

Course Name

DATA STRUCTURES AND APPLICATIONS

Course Code

BCS304

Course Coordinator

Contact Hours

50

Mrs. MADHU NAGARAJ

CIE Marks

50

Assistant Professor

Dept of CSE-DS

ATMECE, Mysuru

SEE Marks

50

Course Learning Objectives

CLO 1. To explain fundamentals of data structures and their applications.

CLO 2. To illustrate representation of Different data structures such as Stack, Queues, Linked Lists, Trees and Graphs.

CLO 3. To Design and Develop Solutions to problems using Linear Data Structures

CLO 4. To discuss applications of Nonlinear Data Structures in problem solving.

CLO 5. To introduce advanced Data structure concepts such as Hashing and Optimal Binary Search Trees

Course Outcomes

CO 1. Explain different data structures and their applications.

CO 2. Apply Arrays, Stacks and Queue data structures to solve the given problems.

CO 3. Use the concept of linked list in problem solving.

CO 4. Develop solutions using trees and graphs to model the real-world problem.

CO 5. Explain the advanced Data Structures concepts such as Hashing Techniques and Optimal Binary Search Trees.



Text Book

Ellis Horowitz and Sartaj Sahni, Fundamentals of Data Structures in C, 2nd Ed, Universities Press, 2014.

Seymour Lipschutz, Data Structures Schaum's Outlines, Revised 1st Ed, McGraw Hill, 2014.



Reference Books

Seymour Lipschutz, Data Structures Schaum's Outlines, Revised 1st Ed, McGraw Hill, 2014.

Reema Thareja, Data Structures using C, 3rd Ed, Oxford press, 2012.

Jean-Paul Tremblay & Paul G. Sorenson, An Introduction to Data Structures with Applications, 2nd Ed, McGraw Hill, 2013

A M Tenenbaum, Data Structures using C, PHI, 1989

Robert Kruse, Data Structures and Program Design in C, 2nd Ed, PHI, 1996.



Question Paper Pattern

The question paper will have ten questions.

Each full Question consisting of 20 marks.

There will be 2 full questions (with a maximum of four sub questions) from each module.

Each full question will have sub questions covering all the topics under a module.

The students will have to answer 5 full questions, selecting one full question from each module.

- "Get your data structures correct first, and the rest of the program will write itself."
- -Davids Johnson

Program = Data Structure + Algorithm

“What is data?”

- data is a piece of information or simply set of values and data as such may not convey any meaning.
- The quantities, characters, or symbols on which a computer performs operations may be stored and transmitted in the form of electrical signals and recorded on magnetic, optical, or mechanical recording media.
- DATA and INFORMATION are often confusing, and we often interchange these two terms.
- UHDAM SI EMAN YM

What is information?”

- If data is arranged systematically, then it gets a structure and becomes meaningful.

The need for Data Structures?

- We can understand very well that the data needs to be managed in such a way so that it can produce some meaningful information.
- Data structures give us the way to manage the data appropriately so that we can use it effectively whenever possible.

Data Structures

Data Structure is a way to store and organize data so that it can be used efficiently in terms of time as well as space.

There are many ways of organizing the data in the memory, i.e., array.

Array is a collection of memory elements in which data is stored sequentially, i.e., one after another.

There are also other ways to organize the data in memory. Let's see the different types of data structures.

