejection

$$\text{Heat rejected } Q_r = mC_v (T_4 - T_1) \quad \text{-----(4)}$$



Otto cycle (constant volume cycle)

To find air standard efficiency:

$$\text{w.k.t. efficiency } \eta_{\text{air}} = \frac{\text{Work done}}{\text{Heat supplied}}$$

$$= \frac{\text{Heat supplied} - \text{Heat rejected}}{\text{Heat supplied}}$$

$$= \frac{Q_s - Q_r}{Q_s}$$

$$\text{i.e., } \eta_{\text{air}} = 1 - \frac{Q_r}{Q_s} = 1 - \frac{mC_v(T_4 - T_1)}{mC_v(T_3 - T_2)}$$

$$\eta_{\text{air}} = 1 - \frac{(T_4 - T_1)}{(T_3 - T_2)}$$

$$= 1 - \frac{\left(\frac{T_4}{T_1} - 1\right)T_1}{\left(\frac{T_3}{T_2} - 1\right)T_2}$$

$$\text{From equation (1) we have } \frac{T_1}{T_2} = \left(\frac{V_2}{V_1}\right)^{\gamma-1}$$

$$\text{But } V_2 = V_3 \text{ and } V_1 = V_4$$

$$\therefore \frac{T_1}{T_2} = \left(\frac{V_3}{V_4}\right)^{\gamma-1} \quad \text{or} \quad \frac{T_2}{T_1} = \left(\frac{V_4}{V_3}\right)^{\gamma-1}$$

Otto cycle (constant volume cycle)

we have $\frac{T_3}{T_4} = \frac{T_2}{T_1}$

$$\frac{T_4}{T_1} = \frac{T_3}{T_2}$$

$$\eta_{\text{air}} = 1 - \frac{\left(\frac{T_3}{T_2} - 1\right) T_1}{\left(\frac{T_3}{T_2} - 1\right) T_2}$$

$$= 1 - \frac{T_1}{T_2}$$

Defining compression ratio $R_c = \frac{V_1}{V_2}$,

we have from equation (1),

$$\frac{T_1}{T_2} = \left(\frac{1}{R_c}\right)^{\gamma-1} \quad \text{or} \quad \frac{T_1}{T_2} = \frac{1}{(R_c)^{\gamma-1}}$$

we get $\eta_{\text{air}} = 1 - \frac{1}{(R_c)^{\gamma-1}}$ for Otto cycle

Mean Effective Pressure (MEP) for Otto cycle

Mathematically, $MEP = P_m = \frac{\text{Work done / cycle}}{\text{Swept volume}}$

$$= \frac{Q_s - Q_r}{V_1 - V_2}$$

$$= \frac{mC_v(T_3 - T_2) - mC_v(T_4 - T_1)}{V_1 - V_2}$$

$$MEP = \frac{mC_v[(T_3 - T_2) - (T_4 - T_1)]}{V_1 - V_2} \quad \text{-----(1)}$$

Mean Effective Pressure (MEP) for Otto cycle

Express temperatures T_2 , T_3 and T_4 in terms of T_1

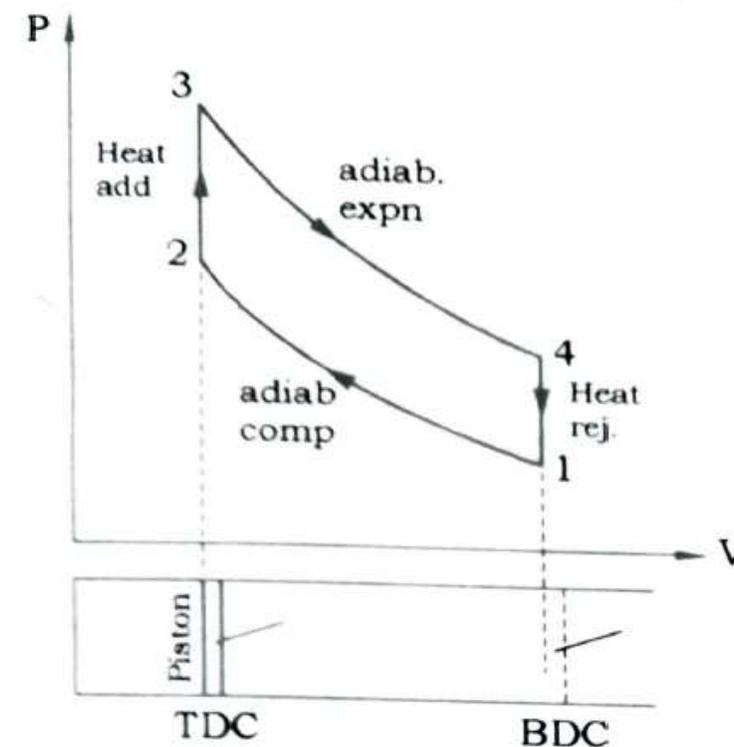
$$\frac{T_1}{T_2} = \left(\frac{V_2}{V_1}\right)^{\gamma-1} \quad \text{or} \quad \frac{T_1}{T_2} = \left(\frac{1}{R_c}\right)^{\gamma-1} \quad \left(\because R_c = \frac{V_1}{V_2}\right)$$

$$\therefore T_2 = T_1 \cdot (R_c)^{\gamma-1} \quad \text{-----(2)}$$

For constant volume process 2-3,

we have $\frac{P}{T} = \text{constant}$.

$$\frac{P_2}{T_2} = \frac{P_3}{T_3} \quad \text{or} \quad \frac{P_3}{P_2} = \frac{T_3}{T_2}$$



Mean Effective Pressure (MEP) for Otto cycle

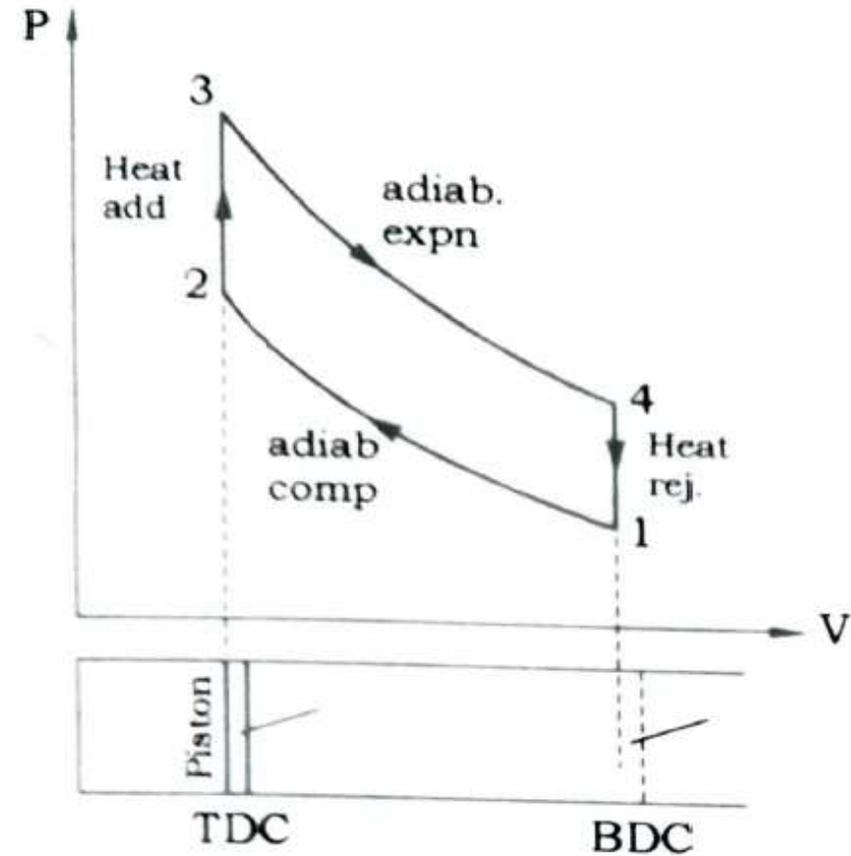
$$\therefore T_3 = T_2 \cdot \left(\frac{P_3}{P_2} \right) = T_2 \alpha$$

where α = explosion ratio or pressure ratio = $\frac{P_3}{P_2}$

$$T_3 = T_1 (R_C)^{\gamma-1} \cdot \alpha \quad \text{from equation (2)} \quad \text{-----(3)}$$

For adiabatic process 3-4, we have, $\frac{T_3}{T_4} = \left(\frac{V_4}{V_3} \right)^{\gamma-1}$

But $V_4 = V_1$ & $V_3 = V_2$



Mean Effective Pressure (MEP) for Otto cycle

$$\therefore \frac{T_3}{T_4} = \left(\frac{V_1}{V_2}\right)^{\gamma-1} \quad \text{or} \quad \frac{T_3}{T_4} = (R_c)^{\gamma-1} \quad \text{-----(5)}$$

$$= \frac{mC_v \cdot T_1 \left[(\alpha \cdot R_c^{\gamma-1} - R_c^{\gamma-1}) - (\alpha - 1) \right]}{(V_1 - V_2)}$$

$$T_4 = \frac{T_3}{(R_c)^{\gamma-1}} = \frac{T_1 \cdot (R_c)^{\gamma-1} \cdot \alpha}{(R_c)^{\gamma-1}} \quad \text{from equation (3)}$$

Under ideal conditions, at point (1),

$$\therefore T_4 = T_1 \alpha \quad \text{-----(4)}$$

we have $P_1 V_1 = mRT_1$, $V_1 = \frac{mRT_1}{P_1}$ -----(6)

Substituting equations (2), (3) and (4) in (1), we have

compression ratio $R_c = \frac{V_1}{V_2}$

$$MEP = \frac{mC_v \left\{ \left[T_1 (R_c)^{\gamma-1} \cdot \alpha - T_1 (R_c)^{\gamma-1} \right] \right\}}{(V_1 - V_2)}$$

$$\therefore V_2 = \frac{V_1}{R_c} = \frac{mRT_1}{P_1 \cdot R_c} \quad \text{from equation (6)} \quad \text{-----(7)}$$

Mean Effective Pressure (MEP) for Otto cycle

Substituting equations (6) and (7) in (5), we have

$$\text{MEP} = \frac{m \cdot C_v \cdot T_1 \left[\left(\alpha R_c^{\gamma-1} - R_c^{\gamma-1} \right) - (\alpha - 1) \right]}{\frac{mRT_1}{P_1} - \frac{mRT_1}{P_1 R_c}} = \frac{m \cdot C_v \cdot T_1 \left[R_c^{\gamma-1} (\alpha - 1) - (\alpha - 1) \right]}{\frac{mRT_1}{P_1} \left[1 - \frac{1}{R_c} \right]}$$

$$\text{MEP} = \frac{P_1 C_v (\alpha - 1) \left[R_c^{\gamma-1} - 1 \right]}{R \left[\frac{R_c - 1}{R_c} \right]}$$

----- (8)

w.k.t. Gas constant $R = C_p - C_v$

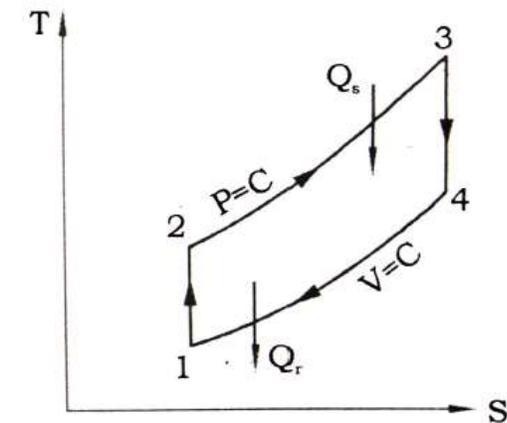
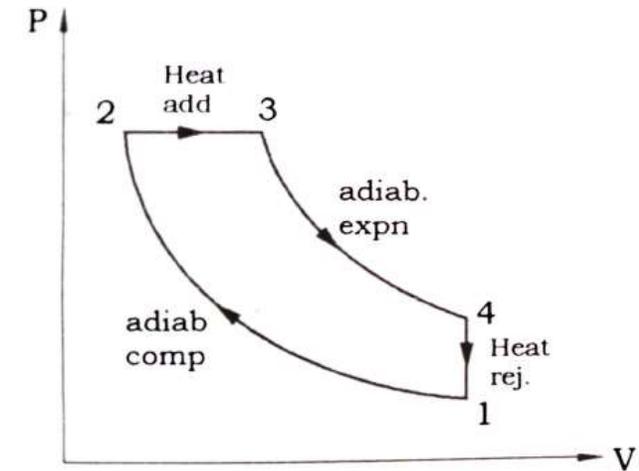
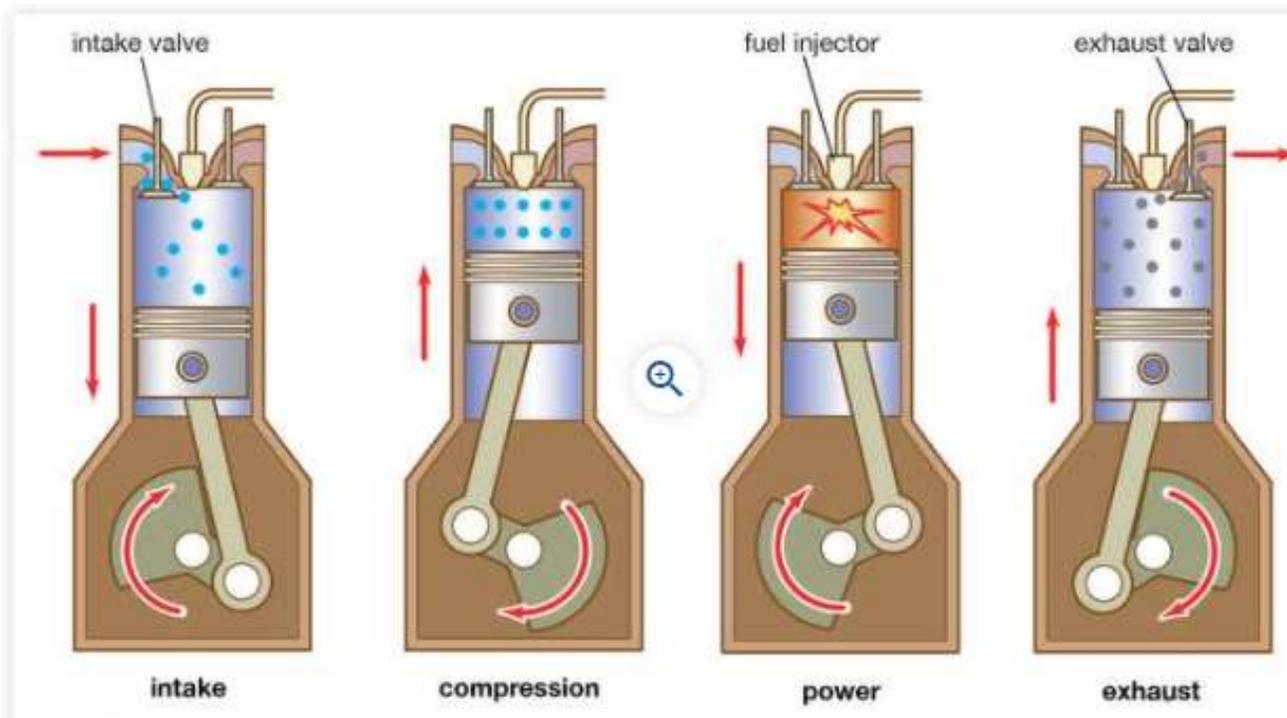
$$\frac{R}{C_v} = \frac{C_p}{C_v} - 1$$

$$\frac{R}{C_v} = \gamma - 1 \quad \therefore \frac{C_v}{R} = \frac{1}{\gamma - 1}$$

$$\text{MEP} = P_m = \frac{P_1 \cdot R_c (\alpha - 1) R_c^{\gamma-1} - 1}{(\gamma - 1)(R_c - 1)}$$

Diesel cycle (Constant Pressure cycle)

Expression for air standard efficiency in Diesel cycle

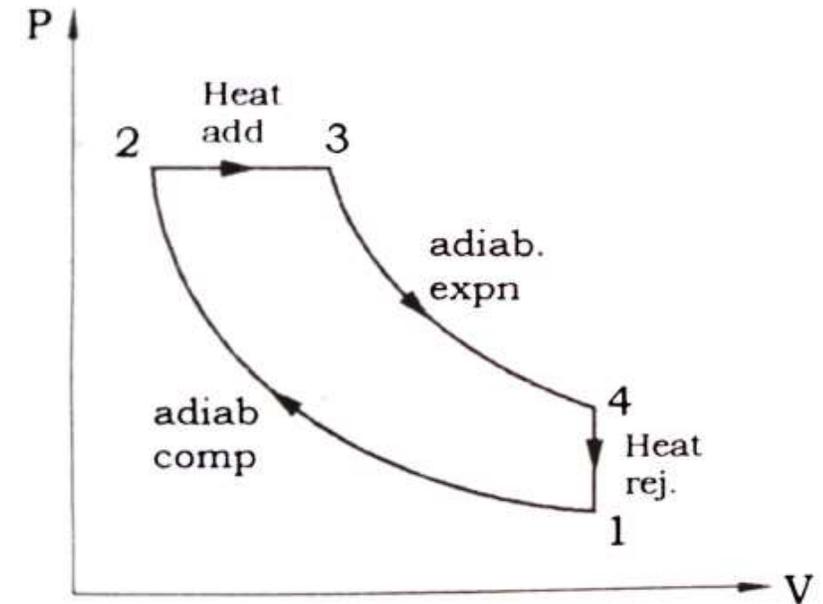


Diesel cycle (constant Pressure cycle)

Process 1-2: Adiabatic compression

heat transfer $Q = 0$, and $\frac{T_1}{T_2} = \left(\frac{V_2}{V_1}\right)^{\gamma-1}$ -----(1)

Process 2-3: constant Pressure heat addition



Heat supplied at constant pressure = $Q_s = mC_p (T_3 - T_2)$ -----(2)

Diesel cycle (constant Pressure cycle)

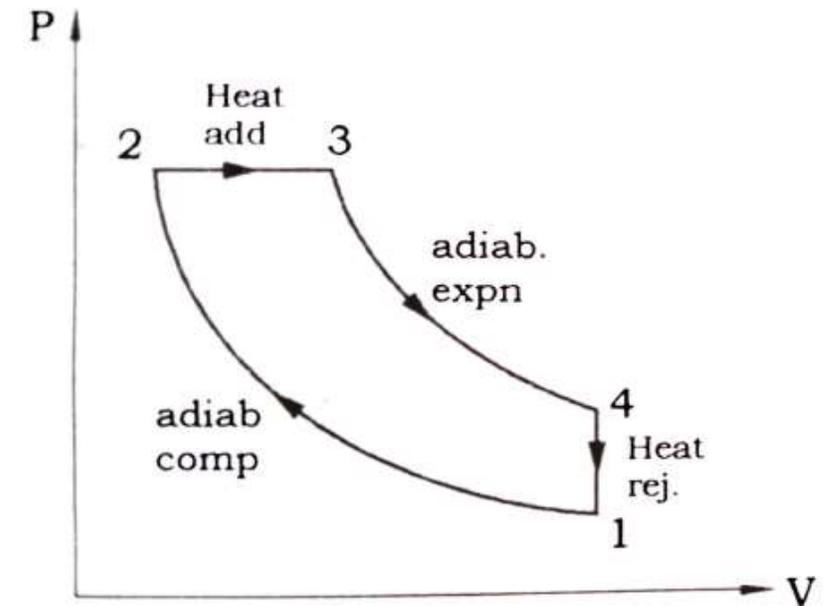
Process 3-4: Adiabatic Expansion

w.k.t. for adiabatic process, heat transfer $Q = 0$,

$$\frac{T_3}{T_4} = \left(\frac{V_4}{V_3} \right)^{\gamma-1} \quad \text{-----(3)}$$

Process 4-1: constant volume heat rejection

$$\text{Heat rejected } Q_r = mC_v (T_4 - T_1) \quad \text{-----(4)}$$



Diesel cycle (constant Pressure cycle)

Express temperatures T_2 , T_3 and T_4 in terms of T_1

w.k.t. $\eta_{\text{air}} = \frac{\text{Work done}}{\text{Heat supplied}}$

$$= \frac{Q_s - Q_r}{Q_s} = 1 - \frac{Q_r}{Q_s}$$

$$\eta_{\text{air}} = 1 - \frac{mC_v(T_4 - T_1)}{m.C_p(T_3 - T_2)}$$

$$\frac{C_p}{C_v} = \gamma$$

$$\therefore \eta_{\text{air}} = 1 - \frac{1(T_4 - T_1)}{\gamma(T_3 - T_2)}$$

From equation (1), $\frac{T_1}{T_2} = \left(\frac{1}{R_c}\right)^{\gamma-1}$

$$\therefore R_c = \frac{V_1}{V_2} = \text{compression ratio}$$

$$T_2 = T_1 (R_c)^{\gamma-1}$$

For constant pressure process 2-3, $\frac{V}{T} = \text{constant}$

$$\frac{V_2}{T_2} = \frac{V_3}{T_3} \quad \text{or} \quad \frac{T_3}{T_2} = \frac{V_3}{V_2}$$

Diesel cycle (constant Pressure cycle)

Defining cut-off ratio $\rho = \frac{V_3}{V_2}$,

$$T_3 = T_2 \left(\frac{V_3}{V_2} \right) = T_2 \rho$$

$$T_3 = T_1 (R_C)^{\gamma-1} \cdot \rho$$

From equation (3), $\frac{T_3}{T_4} = \left(\frac{V_1}{V_3} \right)^{\gamma-1}$

or $\frac{T_3}{T_4} = \left(\frac{V_1}{V_2} \cdot \frac{V_2}{V_3} \right)^{\gamma-1}$

$$\frac{T_3}{T_4} = R_C^{\gamma-1} \cdot \frac{1}{\rho^{\gamma-1}} \quad T_4 = T_3 \cdot \frac{\rho^{\gamma-1}}{(R_C)^{\gamma-1}}$$

we have $T_4 = T_1 \cdot (R_C)^{\gamma-1} \rho \frac{\rho^{\gamma-1}}{(R_C)^{\gamma-1}}$

$$\therefore T_4 = T_1 \rho^\gamma$$

$$\therefore \eta_{\text{air}} = 1 - \frac{1(T_4 - T_1)}{\gamma (T_3 - T_2)}$$

$$\eta_{\text{air}} = 1 - \frac{1}{\gamma} \frac{(T_1 \rho^\gamma - T_1)}{(T_1 R_C^{\gamma-1} \rho - T_1 R_C^{\gamma-1})}$$

$$= 1 - \frac{1}{\gamma} \frac{T_1 (\rho^\gamma - 1)}{T_1 R_C^{\gamma-1} (\rho - 1)}$$

$$\therefore \eta_{\text{air}} = 1 - \frac{1}{\gamma \cdot (R_C)^{\gamma-1}} \cdot \frac{(\rho^\gamma - 1)}{(\rho - 1)}$$

Mean Effective Pressure (MEP) for Diesel cycle

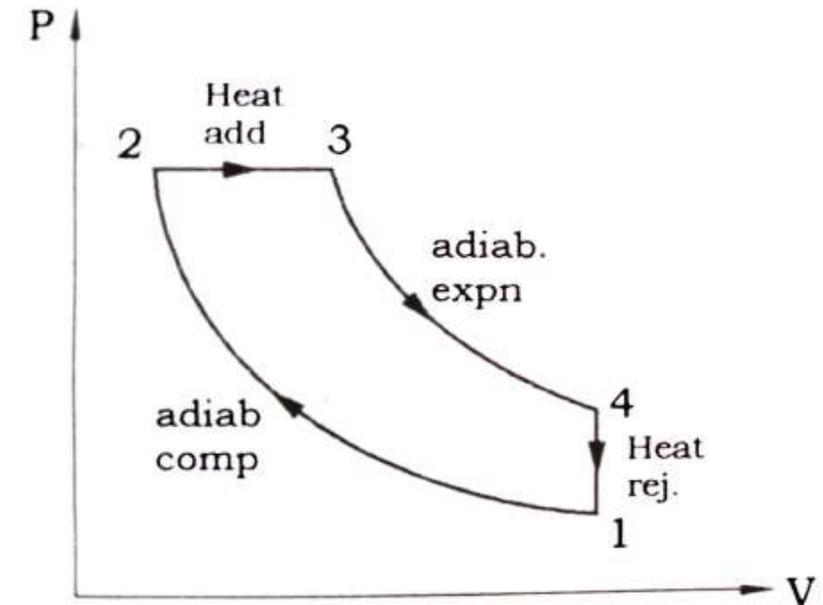
$$P_m = \frac{\text{Work done / cycle}}{\text{swept volume}}$$

$$= \frac{Q_s - Q_r}{V_1 - V_2}$$

$$= \frac{mC_p (T_3 - T_2) - mC_v (T_4 - T_1)}{V_1 - V_2}$$

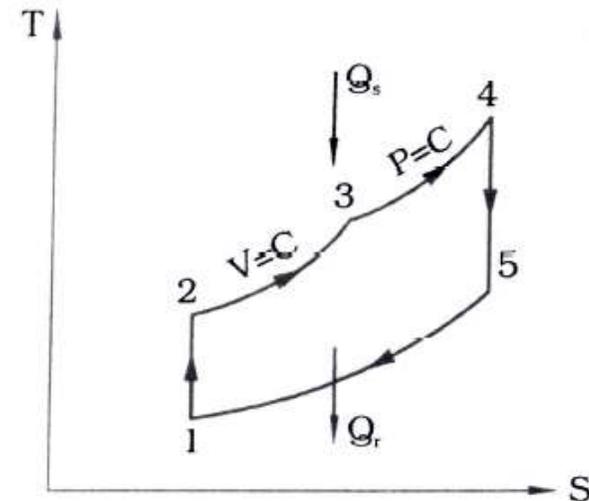
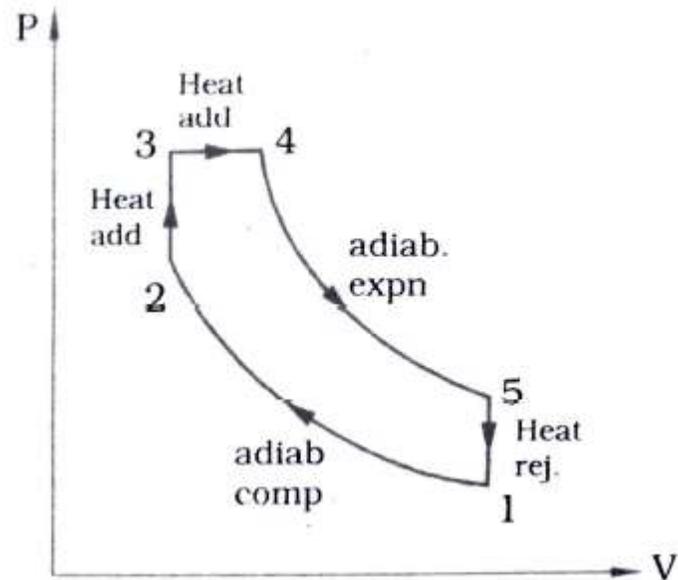
Express all temperature in terms of T_1

$$MEP = \frac{P_1 R_c \left\{ \gamma R_c^{\gamma-1} (\rho - 1) - \rho^\gamma - 1 \right\}}{(\gamma - 1)(R_c - 1)}$$



Dual Combustion Cycle (Semi- Diesel/Limited Pressure cycle)

Expression for air standard efficiency:



Dual Combustion Cycle (Semi- Diesel/Limited Pressure cycle)

Process 1-2: Adiabatic compression

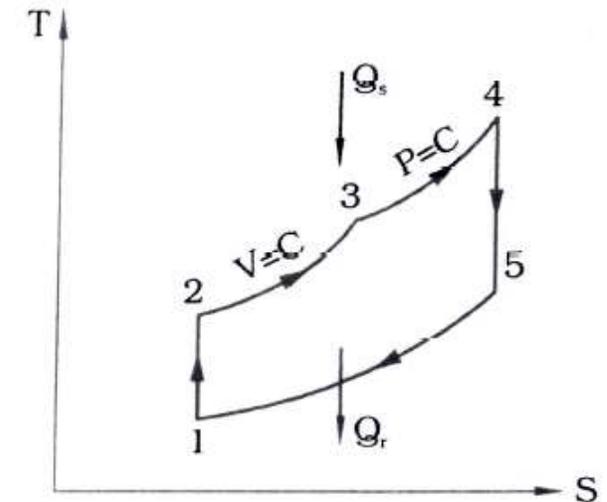
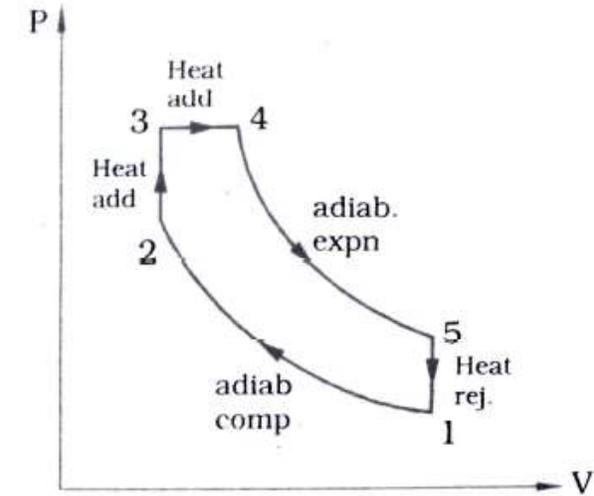
heat transfer $Q = 0$, and $\frac{T_1}{T_2} = \left(\frac{V_2}{V_1}\right)^{\gamma-1}$ -----(1)

Process 2-3: constant volume heat addition

Heat supplied $(Q_s)_{2,3} = mC_v (T_3 - T_2)$

Process 3-4: constant Pressure heat addition

Heat supplied $(Q_s)_{3,4} = mC_p (T_4 - T_3)$



Dual Combustion Cycle (Semi- Diesel/Limited Pressure cycle)

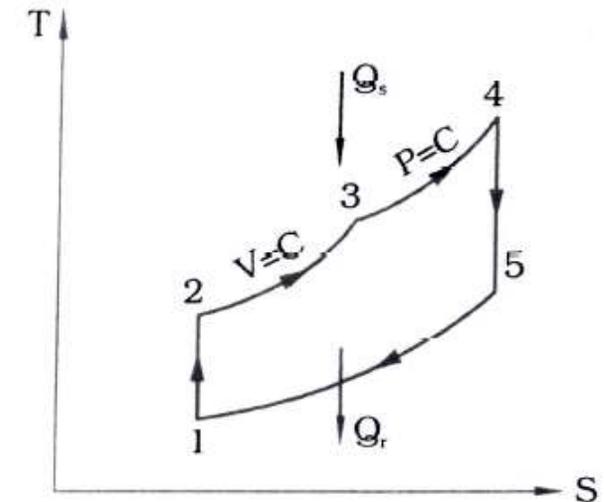
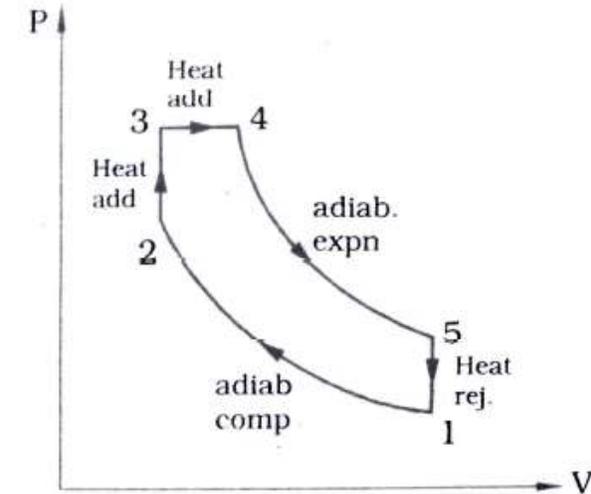
Process 4-5: Adiabatic Expansion

w.k.t. for adiabatic process, heat transfer, $Q = 0$,

$$\frac{T_4}{T_5} = \left(\frac{V_5}{V_4} \right)^{\gamma-1}$$

Process 5-1: constant volume heat rejection

$$\therefore \text{Heat rejected } Q_r = mC_v (T_5 - T_1)$$



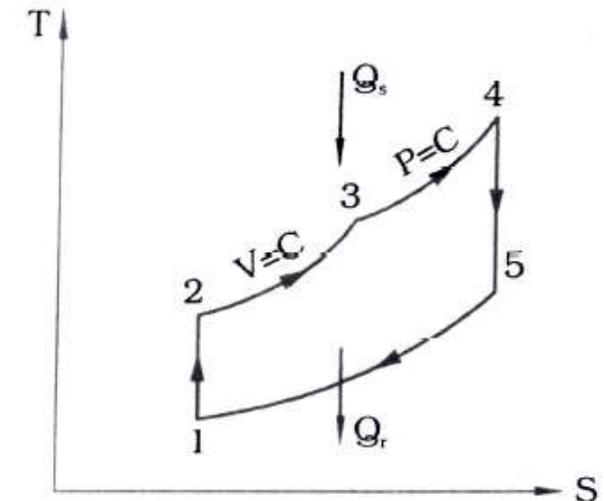
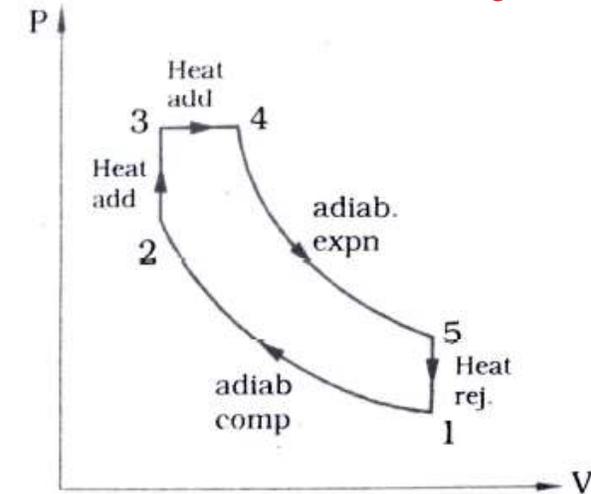
Dual Combustion Cycle (Semi- Diesel/Limited Pressure cycle)

w.k.t. $\eta_{air} = \frac{\text{Work done}}{\text{Heat supplied}}$

$$= \frac{Q_s - Q_r}{Q_s} = 1 - \frac{Q_r}{Q_s} = 1 - \frac{Q_r}{(Q_s)_{2-3} + (Q_s)_{3-4}}$$

$$, \eta_{air} = 1 - \frac{mC_v(T_5 - T_1)}{mC_v(T_3 - T_2) + mC_p(T_4 - T_3)}$$

$$= 1 - \frac{C_v(T_5 - T_1)}{C_v(T_3 - T_2) + C_p(T_4 - T_3)}$$



Dual Combustion Cycle (Semi- Diesel/Limited Pressure cycle)

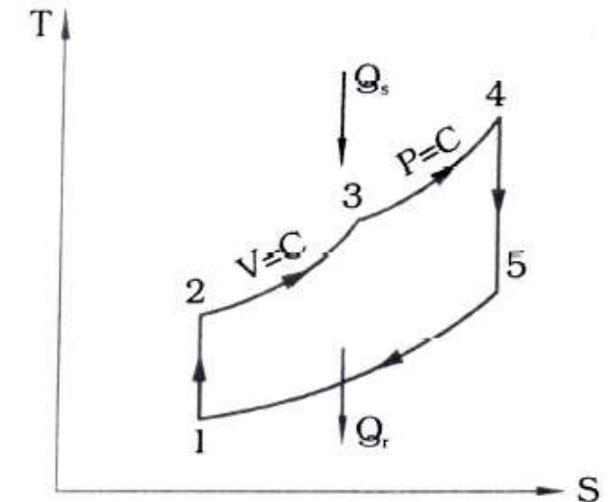
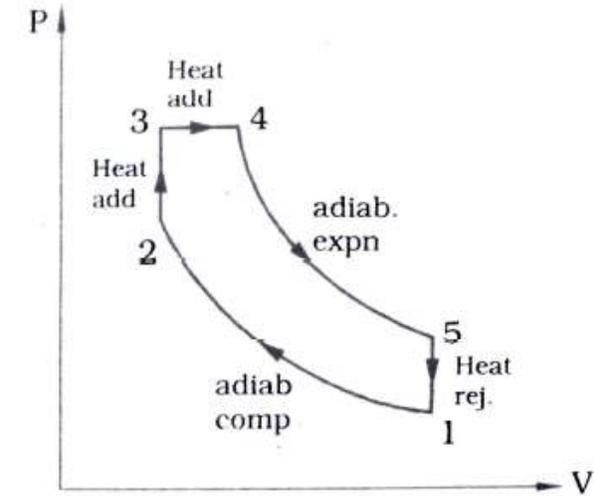
Express all temperatures in terms of T_1

we have $\frac{T_1}{T_2} = \left(\frac{1}{R_c}\right)^{\gamma-1}$ where $R_c = \frac{V_1}{V_2}$ = compression ratio

we have $\frac{T_4}{T_5} = \left(\frac{V_1}{V_4}\right)^{\gamma-1}$ $\because V_5 = V_1$

$$\frac{T_4}{T_5} = \left(\frac{V_1}{V_2} \times \frac{V_2}{V_4}\right)^{\gamma-1}$$

$$\frac{T_4}{T_5} = \left(\frac{V_1}{V_2} \times \frac{V_3}{V_4}\right)^{\gamma-1} \quad \because V_2 = V_3$$



Dual Combustion Cycle (Semi- Diesel/Limited Pressure cycle)

$$\frac{T_4}{T_5} = \left(R_c \times \frac{1}{\rho} \right)^{\gamma-1}$$

$$\therefore \frac{V_4}{V_3} = \rho \text{ cut-off ratio}$$

$$T_4 = T_5 \left[R_c^{\gamma-1} \cdot \rho^{1-\gamma} \right]$$

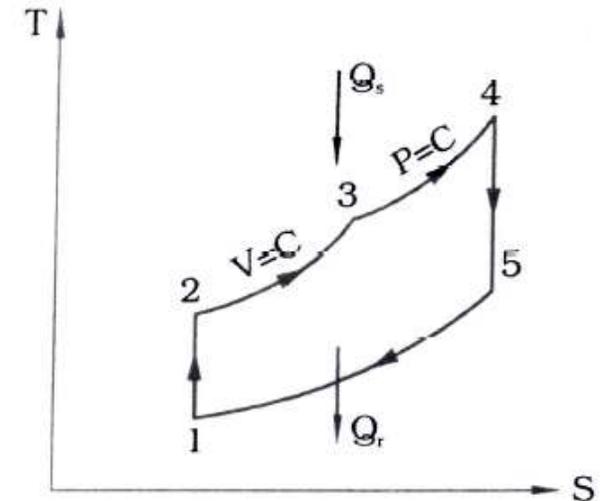
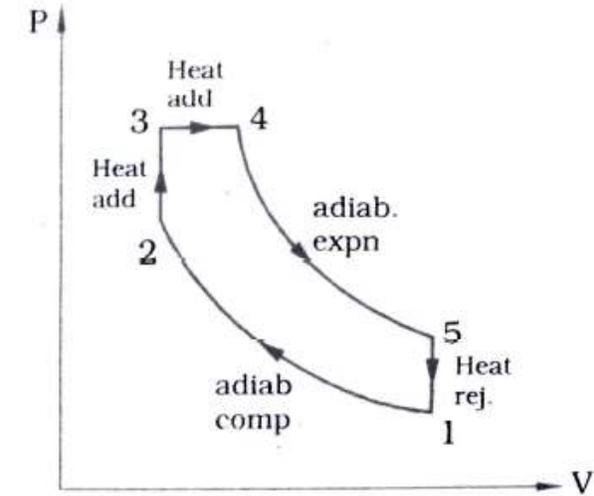
For constant volume process 2-3,

we have $\frac{P}{T} = \text{constant}$

$$\frac{P_2}{T_2} = \frac{P_3}{T_3} \quad \text{or} \quad T_3 = T_2 \left(\frac{P_3}{P_2} \right)$$

$$= T_2 (\alpha)$$

$$\text{where } \alpha = \text{explosion ratio} = \frac{P_3}{P_2}$$



Dual Combustion Cycle (Semi- Diesel/Limited Pressure cycle)

we have, $T_3 = T_1 \cdot (R_C)^{\gamma-1} \cdot \alpha$

For constant pressure process 3-4,

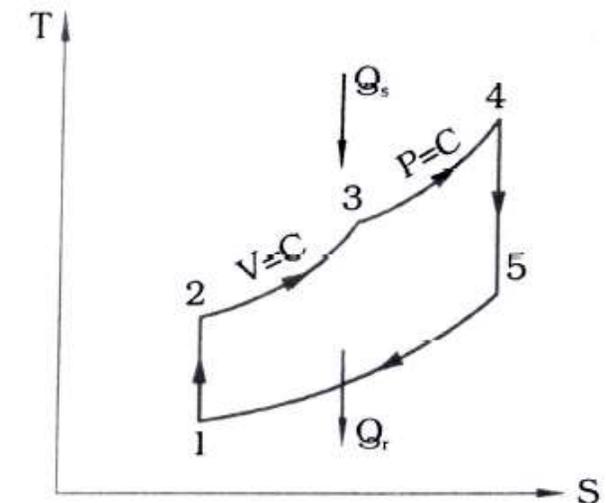
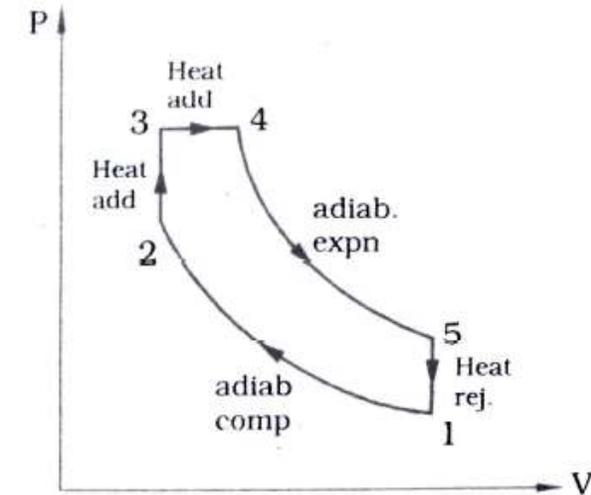
we have $\frac{V}{T} = \text{constant}$.

$$T_4 = T_3 \left(\frac{V_4}{V_3} \right) = T_3 (\rho)$$

we have $T_4 = T_1 \cdot (R_C)^{\gamma-1} \cdot \alpha \cdot \rho$

we have $T_1 \cdot (R_C)^{\gamma-1} \cdot \alpha \cdot \rho = T_5 \cdot (R_C)^{\gamma-1} \cdot \rho^{1-\gamma}$

$$\begin{aligned} T_5 &= \frac{T_1 \alpha \rho}{\rho^{1-\gamma}} \\ &= T_1 \alpha \rho^\gamma \end{aligned}$$



Dual Combustion Cycle (Semi- Diesel/Limited Pressure cycle)

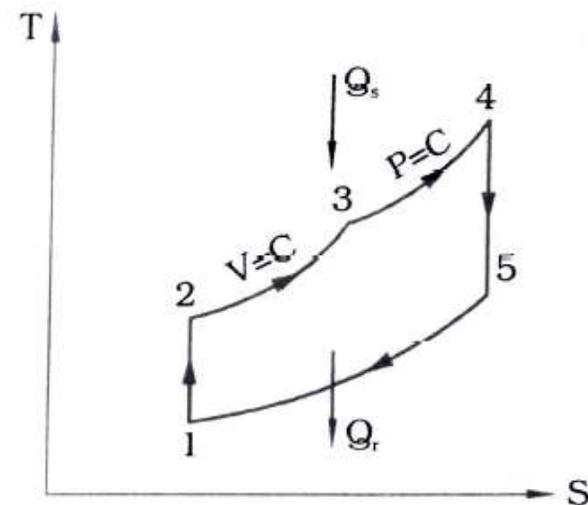
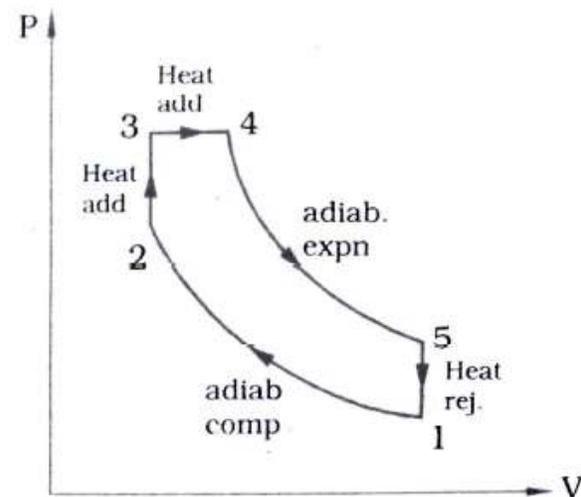
Substituting T_2 , T_3 , T_4 and T_5 in equation (6), we have

$$\eta_{\text{air}} = 1 - \frac{C_v T_1 \alpha \rho^\gamma - T_1}{C_v T_1 R_C^{\gamma-1} \cdot \alpha - T_1 R_C^{\gamma-1} + C_p T_1 R_C^{\gamma-1} \cdot \alpha \rho - T_1 R_C^{\gamma-1} \cdot \alpha}$$

$$= 1 - \frac{T_1 \alpha \rho^\gamma - 1}{T_1 R_C^{\gamma-1} \cdot \alpha - R_C^{\gamma-1} + \frac{C_p}{C_v} \cdot T_1 R_C^{\gamma-1} \cdot \alpha \rho - R_C^{\gamma-1} \cdot \alpha}$$

$$= 1 - \frac{\alpha \rho^\gamma - 1}{R_C^{\gamma-1} (\alpha - 1) + \gamma \cdot R_C^{\gamma-1} \cdot \alpha (\rho - 1)}$$

$$\eta_{\text{air}} = 1 - \frac{1}{R_C^{\gamma-1}} \frac{\alpha \cdot \rho^\gamma - 1}{(\alpha - 1) + \alpha \gamma (\rho - 1)}$$