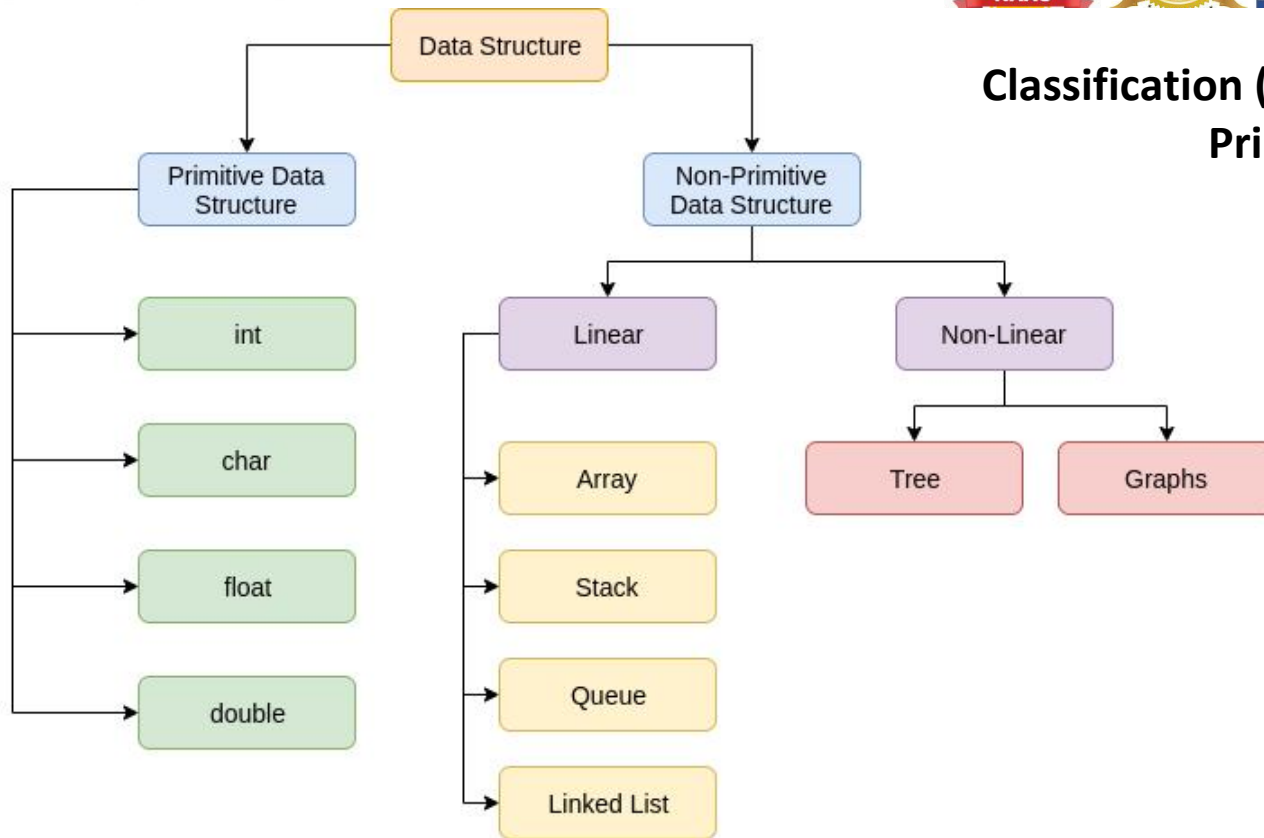
```

11001
10001 11100110
0010 110001 11000110
00101001 01011010 1100
010101 1100000100 100
00011111 101001110
00101 11010 10
10010 101
00100
01001
00110
0000110
    
```