Dual Combustion Cycle (Semi- Diesel/Limited Pressure cycle)

$$\text{MEP} = \frac{P_1 R_C}{(R_C - 1)(\gamma - 1)} R_C^{\gamma-1} (\alpha - 1) + \alpha \cdot \gamma R_C^{\gamma-1} (\rho - 1) - (\alpha \cdot \rho^\gamma - 1)$$

Comparison of Otto, Diesel and Dual Cycles

For same compression ratio and heat supplied

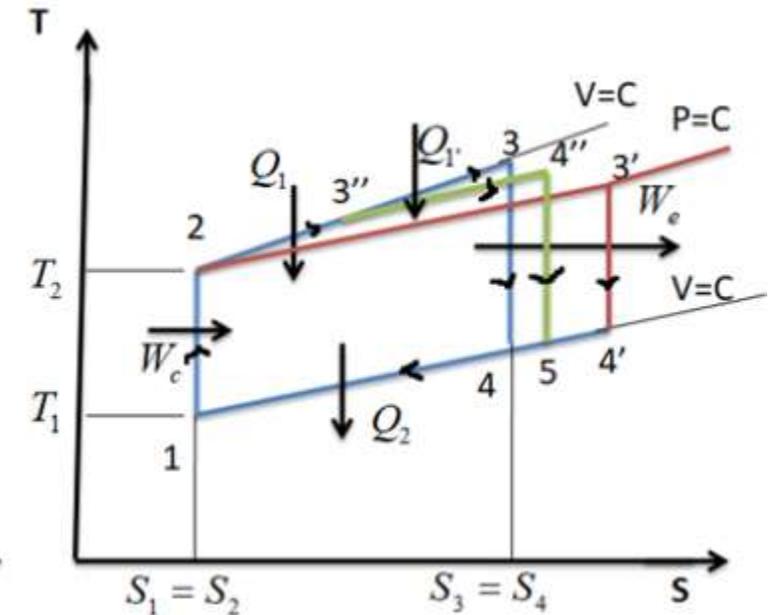
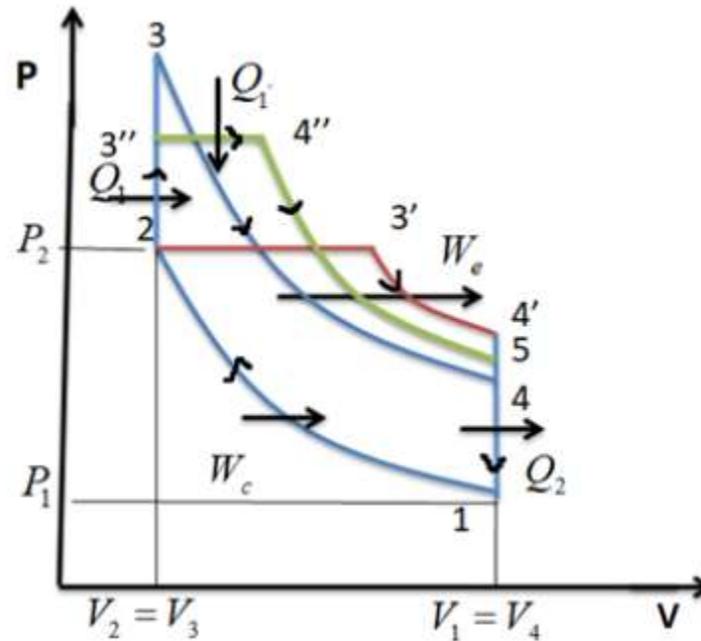
1-2-3-4 -1 is Otto cycle

1-2-3'-4'-1 is diesel cycle

1-2-3''-4''-5-1 is dual cycle

w.k.t. $\eta_{\text{air}} = \frac{\text{Work done}}{\text{Heat supplied}}$

$$= \frac{Q_s - Q_r}{Q_s} = 1 - \frac{Q_r}{Q_s}$$



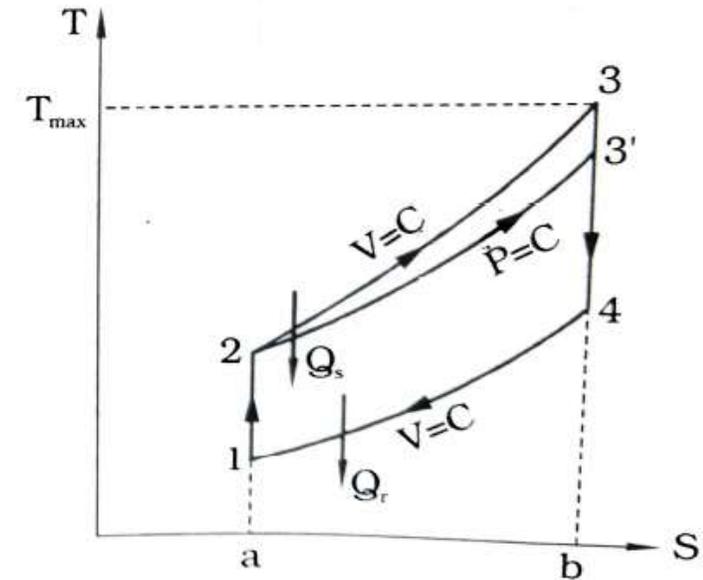
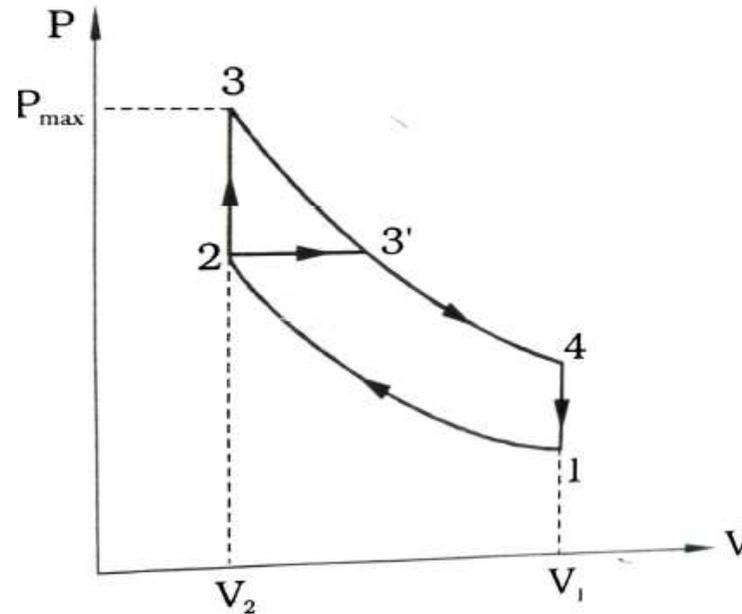
$$\therefore \eta_{\text{Otto}} > \eta_{\text{Dual}} > \eta_{\text{Diesel}}$$

Comparison of Otto, Diesel and Dual Cycles

Same compression ratio and heat rejection

w.k.t. $\eta_{\text{air}} = \frac{\text{Work done}}{\text{Heat supplied}}$

$$= \frac{Q_s - Q_r}{Q_s} = 1 - \frac{Q_r}{Q_s}$$



Otto Cycle : 1-2-3-4
Diesel Cycle : 1-2-3'-4

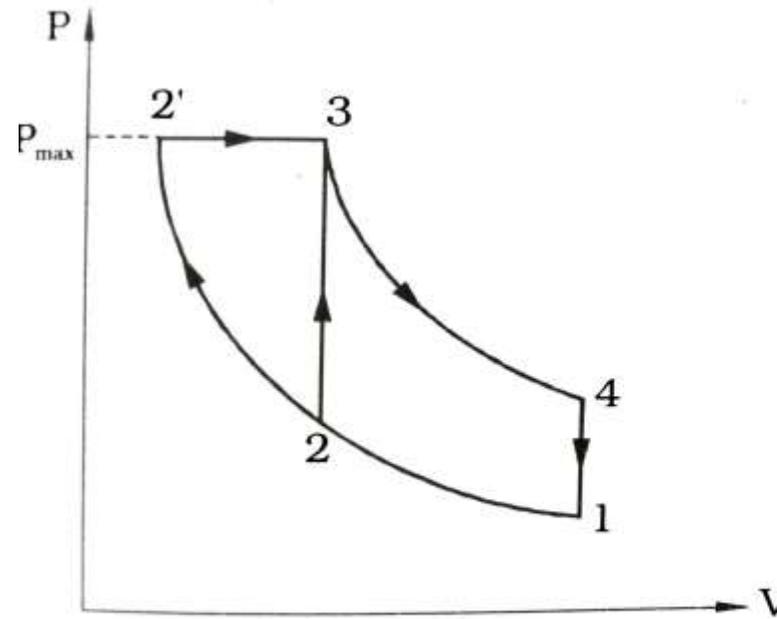
Otto cycle has a comparatively higher efficiency than Diesel cycle

Comparison of Otto, Diesel and Dual Cycles

For Same maximum pressure, maximum temperature and heat rejection

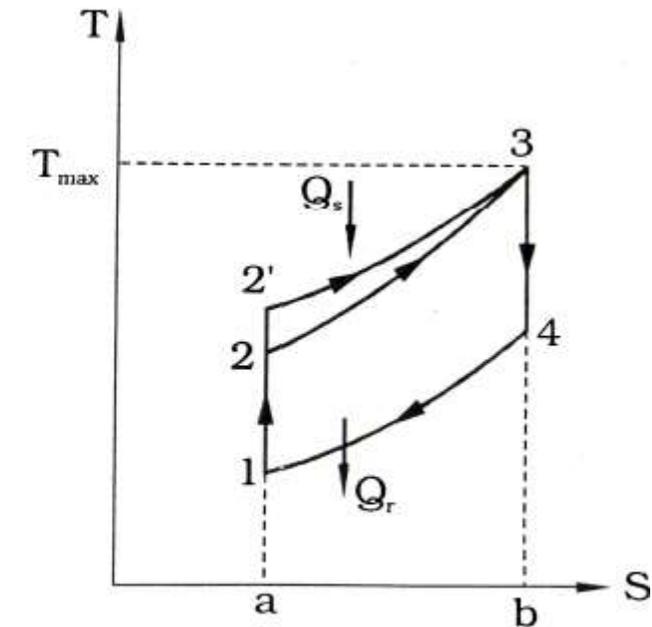
w.k.t. $\eta_{\text{air}} = \frac{\text{Work done}}{\text{Heat supplied}}$

$$= \frac{Q_s - Q_r}{Q_s} = 1 - \frac{Q_r}{Q_s}$$



Otto Cycle : 1-2-3-4

Diesel Cycle : 1-2'-3-4



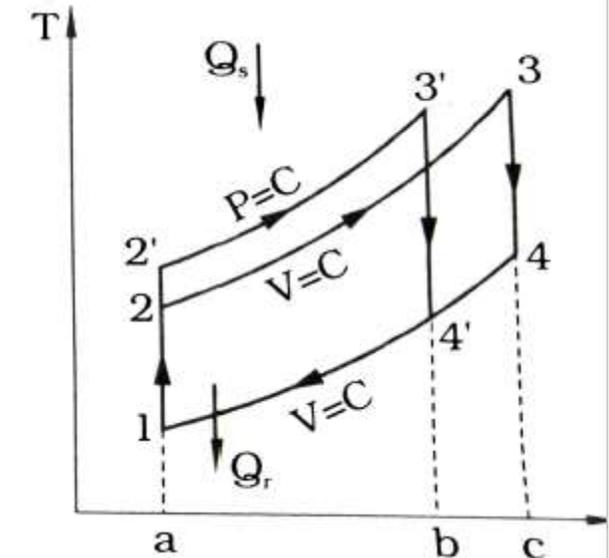
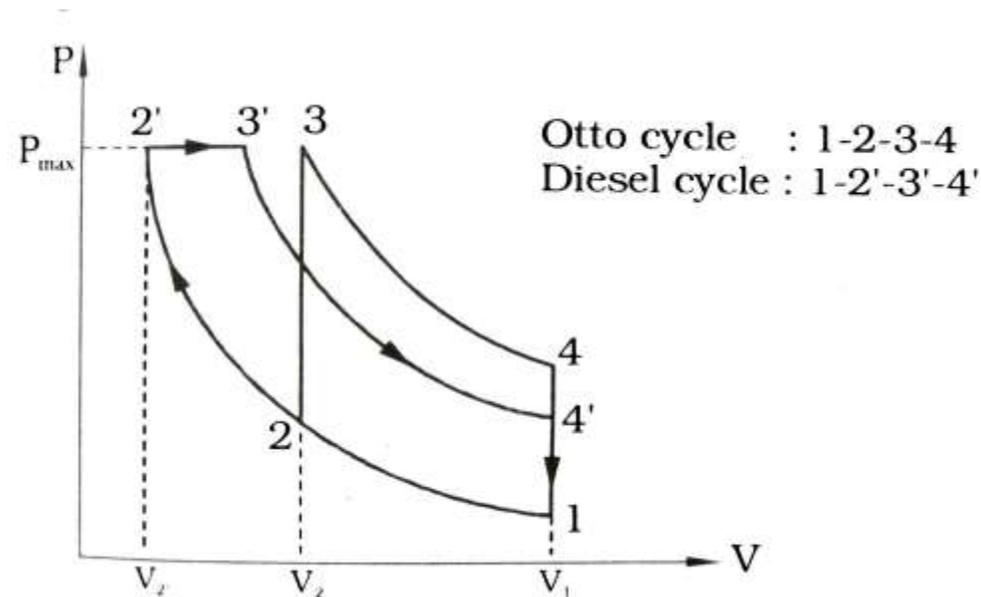
Diesel cycle has a comparatively higher efficiency than Otto cycle

Comparison of Otto, Diesel and Dual Cycles

- For Same maximum pressure and heat input

w.k.t. $\eta_{\text{air}} = \frac{\text{Work done}}{\text{Heat supplied}}$

$$= \frac{Q_s - Q_r}{Q_s} = 1 - \frac{Q_r}{Q_s}$$



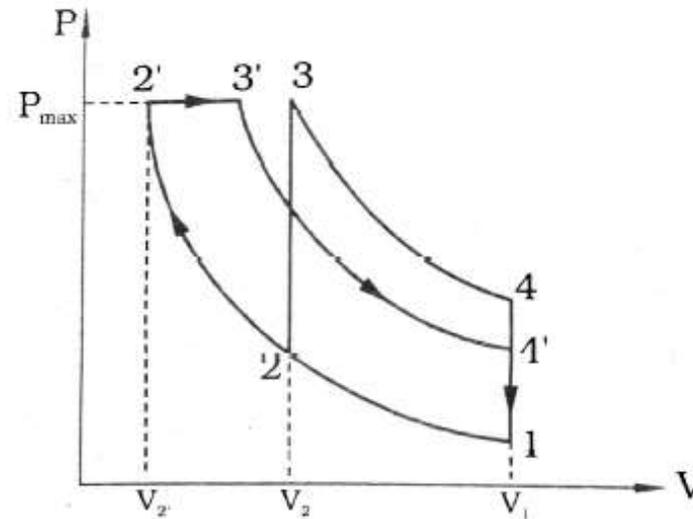
Diesel cycle is more efficient than Otto cycle

Comparison of Otto, Diesel and Dual Cycles

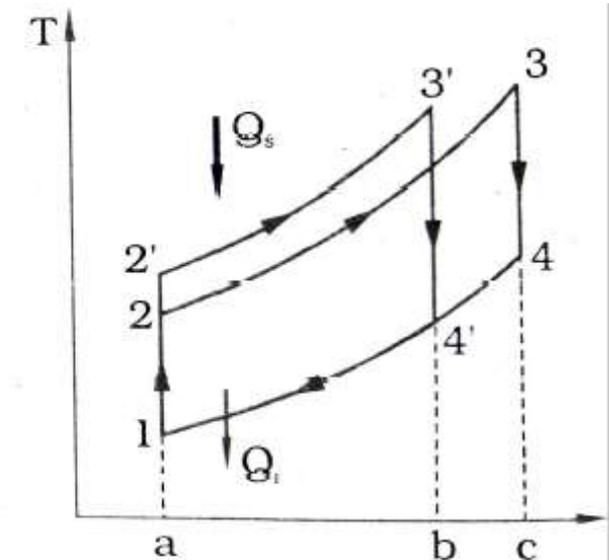
For Same maximum pressure and work output

w.k.t. $\eta_{\text{air}} = \frac{\text{Work done}}{\text{Heat supplied}}$

$$= \frac{Q_s - Q_r}{Q_s} = 1 - \frac{Q_r}{Q_s}$$



Otto cycle : 1-2-3-4
Diesel cycle : 1-2'-3'-4'

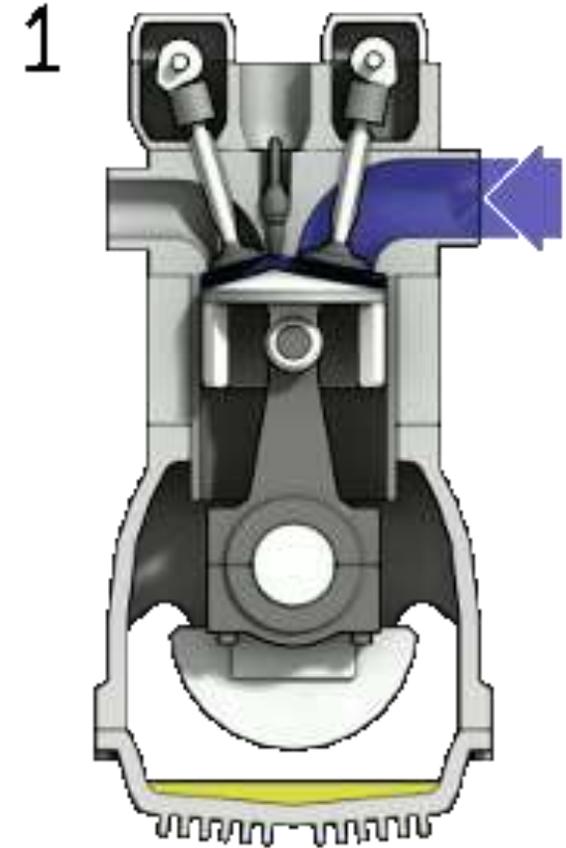
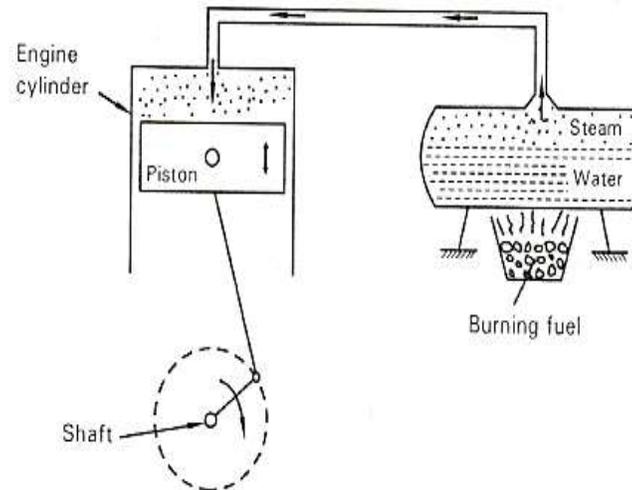


Diesel cycle is more efficient than Otto cycle

I.C ENGINE

Heat engine can be defined as a device or machine that converts the chemical energy of a fuel into heat energy by combustion of fuel, and utilizes this heat energy to perform useful mechanical work (usually in the form of rotation of shaft)

- Internal combustion engine
- External combustion engine





CLASSIFICATION OF IC ENGINE



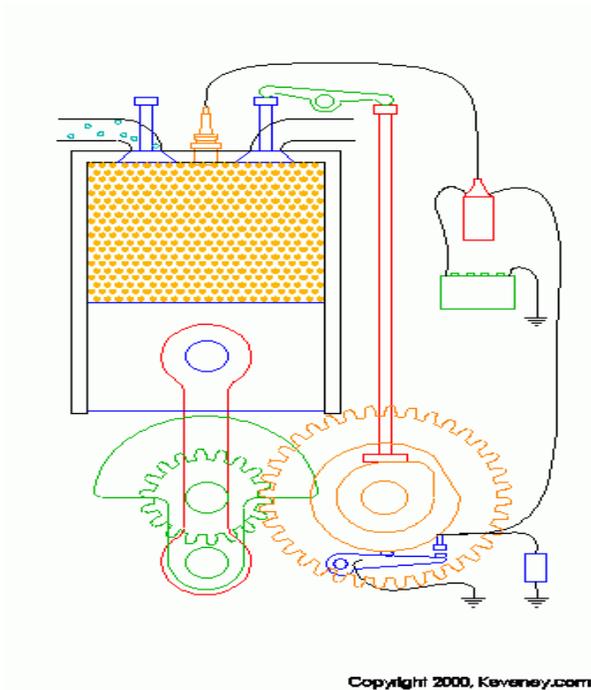
(1) According to the type of fuel used:

- a) Petrol engine
- b) Diesel engine
- c) Gas engine
- d) Bi-fuel (Bio-fuel) engine

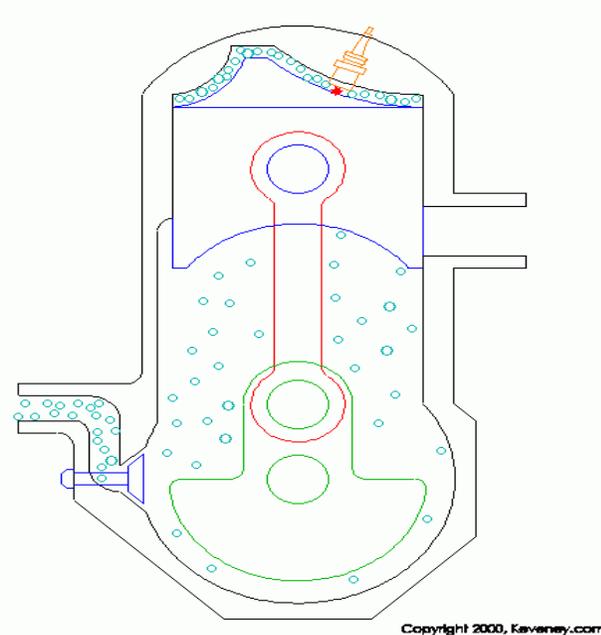
CLASSIFICATION OF IC ENGINE

(2) According to the number of strokes per cycle:

- 4-stroke engine



- 2-stroke engine



CLASSIFICATION OF IC ENGINE

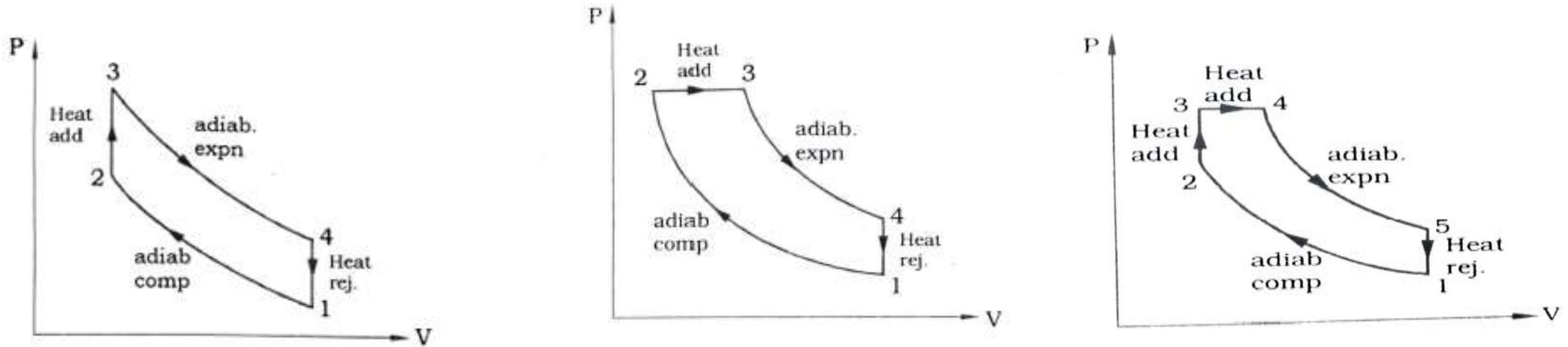
(3) According to the method of ignition:

- a) Spark Ignition (SI) engine
- b) Compression Ignition (CI) engine

CLASSIFICATION OF IC ENGINE

(4) According to the cycle of combustion:

- a) Otto cycle engine
- b) Diesel cycle engine
- c) Dual combustion cycle engine

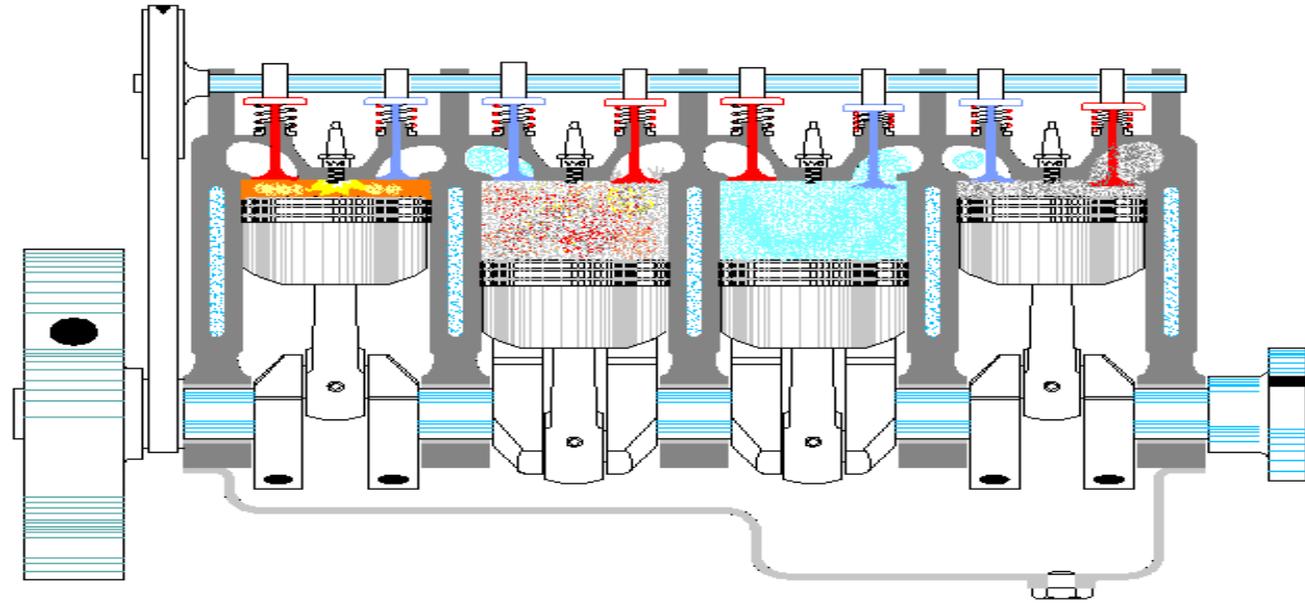


CLASSIFICATION OF IC ENGINE

(5) According to the number of cylinders used:

- a) Single cylinder engine
- b) Multi-cylinder engine

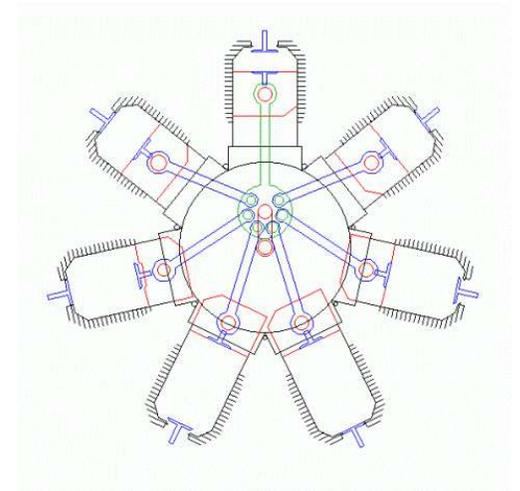
1



CLASSIFICATION OF IC ENGINE

(6) According to the arrangement of cylinders:

- a) Vertical engine
- b) Horizontal engine
- c) Inline engine
- d) Radial engine
- e) V-engine
- f) Opposed type engine



CLASSIFICATION OF IC ENGINE

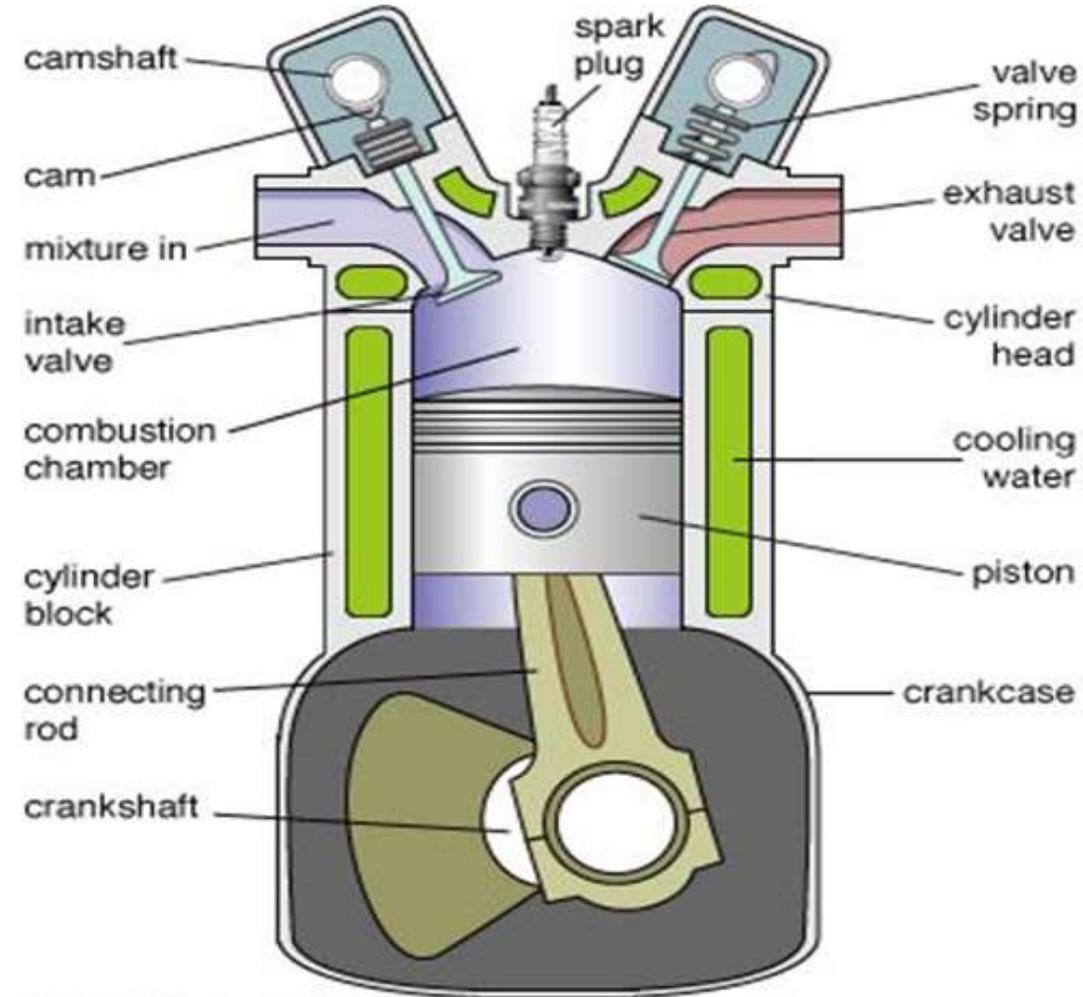
(7) According to the method of cooling:

- a) Air cooled engine
- b) Water cooled engine

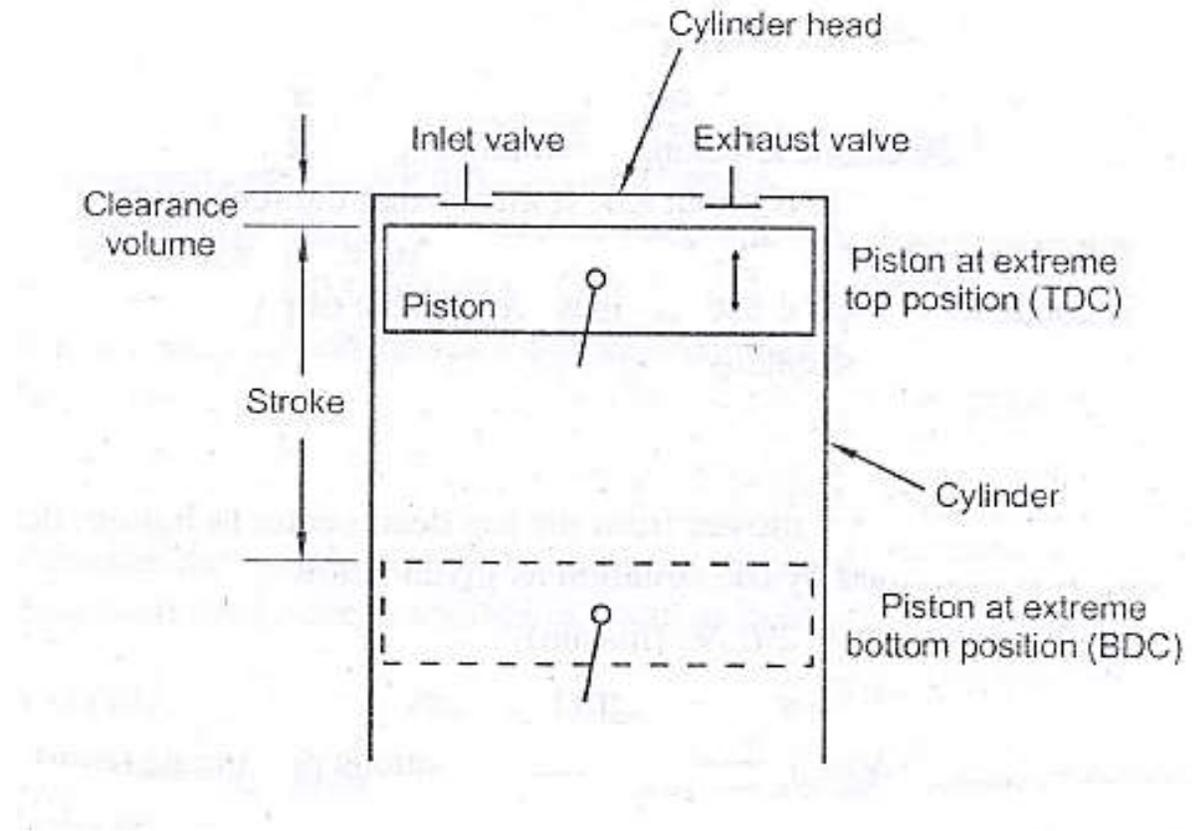
(8) According to their uses:

- a) Stationary engine
- b) Automobile engine
- c) Marine engine
- d) Aircraft engine, etc

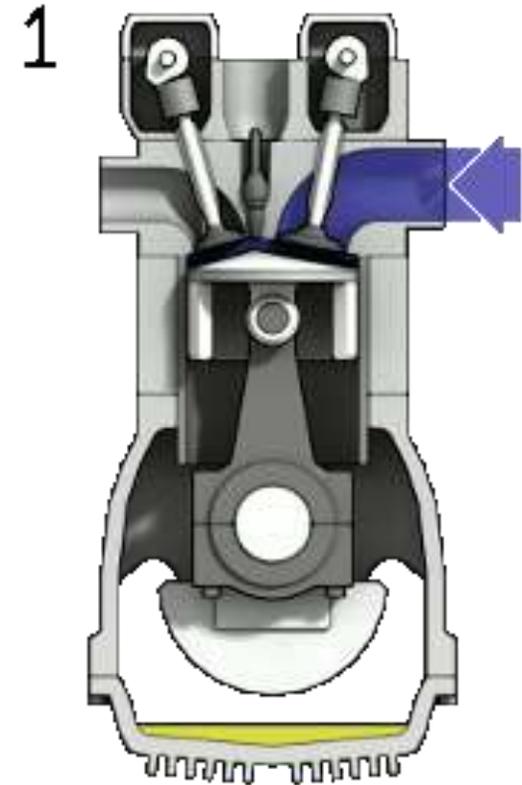
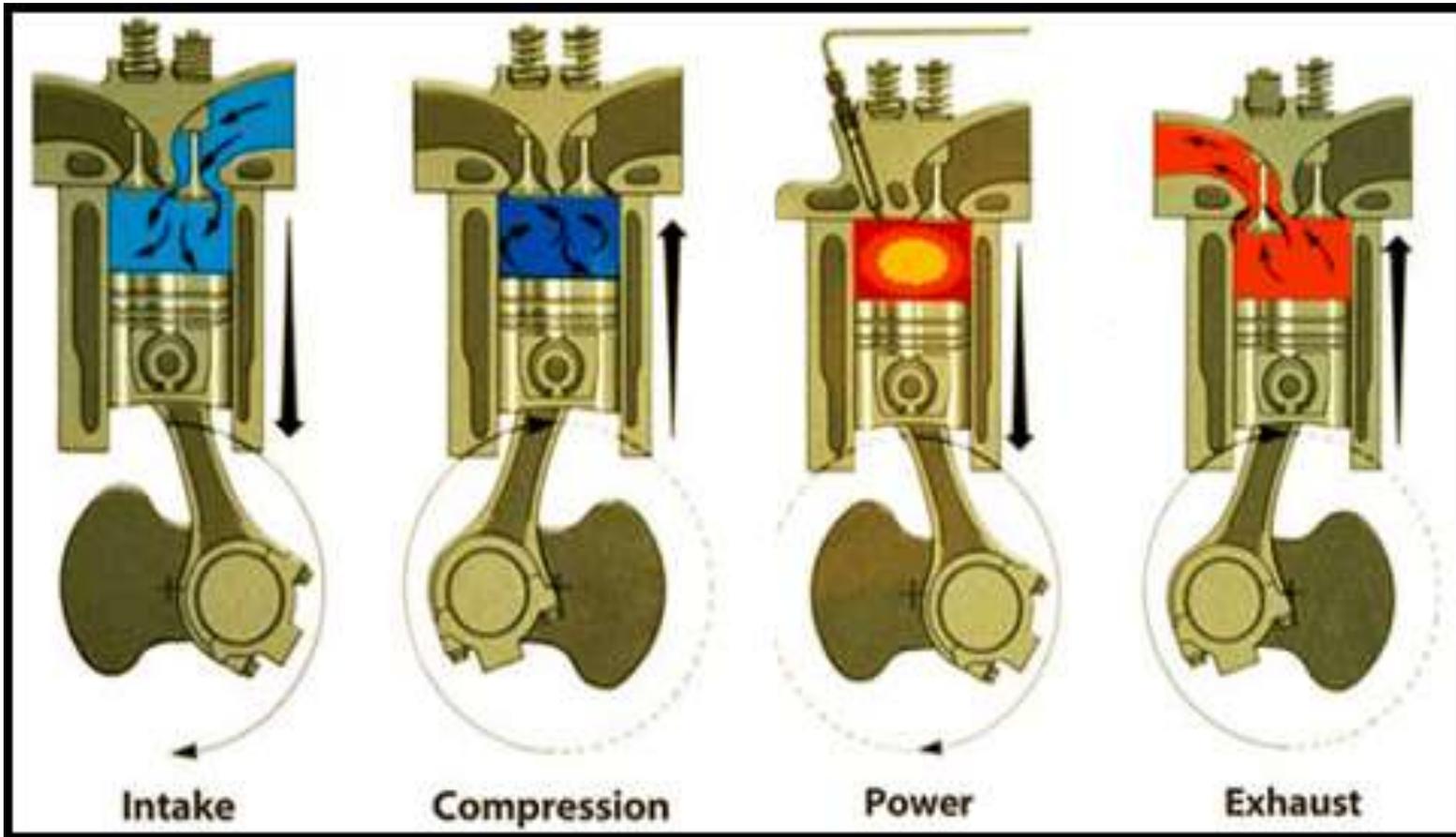
PARTS OF IC ENGINE



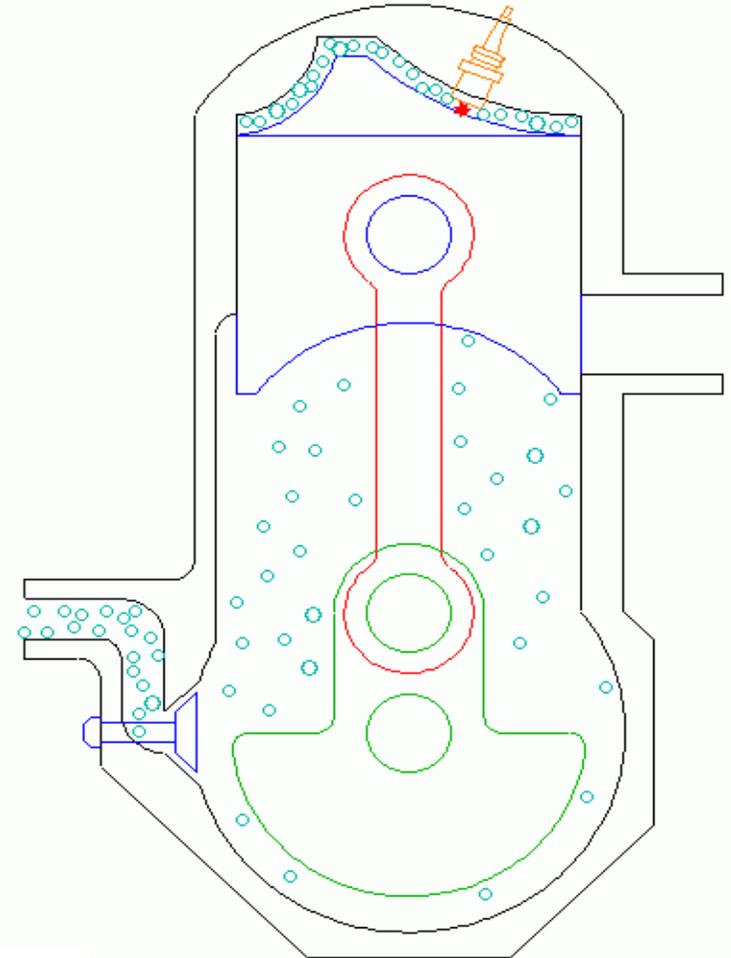
IC ENGINE TERMINOLOGY



Four - Stroke (4-s) Engine



2-stroke engine



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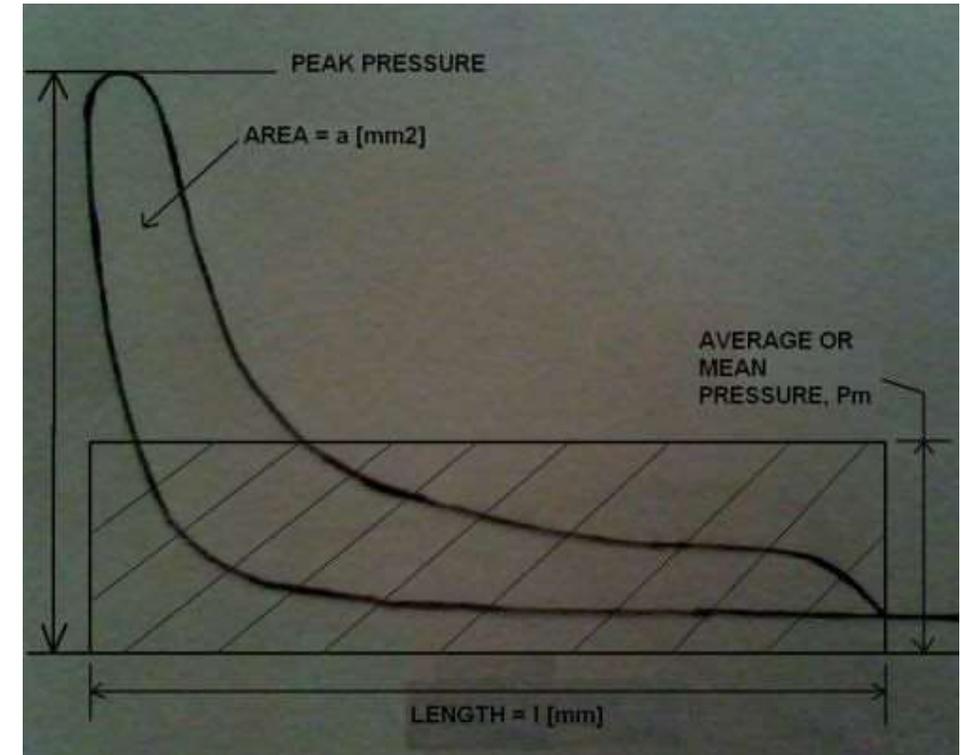
Performance Parameters

- Mean Effective Pressure (MEP) - P_m

It is expressed in Bar (1Bar = 10^5 N/m²)

$$MEP = P_m = \frac{\left(\begin{array}{l} \text{spring value of the spring used} \\ \text{in the indicator (S) in bar / m} \end{array} \right) \times \left(\begin{array}{l} \text{net area of the indicator} \\ \text{diagram (a) in m}^2 \end{array} \right)}{\text{length of the indicator diagram (l) in m}}$$

$$P_m = \frac{Sa}{l} \text{ Bar}$$



Performance Parameters

Indicated Power (IP)

Brake Power (BP)

$$\text{Indicated Power} = \frac{p_m L A N}{60 \times 2 \times 1000} \text{ kW}$$

- p_m = Mean Effective Pressure, N/m^2
- L = Length of Stroke, m
- A = Area of Cross section of the Cylinder, sq m
- N = RPM of the Crankshaft.
- n = Number of cycles per minute.

$$BP \text{ is given by, } BP = \frac{2\pi NT}{60 \times 1000} \text{ kW}$$

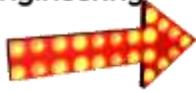
where N = speed of engine in *rpm*

T = Torque in N-m

Torque (T) is measured by using either *belt* or *rope brake dynamometer*.

Friction Power (FP)

$$FP = IP - BP \text{ kW}$$



Performance Parameters

Mechanical Efficiency

$$\eta_{\text{mech}} = (\text{BP}/\text{IP}) \times 100$$

Thermal Efficiency

$$\eta_{\text{th}} = \frac{\text{power output}}{\text{heat supplied}} \times 100$$

w.k.t. Heat supplied = $(m_f) \times CV$

where m_f = mass of fuel in kg/sec.

CV = calorific value of fuel in kJ/kg.

$$\text{Indicated thermal efficiency} = \eta_{\text{ITH}} = \frac{IP}{m_f \times CV} \times 100$$

$$\text{Brake thermal efficiency} = \eta_{\text{BTH}} = \frac{BP}{m_f \times CV} \times 100$$

Performance Parameters

Specific Fuel Consumption

$$\text{i.e., SFC} = \frac{m_f (\text{kg/hr})}{\text{Power developed (kW)}} \text{ kg/kW-hr}$$

where m_f = mass of fuel (kg/hr)

Power developed can be based on IP or BP.

SFC based on IP is termed indicated specific fuel consumption (ISFC), and is given by the equation

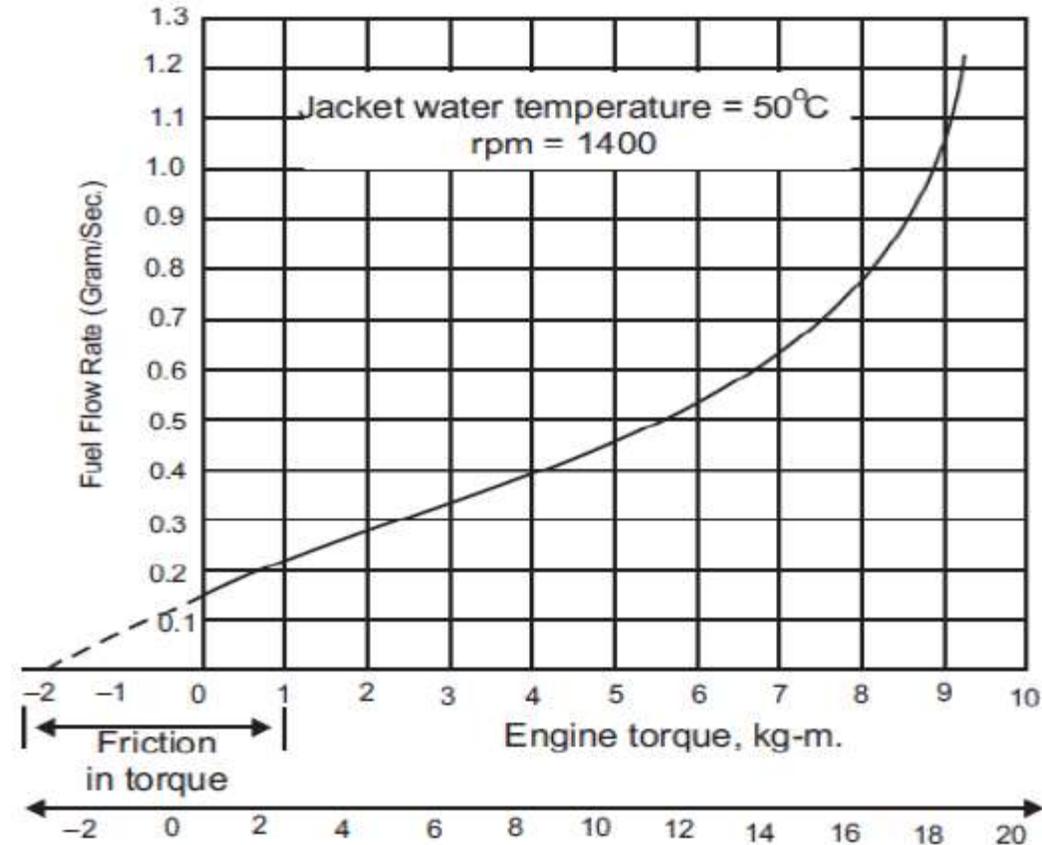
$$\text{ISFC} = \frac{\text{Fuel consumed in kg/hr}}{\text{IP in kW}} \text{ kg/kWhr}$$

While SFC based on BP is termed brake specific fuel consumption (BSFC), and is given by the equation

$$\text{BSFC} = \frac{\text{Fuel consumed in kg/hr}}{\text{BP in kW}} \text{ kg/kWhr}$$

Measurement of Friction power

- *Willan's line method.*
- *Morse test.*
- *Motoring test.*



Morse test.

- The Morse test is applicable only to multicylinder engines.
- With all cylinder firing = BP kW
- Cut off at 1st cylinder = BP1 kW
- Cut off at 2nd cylinder = BP2 kW
- Cut off at 3rd cylinder = BP3 Kw

$$IP1 = BP - BP1, \quad IP3 = BP - BP3$$

$$IP = IP_1 + IP_2 + IP_3$$

Heat Balance sheet

- The heat balance sheet from the above data can be drawn as follows:

<i>Particulars</i>	<i>kJ/s or kJ/min or kJ/hr</i>	<i>Percent</i>
a) Heat supplied by fuel	----	-----
b) Heat absorbed in B.P.	----	-----
c) Heat taken away by cooling water	----	-----
d) Heat carried away by the exhaust gases	----	-----
e) Heat unaccounted for (a-(b+c+d))		
Total	----	-----



Module – 2: Gas Power Cycles

➤ Gas-Turbine

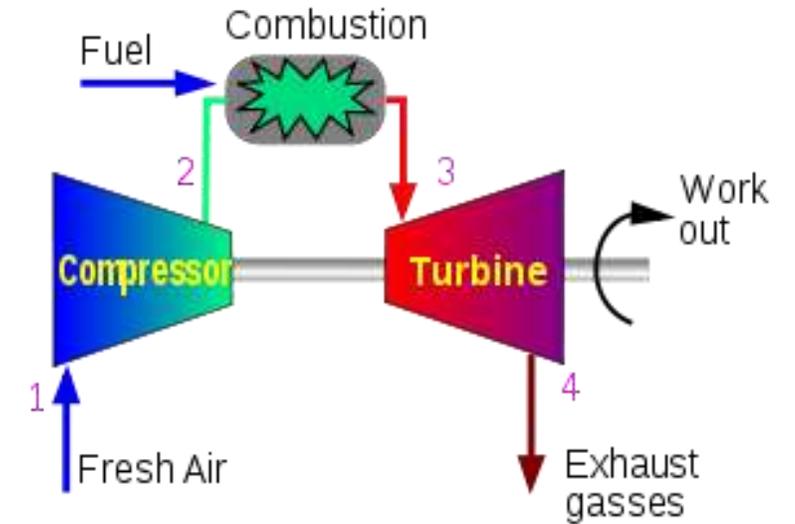
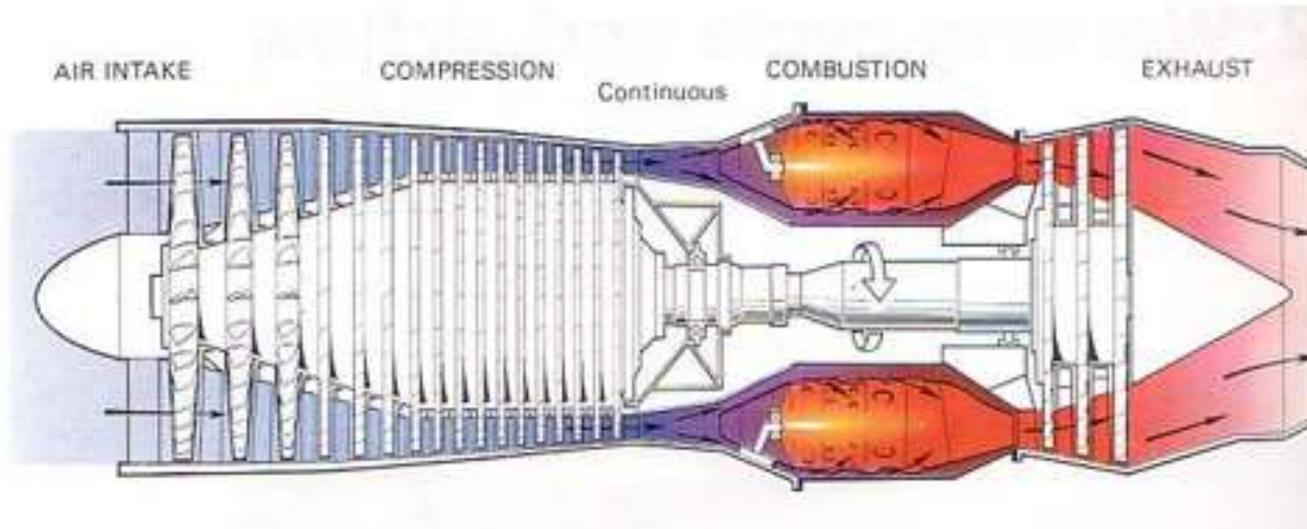
- Open cycle gas turbine
- Closed cycle gas turbine

➤ Brayton Cycle

➤ Methods to improve Thermal Efficiency of Gas Turbine- Intercooling, Reheat & Regeneration

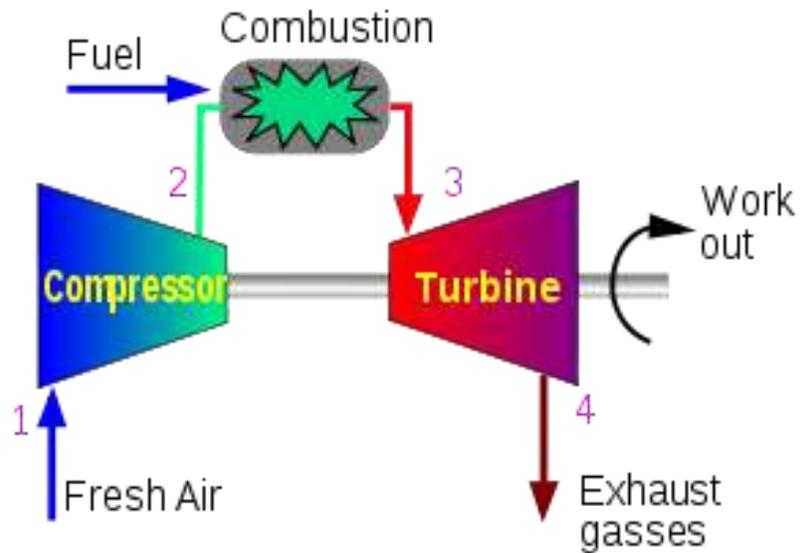
➤ Jet Propulsion System

Gas-Turbine

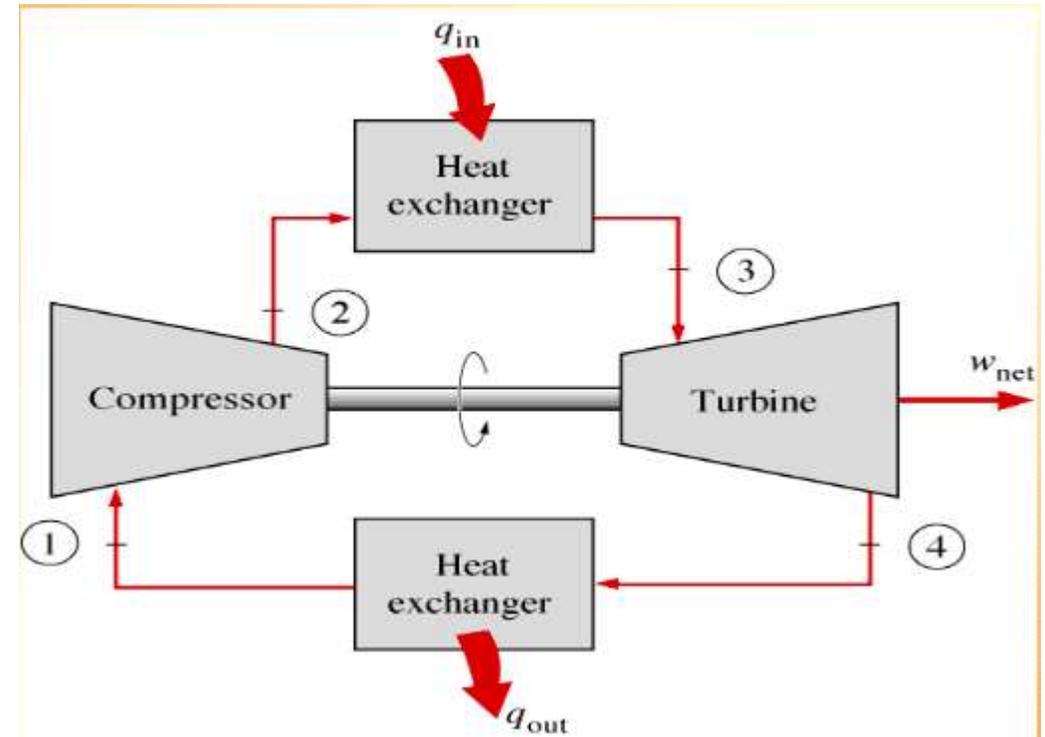


Classification of Gas-Turbine

- Open cycle gas turbine



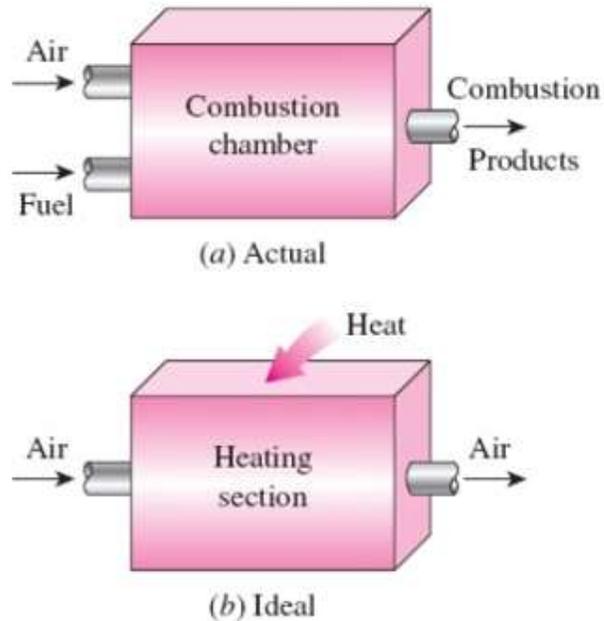
- Closed cycle gas turbine



Comparison between Open cycle gas turbine and Closed cycle gas turbine

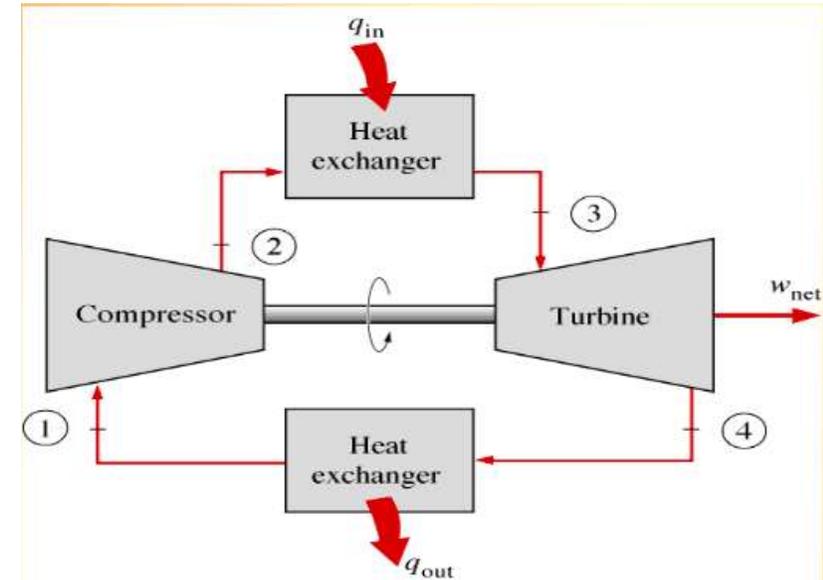
Closed Cycle Gas Turbine	Open Cycle Gas Turbine
1. The compressed air is heated in heating chamber.	1. The compressed air is heated in combustion chamber.
2. As the gas is heated by an external source, hence the amount of gas remains same through the cycle	2. The products of combustion are get mixed up in the heated air hence same gas doesn't remain in cycle.
3. The gas after turbine is passed into the cooling chamber.	3. The gas after turbine is exhausted into the atmosphere.
4. The working fluid is circulated continuously.	4. The working fluid is replaced continuously.
5. Any fluid with better thermodynamic properties can be used.	5. Only air is used as the working fluid.
6. The turbine blades do not wear away earlier, as the enclosed gas does not get contaminated while flowing through heating chamber.	6. The turbine blades wear away earlier, as the air from atmosphere get contaminated while flowing through combustion chamber.
7. The mass of installation per Kwatt is more	7. The mass of installation per Kwatt is less
8. High maintenance cost	8. Maintenance cost is low

Analysis of Brayton Cycle



Air-standard assumptions:

1. The working fluid is air, which continuously circulates in a closed loop and always behaves as an ideal gas.
2. All the processes that make up the cycle are internally reversible.
3. The combustion process is replaced by a heat-addition process from an external source.
4. The exhaust process is replaced by a heat-rejection process that restores the working fluid to its initial state.



The combustion process is replaced by a heat-addition process in ideal cycles.

Analysis of Brayton Cycle

Efficiency of Brayton cycle

1-2 Isentropic Compression (compressor)

$$W_C = C_P (T_2 - T_1)$$

2-3 Constant-pressure heat addition

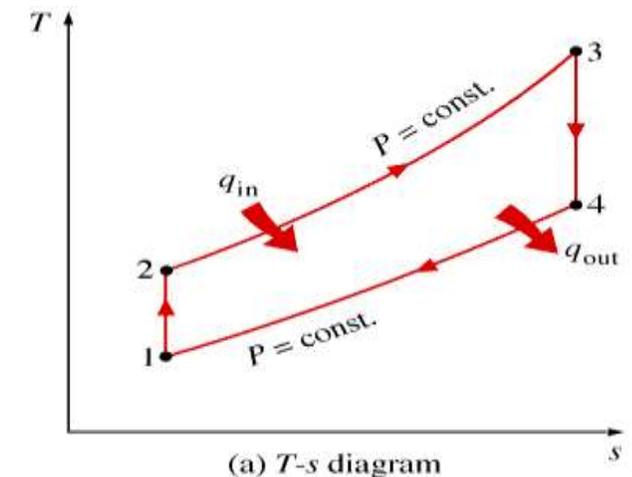
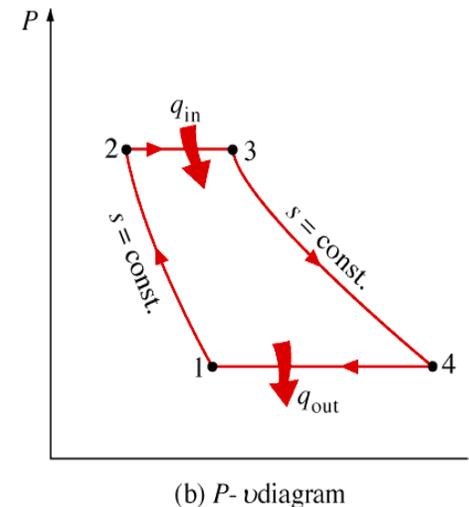
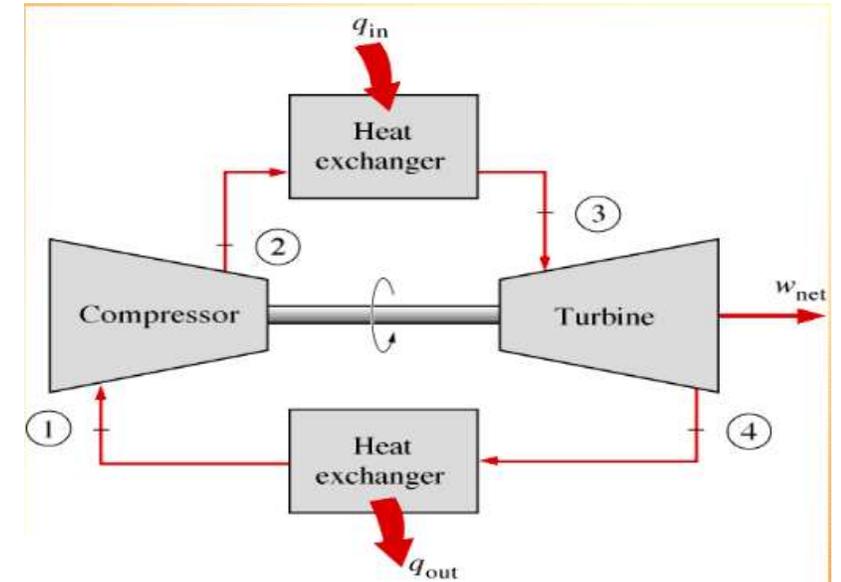
$$Q_S = C_P (T_3 - T_2)$$

3-4 Isentropic expansion (turbine)

$$W_T = C_P (T_3 - T_4)$$

4-1 Constant-pressure heat rejection

$$Q_r = C_P (T_4 - T_1)$$



Analysis of Brayton Cycle

Efficiency of Brayton cycle

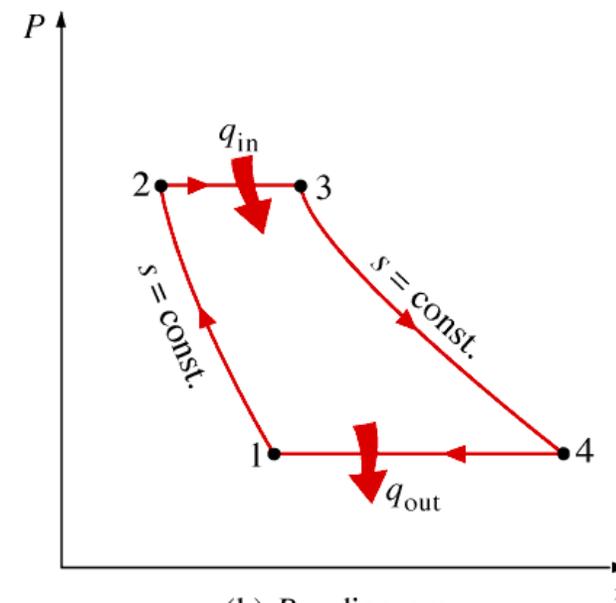
$$\text{efficiency } \eta = \frac{\text{Work done}}{\text{Heat supplied}}$$

$$= \frac{W_T - W_C}{Q_S}$$

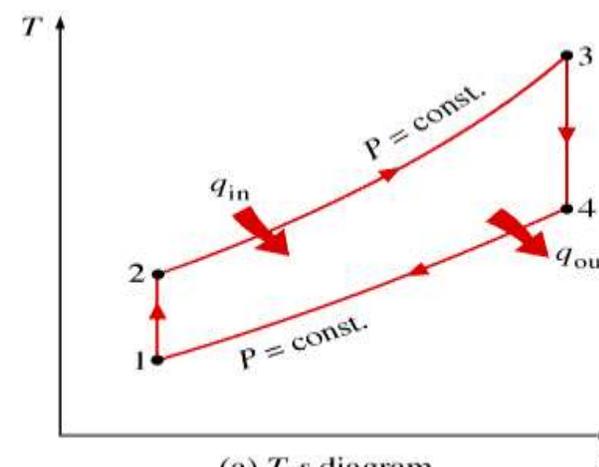
$$= \frac{C_P(T_3 - T_4) - C_P(T_2 - T_1)}{C_P(T_3 - T_2)}$$

$$= \frac{(T_3 - T_4) - (T_2 - T_1)}{(T_3 - T_2)}$$

$$\eta = \frac{(T_3 - T_2) - (T_4 - T_1)}{(T_3 - T_2)}$$



(b) P - v diagram



(a) T - s diagram

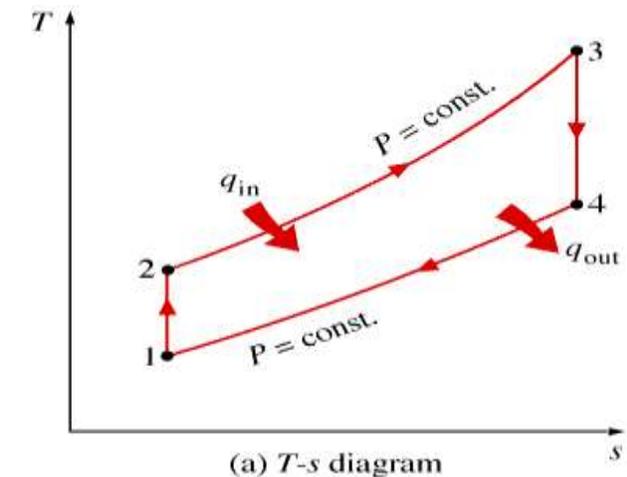
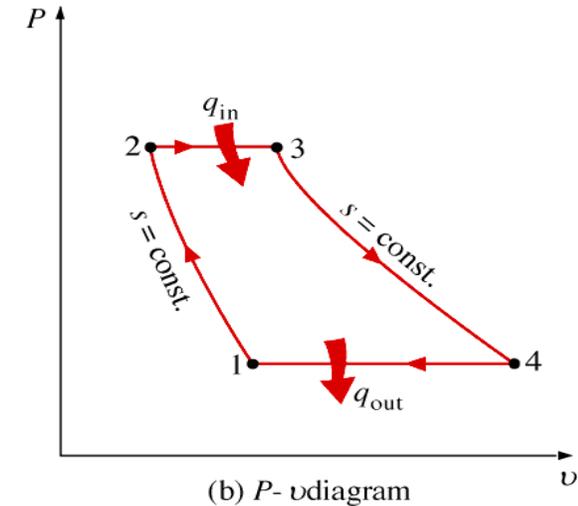
Analysis of Brayton Cycle

$$\eta = \frac{(T_3 - T_2) - (T_4 - T_1)}{(T_3 - T_2)} = 1 - \frac{(T_4 - T_1)}{(T_3 - T_2)}$$

For isentropic (adiabatic) process 1-2,

we have
$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}}$$

Let $\frac{P_2}{P_1} = R_p$ pressure ratio



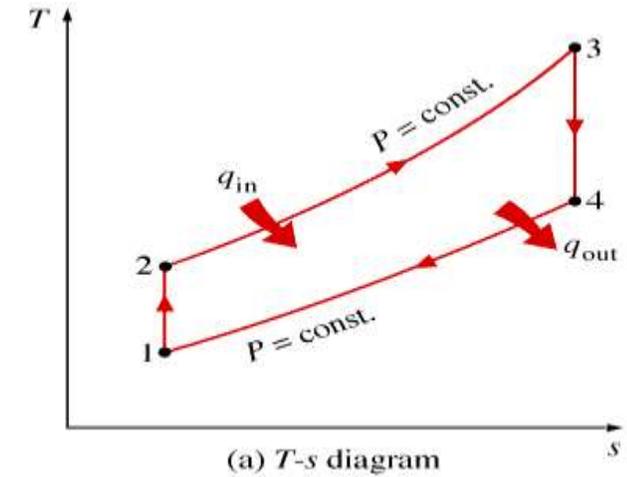
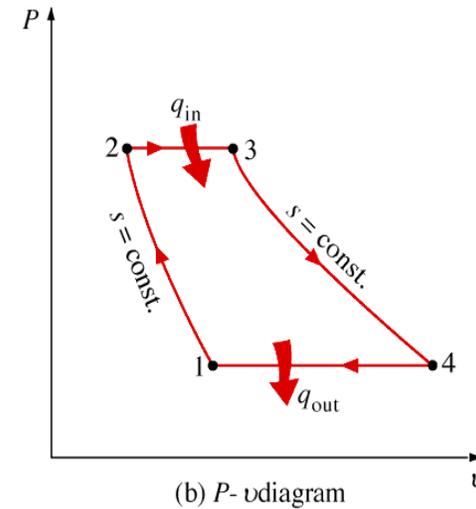
Analysis of Brayton Cycle

for isentropic process 3-4, we have $\frac{T_3}{T_4} = \left(\frac{P_3}{P_4}\right)^{\frac{\gamma-1}{\gamma}}$

But $P_3 = P_2$ and $P_4 = P_1$

$$\therefore \frac{T_3}{T_4} = \left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}} \quad \text{or} \quad \frac{T_3}{T_4} = (R_P)^{\frac{\gamma-1}{\gamma}}$$

$$\therefore T_3 = T_4 (R_P)^{\frac{\gamma-1}{\gamma}}$$



Analysis of Brayton Cycle

Efficiency of Brayton cycle

$$\eta = 1 - \frac{(T_4 - T_1)}{T_4 (R_P)^{\frac{\gamma-1}{\gamma}} - T_1 (R_P)^{\frac{\gamma-1}{\gamma}}}$$

$$= 1 - \frac{(T_4 - T_1)}{(T_4 - T_1)(R_P)^{\frac{\gamma-1}{\gamma}}}$$

$$\eta = 1 - \frac{1}{(R_P)^{\frac{\gamma-1}{\gamma}}}$$

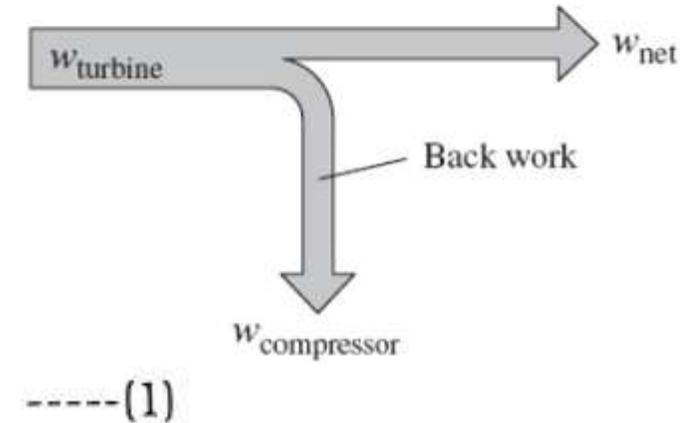
Analysis of Brayton Cycle

Work Ratio:

$$\begin{aligned} \text{i.e., Work ratio} = R_w &= \frac{W_{\text{net}}}{W_T} \\ &= \frac{W_T - W_C}{W_T} = 1 - \frac{W_C}{W_T} \end{aligned}$$

where, compressor work $W_C = C_p (T_2 - T_1)$ kJ/kg of air

Turbine work $W_T = C_p (T_3 - T_4)$ kJ/kg of air



Work Ratio:

$$\begin{aligned} \therefore R_w &= 1 - \frac{C_P(T_2 - T_1)}{C_P(T_3 - T_4)} \\ &= 1 - \frac{(T_2 - T_1)}{(T_3 - T_4)} = 1 - \frac{T_1 \left(\frac{T_2}{T_1} - 1 \right)}{T_3 \left(1 - \frac{T_4}{T_3} \right)} \quad \text{-----(2)} \end{aligned}$$

For isentropic (adiabatic) process 1-2, we have $\frac{T_2}{T_1} = \left(\frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}}$

But $\frac{P_2}{P_1} = R_p$ pressure ratio

$$\therefore \frac{T_2}{T_1} = (R_p)^{\frac{\gamma-1}{\gamma}} \quad \text{-----(3)}$$

Similarly for isentropic (adiabatic) process 3-4, we have $\frac{T_3}{T_4} = \left(\frac{P_3}{P_4}\right)^{\frac{\gamma-1}{\gamma}}$

But $P_3 = P_2$ and $P_4 = P_1$

$$\therefore \frac{T_3}{T_4} = \left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}}$$

$$\text{or } \frac{T_3}{T_4} = (R_p)^{\frac{\gamma-1}{\gamma}}$$

$$\therefore \frac{T_4}{T_3} = \frac{1}{(R_p)^{\frac{\gamma-1}{\gamma}}} \quad \text{-----(4)}$$

Substituting equations (3) and (4) in (2), we get

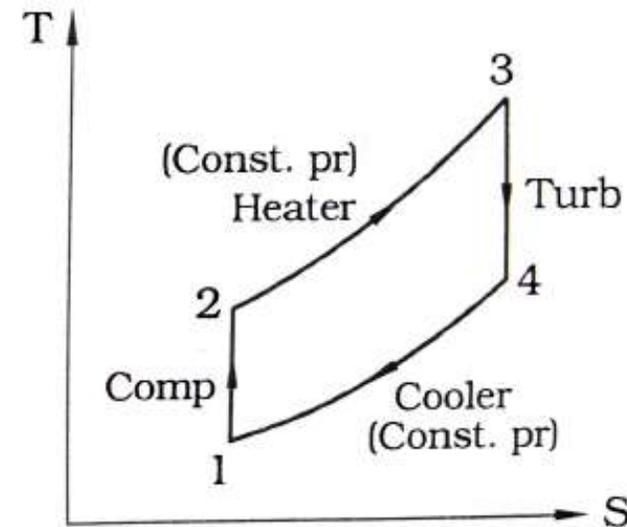
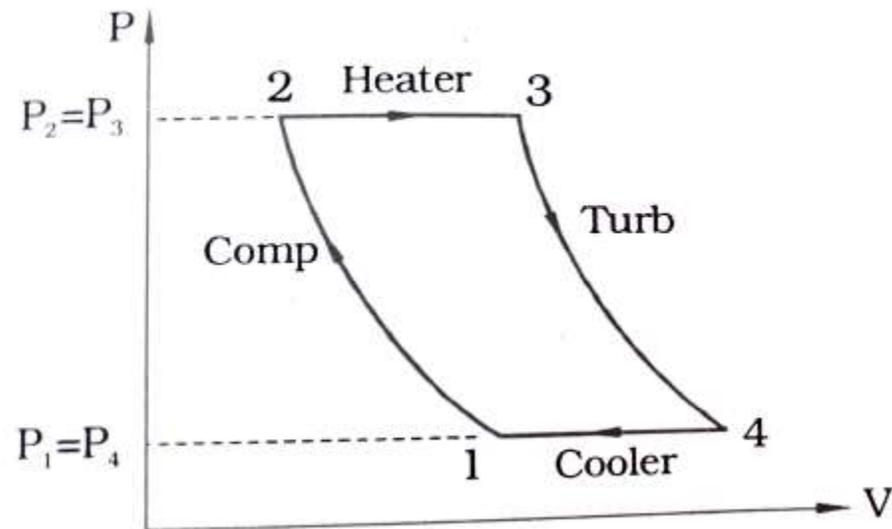
$$R_w = 1 - \frac{T_1}{T_3} \frac{\left[(R_p)^{\frac{\gamma-1}{\gamma}} - 1 \right]}{\left[1 - \frac{1}{(R_p)^{\frac{\gamma-1}{\gamma}}} \right]} = 1 - \frac{T_1}{T_3} \frac{\left[(R_p)^{\frac{\gamma-1}{\gamma}} - 1 \right]}{\left[(R_p)^{\frac{\gamma-1}{\gamma}} - 1 \right]} \cdot (R_p)^{\frac{\gamma-1}{\gamma}}$$

$$R_w = 1 - \frac{T_1}{T_3} (R_p)^{\frac{\gamma-1}{\gamma}}$$

Expression for optimum pressure ratio for maximum net work output

The optimum pressure ratio for maximum net work output is obtained by using the

$$\text{condition } \frac{dW_{\text{net}}}{dR_p} = 0$$



Expression for optimum pressure ratio for maximum net work output

To find net work done (W_{net})

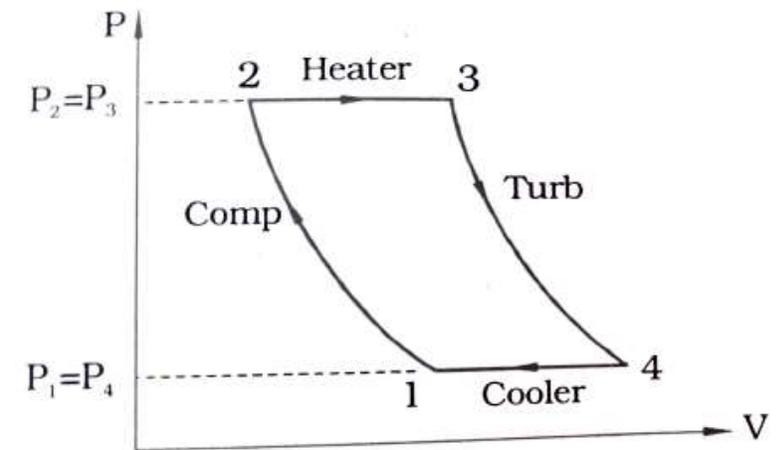
$$\begin{aligned} \text{w.k.t. net work done} &= W_{net} = W_T - W_C \\ &= C_p (T_3 - T_4) - C_p (T_2 - T_1) \quad \text{-----(1)} \end{aligned}$$

For isentropic (adiabatic) process 1-2, we have, $\frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}}$

$$\text{w.k.t. } \frac{P_2}{P_1} = R_p \text{ pressure ratio}$$

$$\therefore T_2 = T_1 (R_p)^{\frac{\gamma-1}{\gamma}} \quad \text{-----(2)}$$

Also, for isentropic process 3-4, we have $\frac{T_3}{T_4} = \left(\frac{P_3}{P_4}\right)^{\frac{\gamma-1}{\gamma}}$



Expression for optimum pressure ratio for maximum net work output

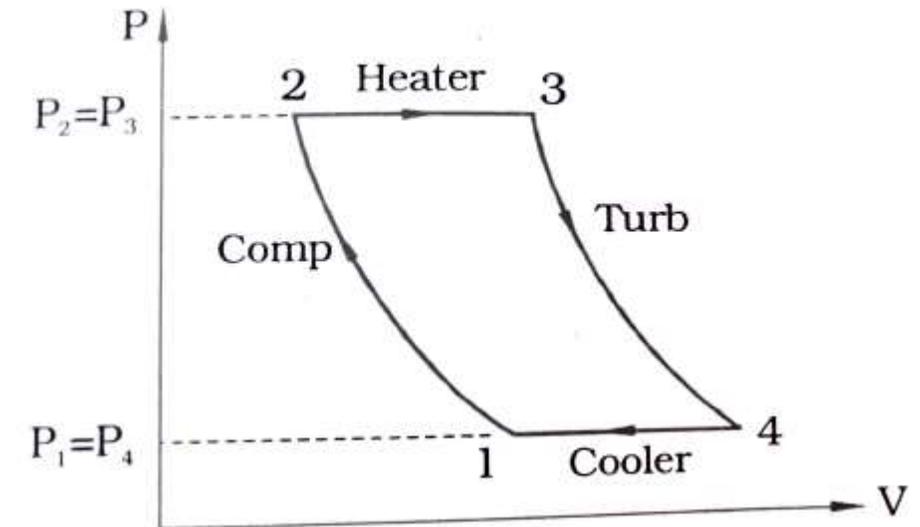
But from p-v diagram, $P_3 = P_2$ and $P_1 = P_4$

$$\therefore \frac{T_3}{T_4} = \left(\frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}} \quad \text{or} \quad \frac{T_3}{T_4} = (R_P)^{\frac{\gamma-1}{\gamma}}$$

$$\therefore T_4 = \frac{T_3}{(R_P)^{\frac{\gamma-1}{\gamma}}} \quad \text{----- (3)}$$

Substituting equations (2) and (3) in (1), we get

$$W_{\text{net}} = C_P \left[T_3 - \frac{T_3}{(R_P)^{\frac{\gamma-1}{\gamma}}} \right] - C_P \left[T_1 (R_P)^{\frac{\gamma-1}{\gamma}} - T_1 \right]$$



Expression for optimum pressure ratio for maximum net work output

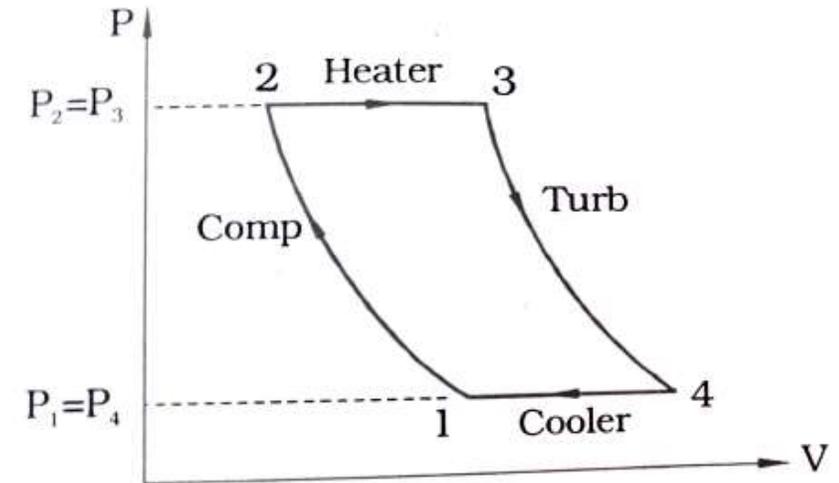
$$= C_p T_3 \left[1 - \frac{1}{(R_p)^{\frac{\gamma-1}{\gamma}}} \right] - C_p T_1 \left[(R_p)^{\frac{\gamma-1}{\gamma}} - 1 \right]$$

For simplicity, let $\frac{\gamma-1}{\gamma} = y$

$$\therefore W_{\text{net}} = C_p \cdot T_3 \left[1 - \frac{1}{(R_p)^y} \right] - C_p T_1 \left[(R_p)^y - 1 \right] \quad \text{-----(4)}$$

For optimum condition, we have $\frac{dW_{\text{net}}}{dR_p} = 0$

$$\therefore \frac{dW_{\text{net}}}{dR_p} = C_p \cdot T_3 \left[\frac{(y \cdot R_p^{y-1})}{(R_p^y)^2} \right] - C_p T_1 [y \cdot R_p^{y-1}] = 0$$



Expression for optimum pressure ratio for maximum net work output

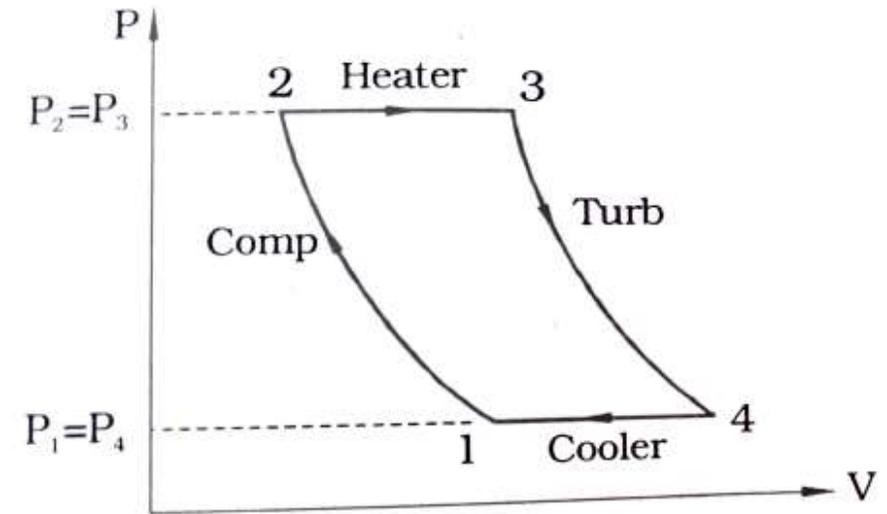
$$\text{or } T_3 \left[\frac{1}{(R_p)^{2y}} \right] - T_1 = 0$$

$$\frac{T_3}{(R_p)^{2y}} = T_1$$

$$\text{or } \frac{T_3}{T_1} = (R_p)^{2y}$$

$$\therefore R_p = \left(\frac{T_3}{T_1} \right)^{\frac{1}{2y}} \quad \text{where } y = \frac{\gamma - 1}{\gamma}$$

$$\text{Thus } (R_p) = (R_p)_{\text{opt}} = \left(\frac{T_3}{T_1} \right)^{\frac{\gamma}{2(\gamma - 1)}}$$



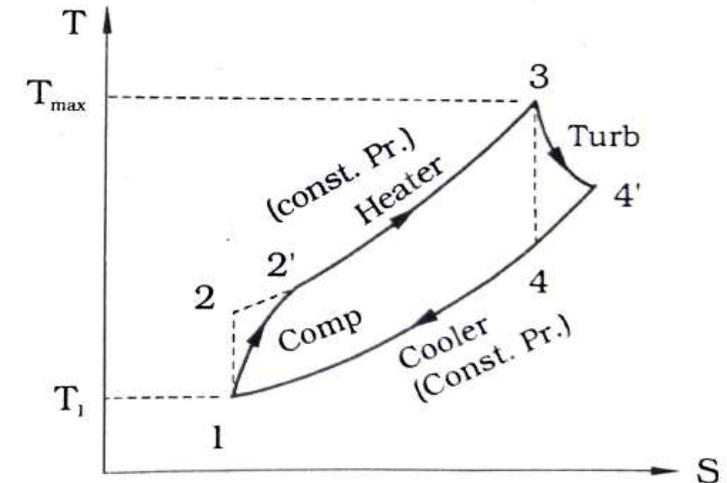
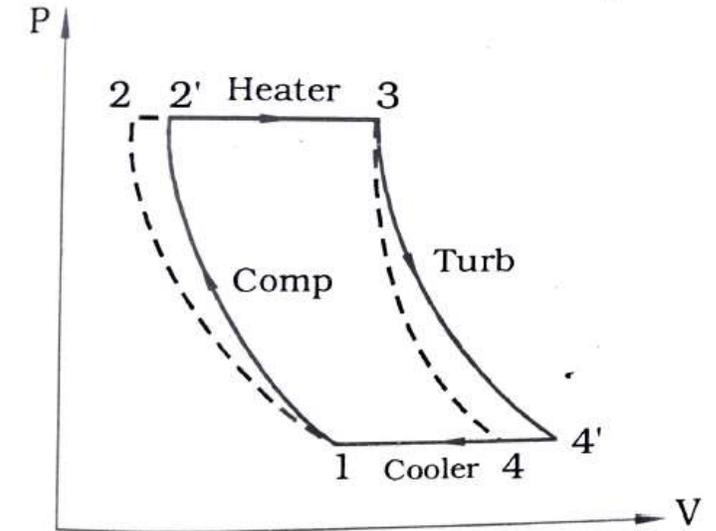
Deviation of Actual Gas-Turbine Cycle From Ideal Brayton cycle

Turbine efficiency = $\frac{\text{Actual workdone by the turbine}}{\text{Isentropic workdone by the turbine}}$

turbine efficiency $\eta_T = \frac{(T_3 - T_{4'})}{(T_3 - T_4)}$

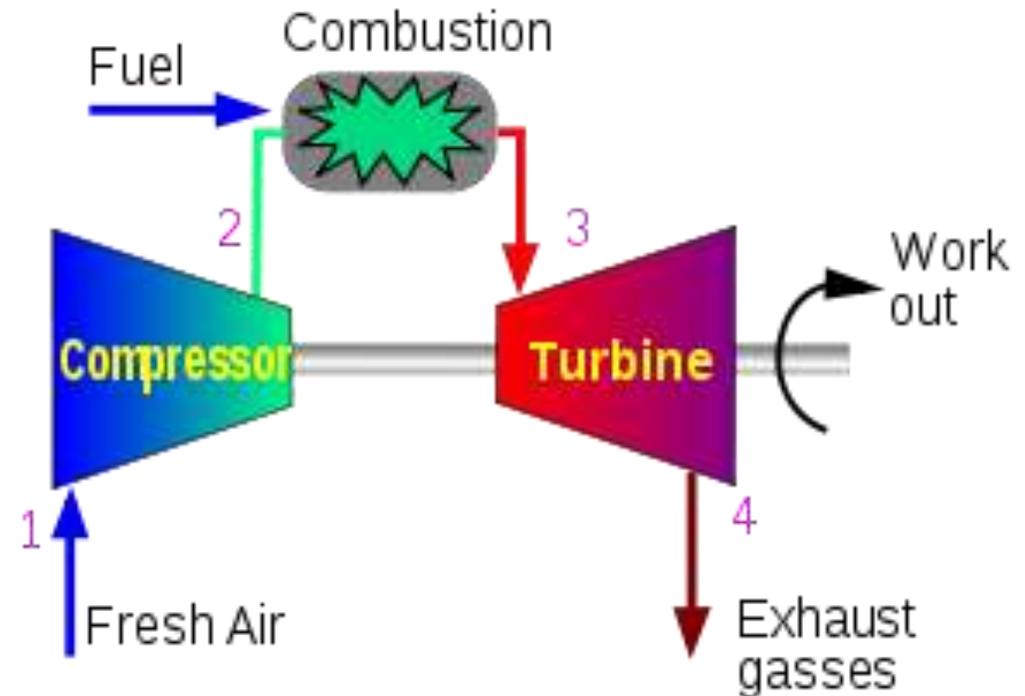
Compressor efficiency = $\frac{\text{Isentropic workdone to the compressor}}{\text{Actual workdone to th compressor}}$

compressor efficiency $\eta_C = \frac{(T_2 - T_1)}{(T_{2'} - T_1)}$



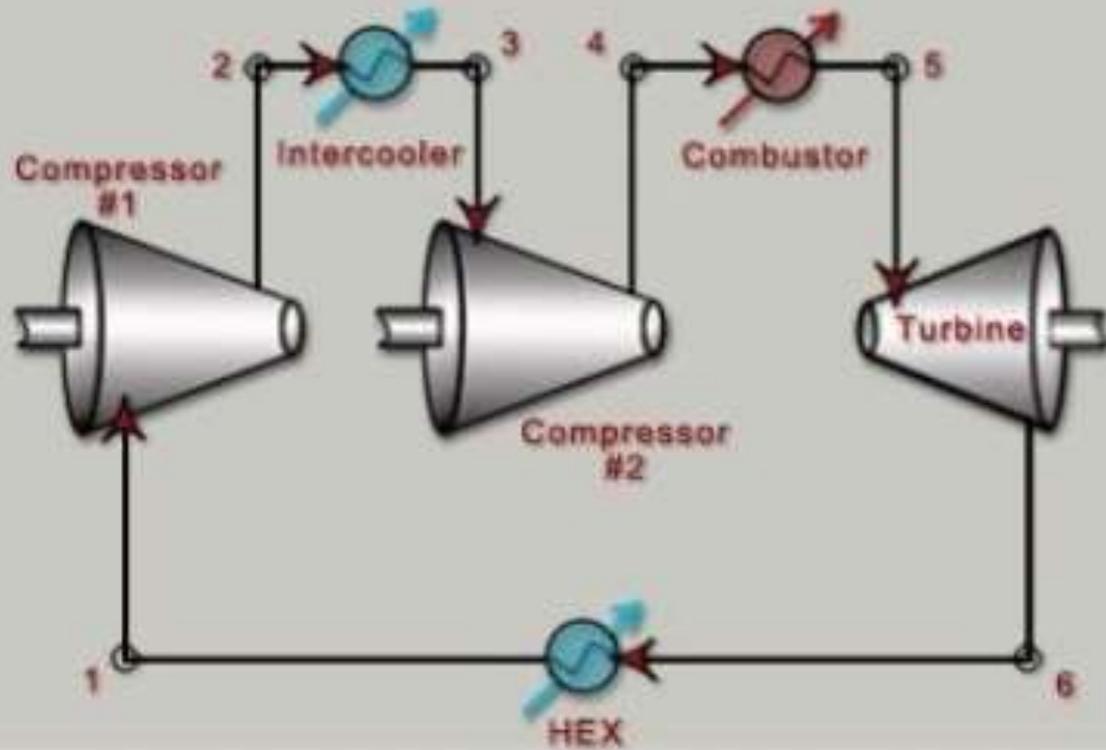
Methods to improve the performance of Gas Turbine

- Intercooling
- Reheating
- Regeneration

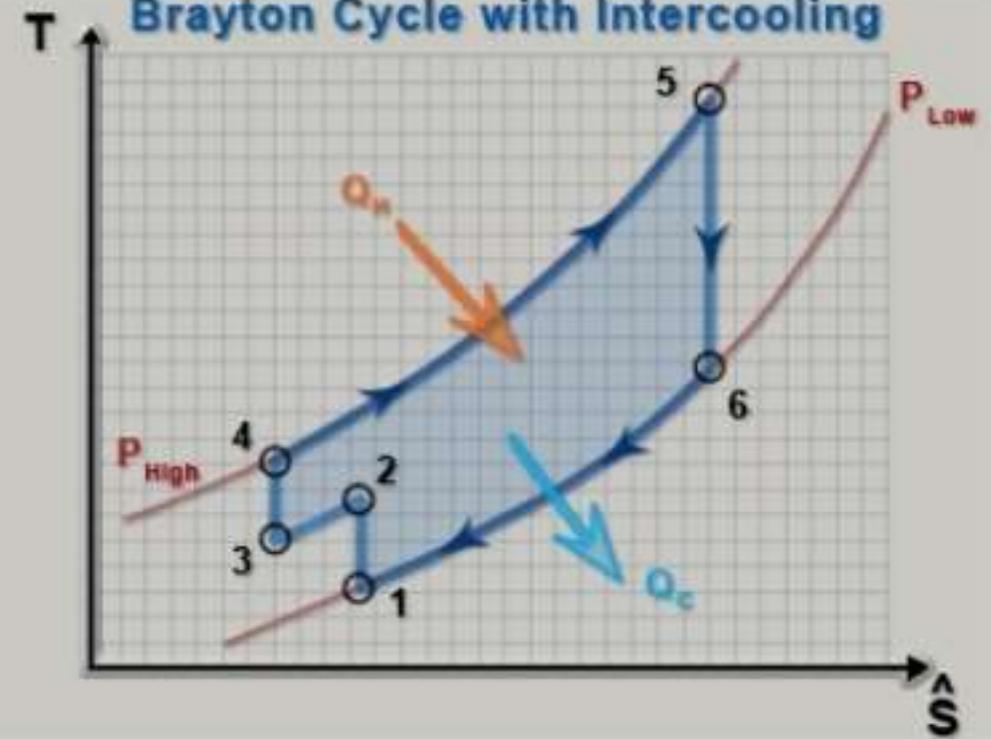


Brayton cycle with Intercooling

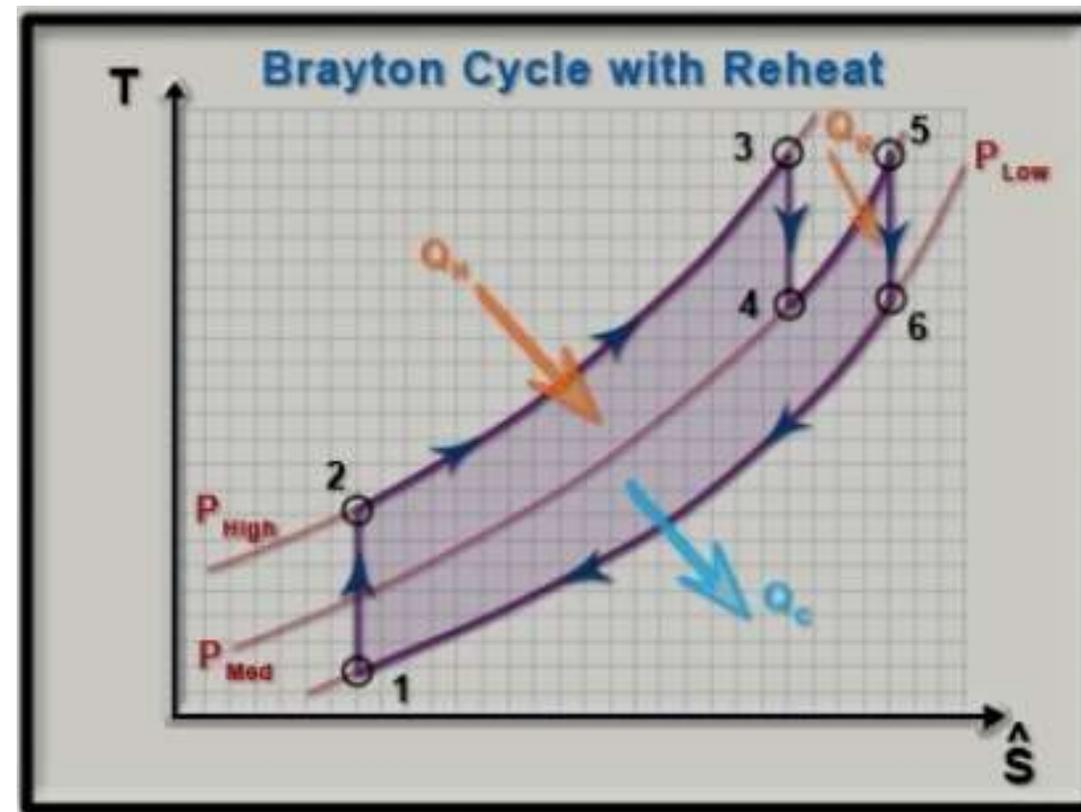
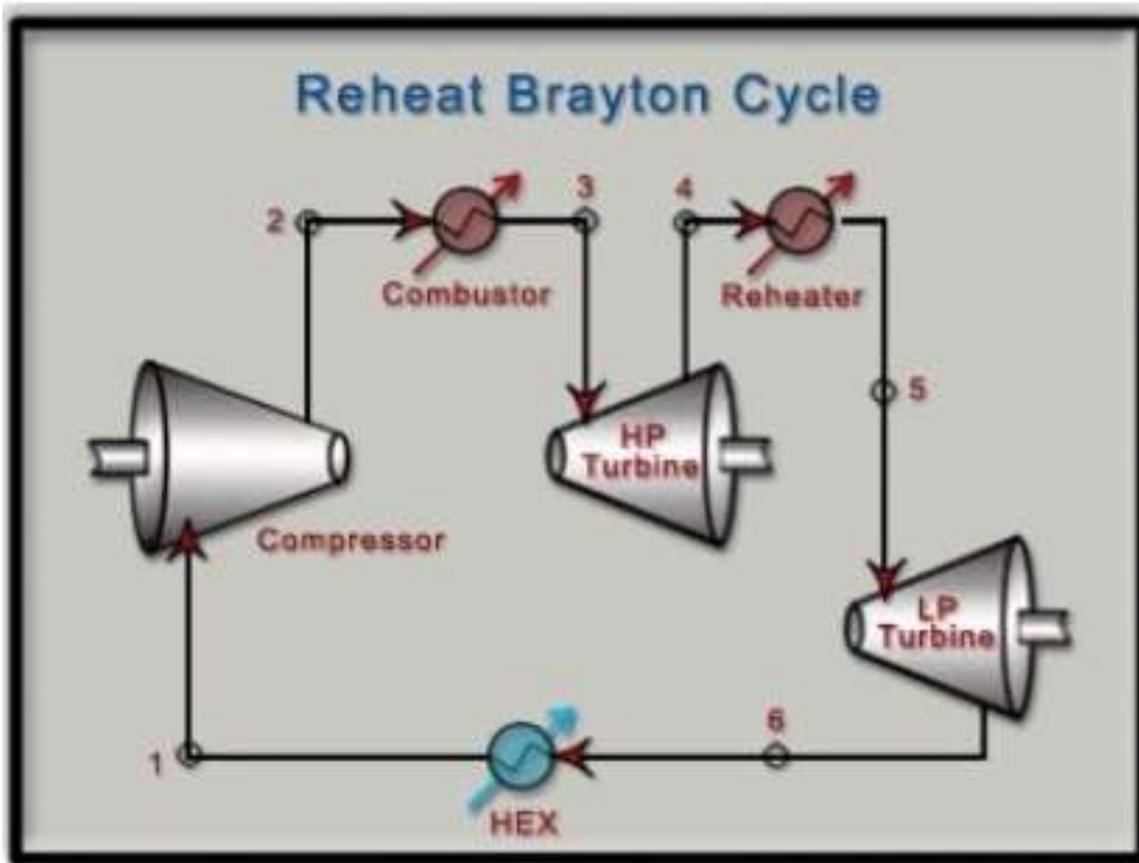
Brayton Cycle with Intercooling



Brayton Cycle with Intercooling



Brayton cycle with Reheating



Brayton cycle with Regeneration

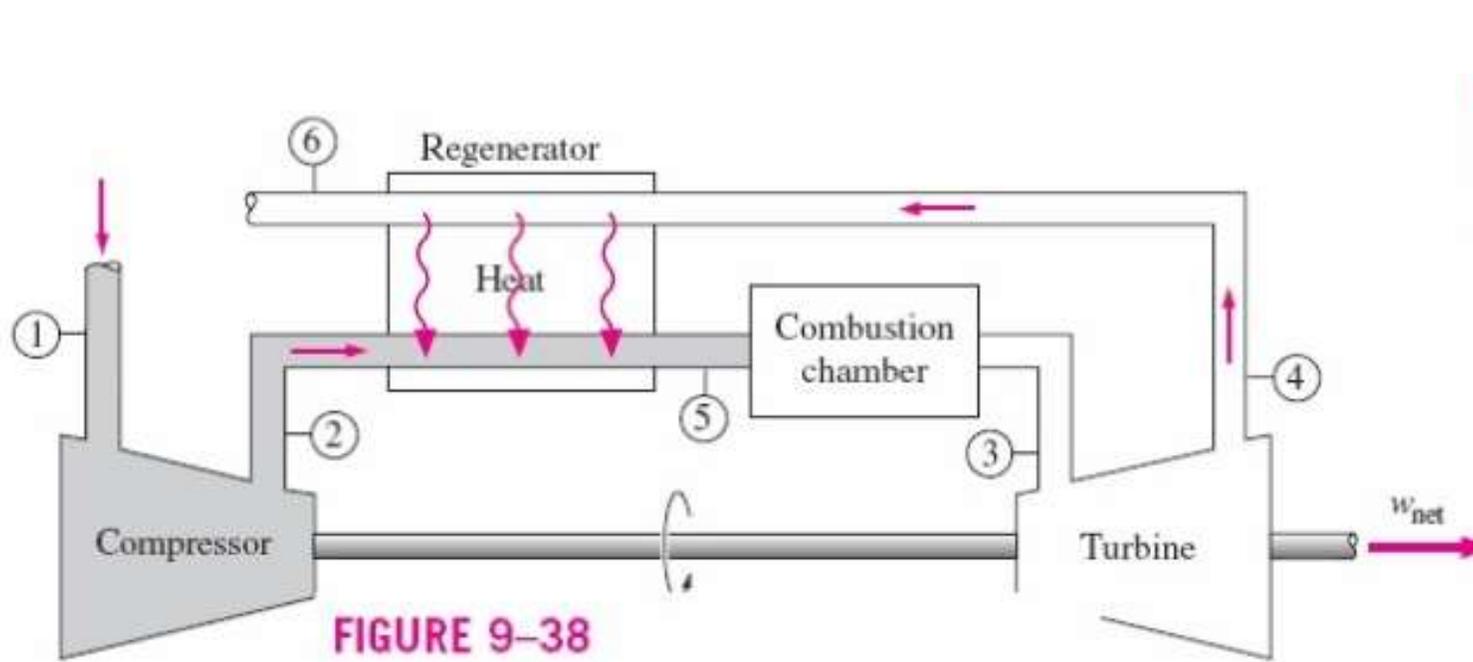
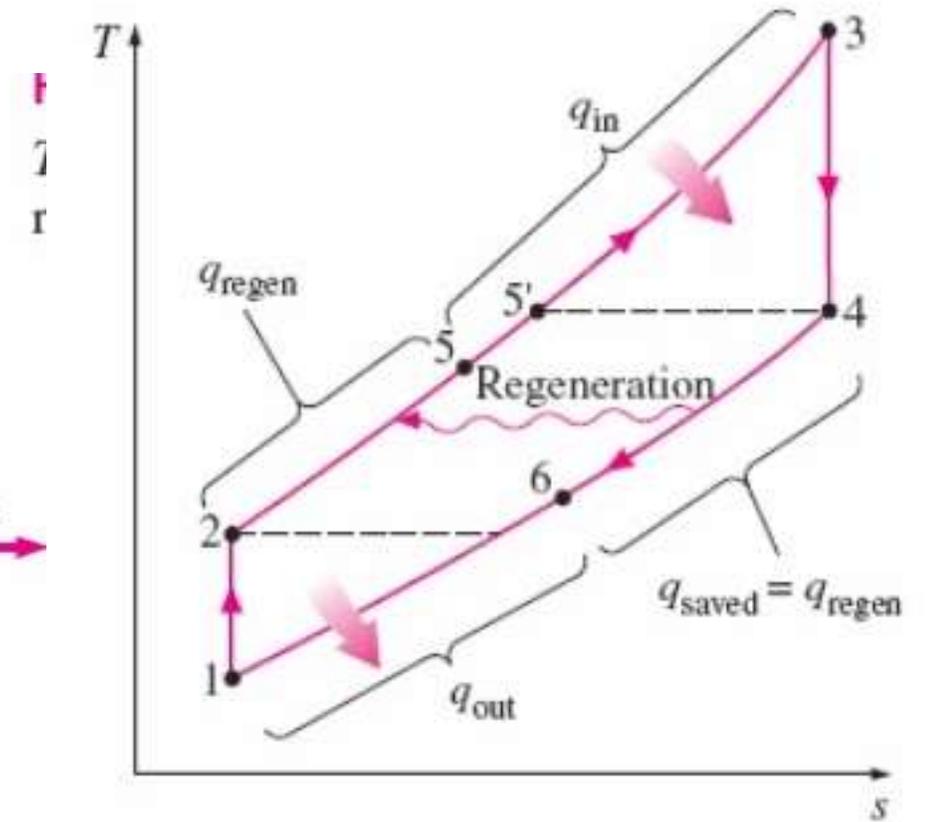


FIGURE 9-38

A gas-turbine engine with regenerator.



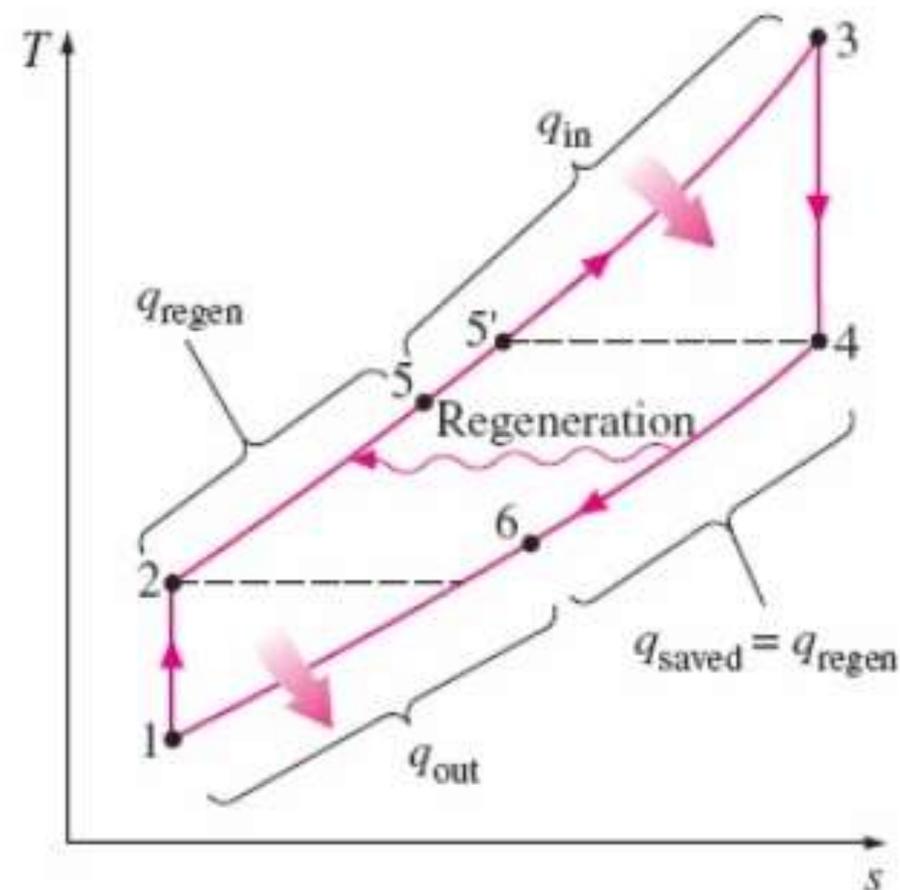
Brayton cycle with Regeneration

Effectiveness of regenerator:

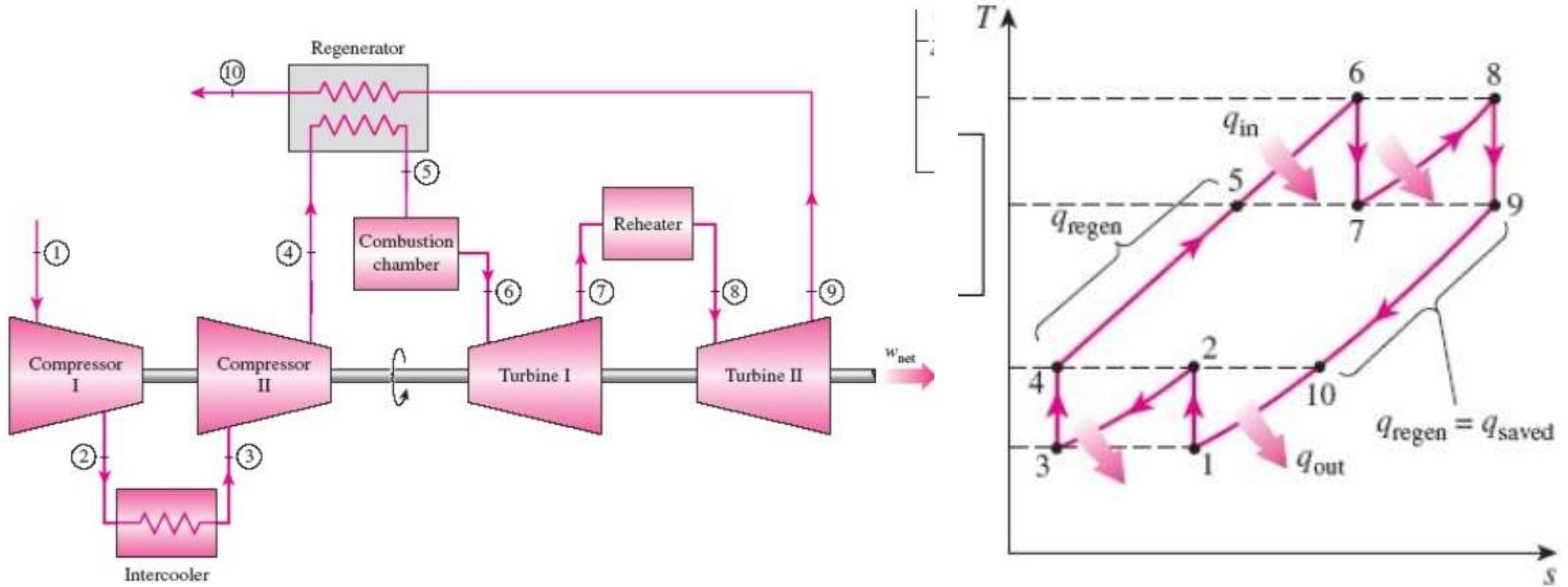
$$q_{\text{regen,act}} = h_5 - h_2$$

$$q_{\text{regen,max}} = h_{5'} - h_2 = h_4 - h_2$$

$$\varepsilon = \frac{q_{\text{regen,act}}}{q_{\text{regen,max}}} = \frac{h_5 - h_2}{h_4 - h_2} \cong \frac{T_5 - T_2}{T_4 - T_2}$$



Brayton cycle with Intercooling, Reheating and Regeneration



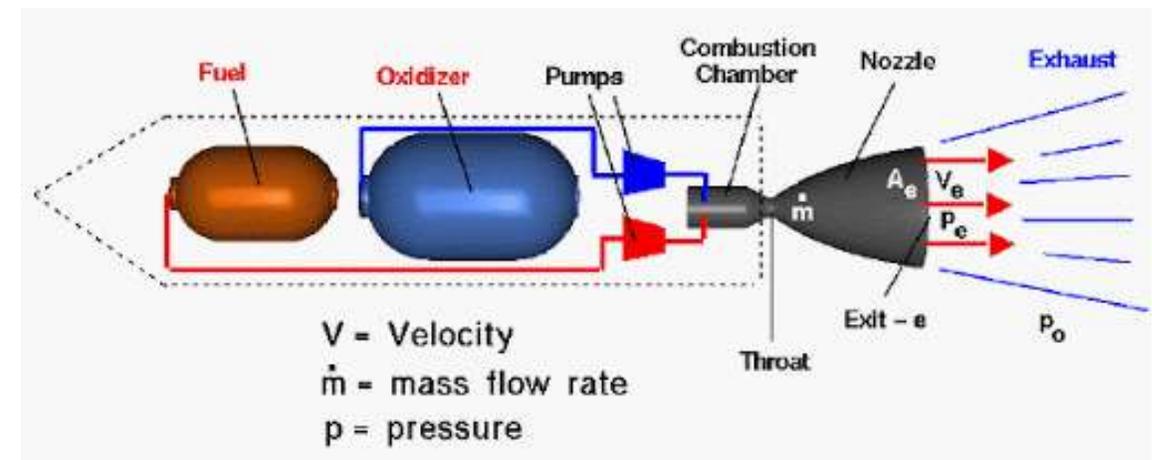
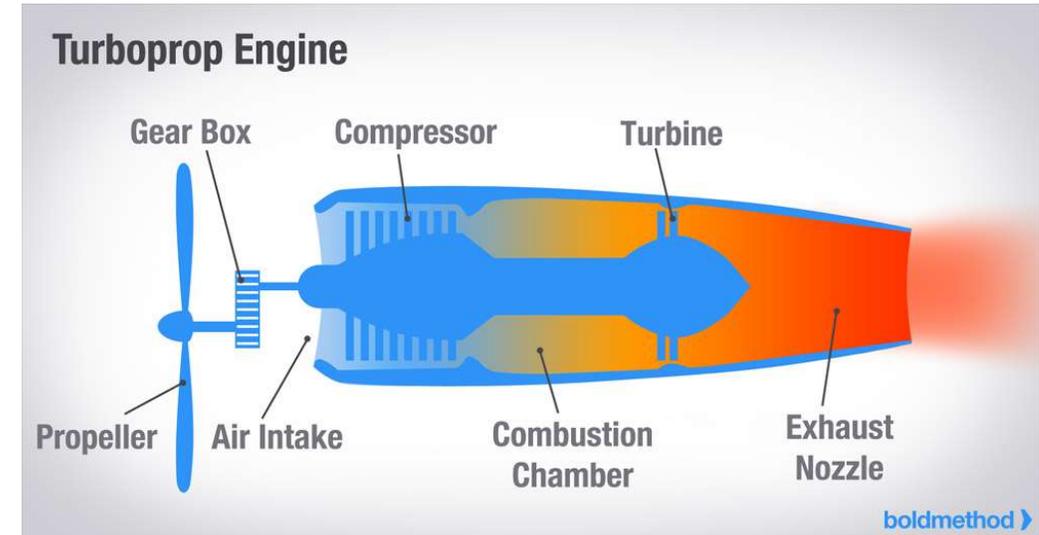
Jet Propulsion System

➤ Air-breathing engines

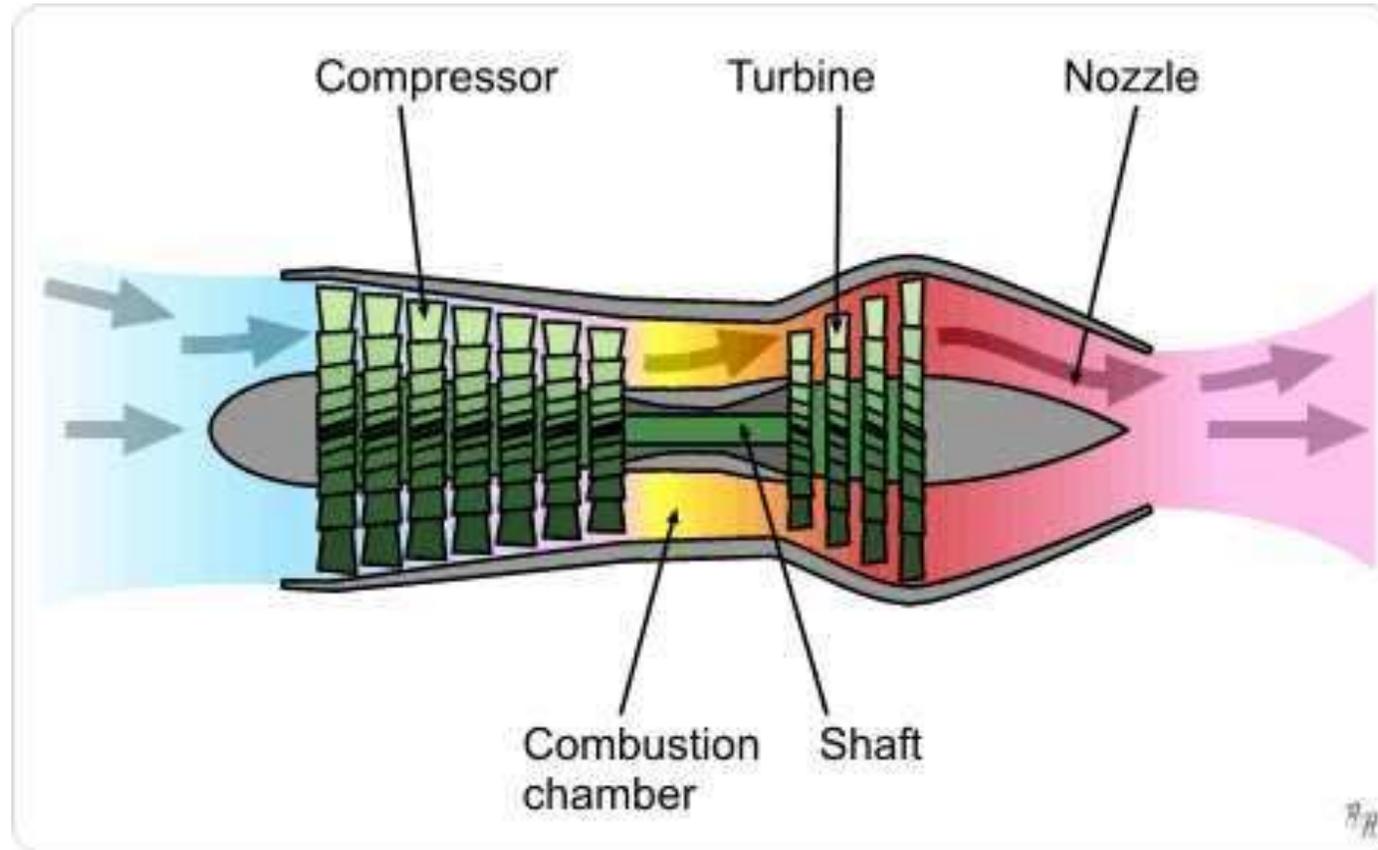
- Turbojet engine
- Turbo-prop engine
- Turbo-fan engine
- Ramjet engine

➤ Non air-breathing engines

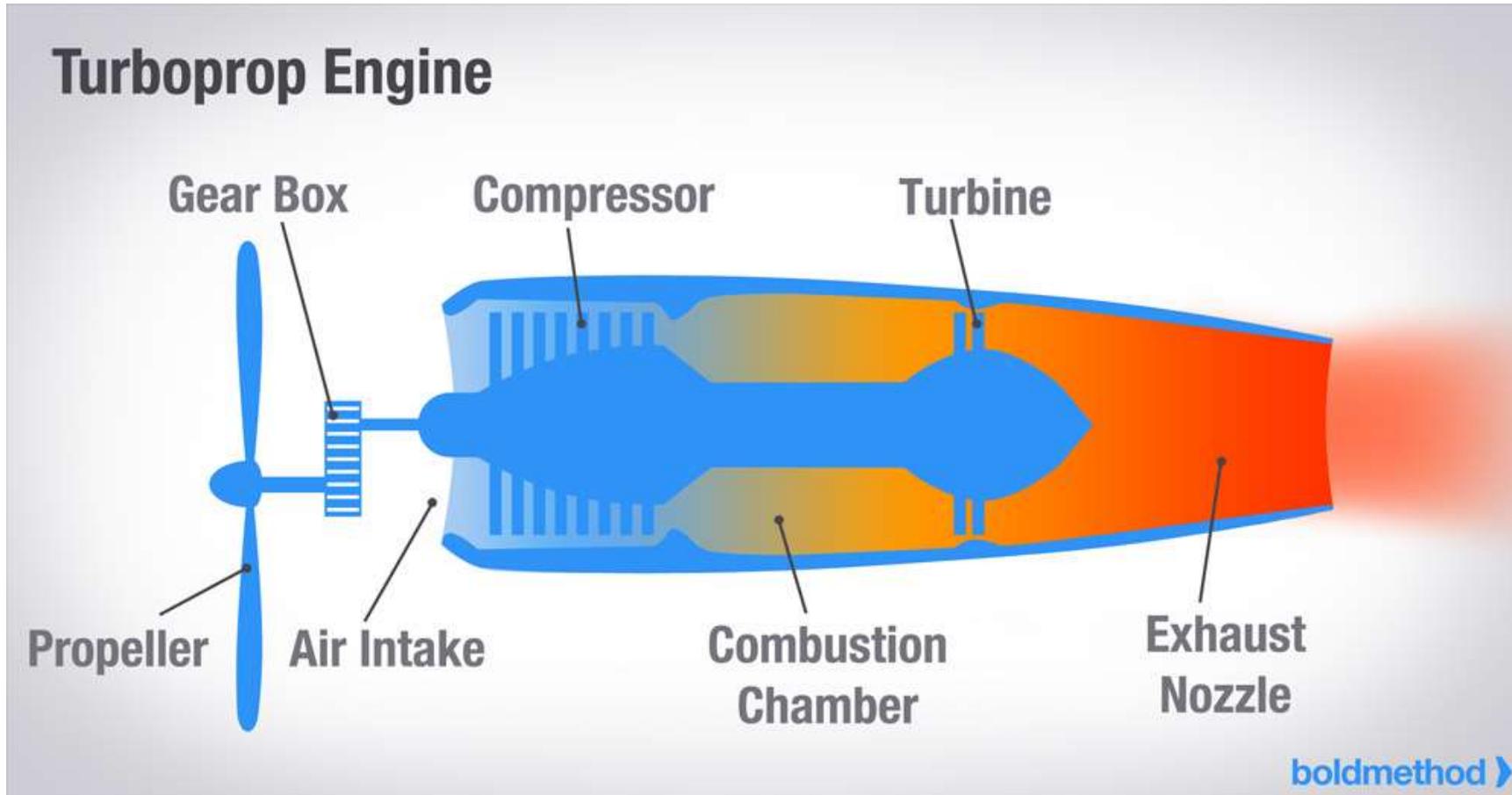
- Rocket engine



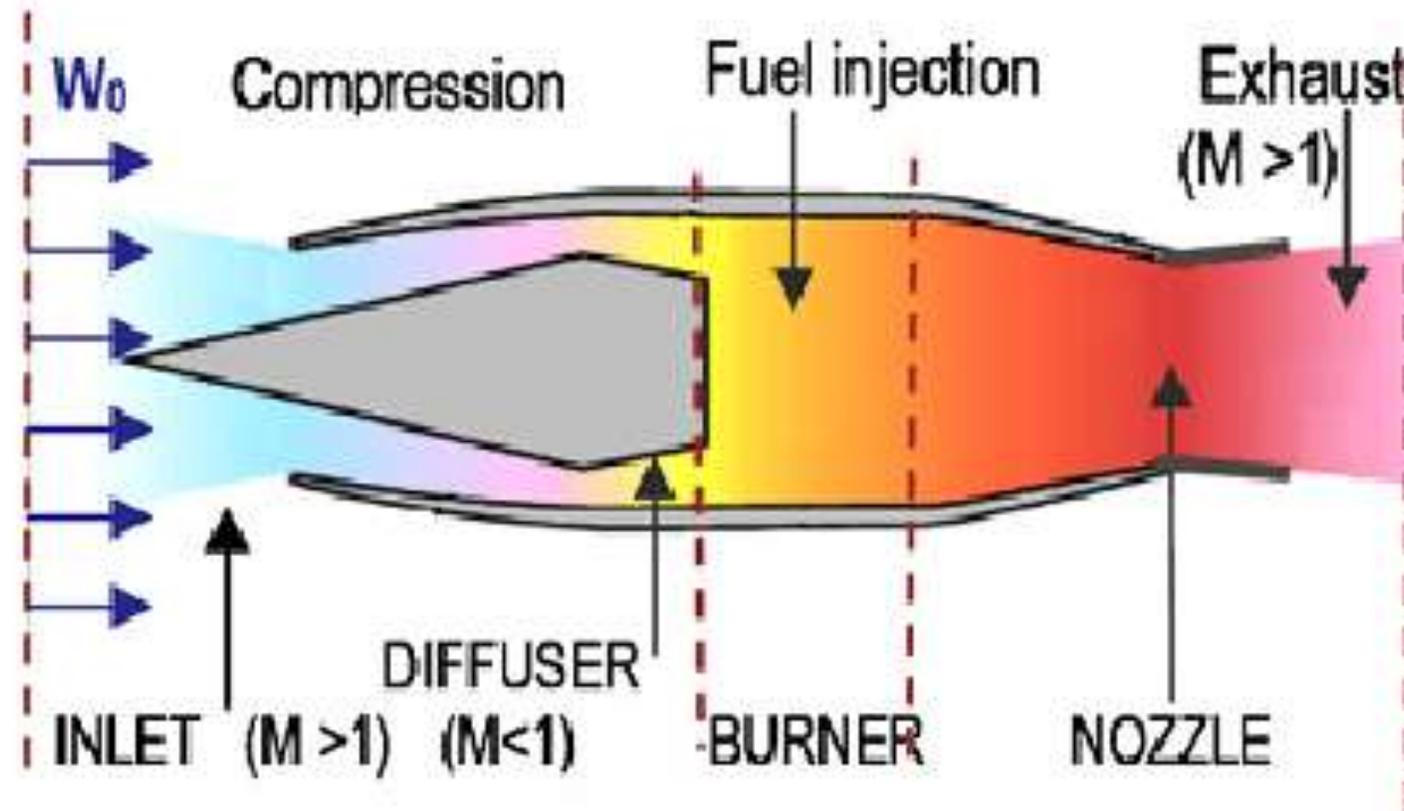
Turbojet engine



Turbo-prop engine



Ramjet engine



Rocket engine