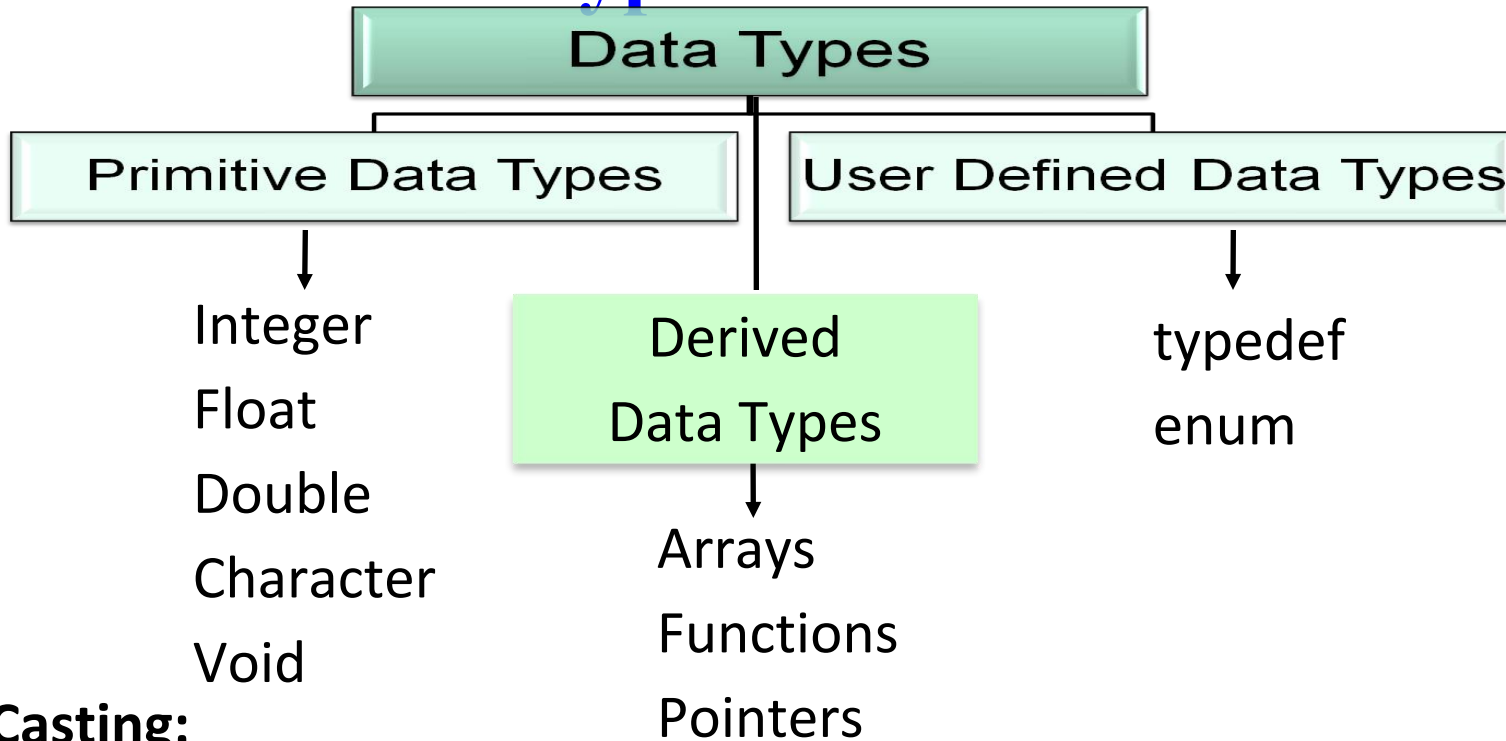
Data Structure

- Deals with how
 - - organization of data in memory
 - - efficient Storage of data in memory
 - - efficient Retrieved & manipulated
 - - logical relationships among different data items

Classification (Primitive and Non Primitive)



Data Types in C



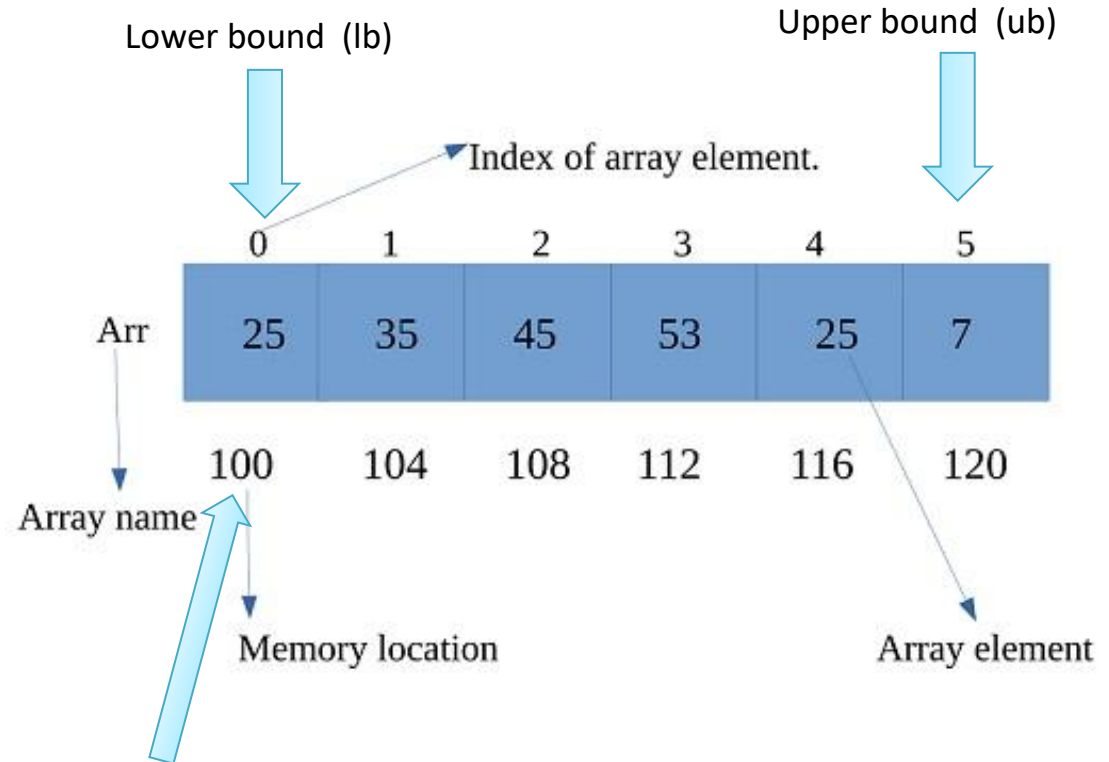
Type Casting:

`float div=float(a/b); //a & b are integer variables`

Data type	Purpose	No. of bytes allocated	Range
int	To hold integer constant	2 bytes	-32768 to +32767
float	To hold real constant	4 bytes	-3.4e38 to +3.4e38
double	To hold real constant	8 bytes	-1.7e308 to +1.7e308
char	To hold character constant	1 byte	-128 to +127
void	non-specific	No memory is allocated	-----

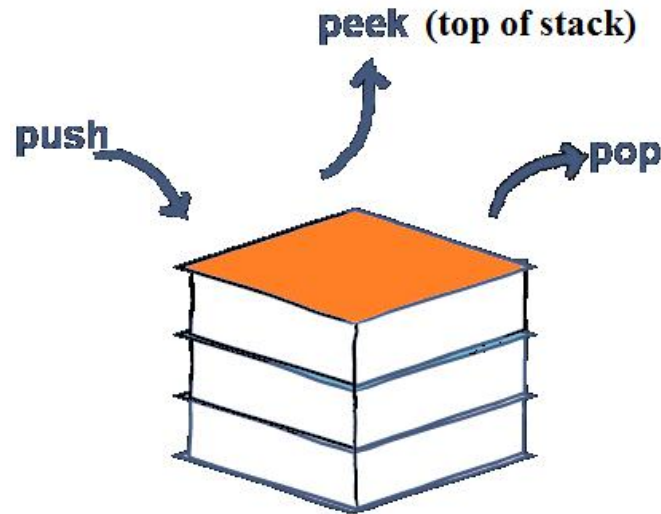
Array

- An array is a **data structure** for storing more than one data item that has a similar data type.
- The items of an array are allocated at adjacent memory locations.

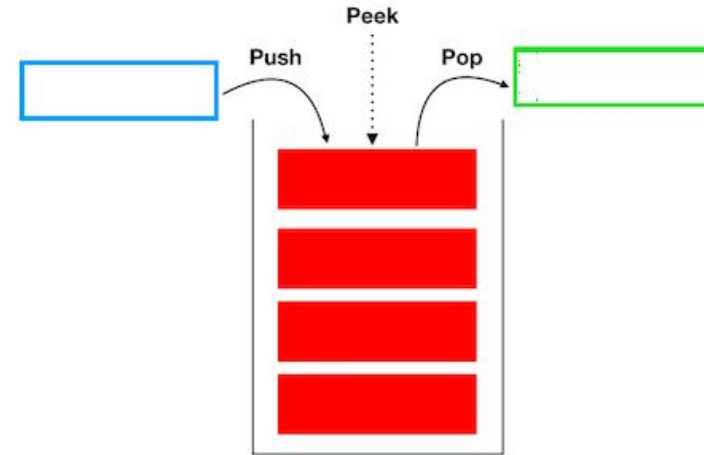


Stack

*Stack is a linear data structure which follows a particular order in which the operations are performed. The order may be **LIFO**(Last In First Out) or **FILO**(First In Last Out)*



Real Life Stack



Stack Data Structure

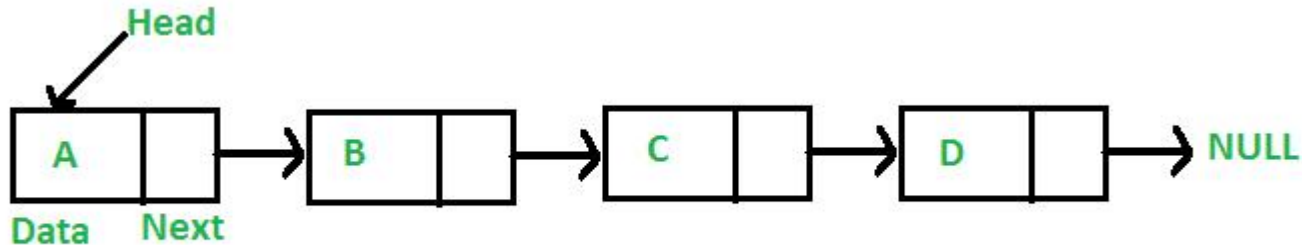
Queue

A Queue is a linear structure which follows a particular order in which the operations are performed. The order is **First In First Out (FIFO)**. A good example of a queue is any queue of consumers for a resource where the consumer that came first is served first.



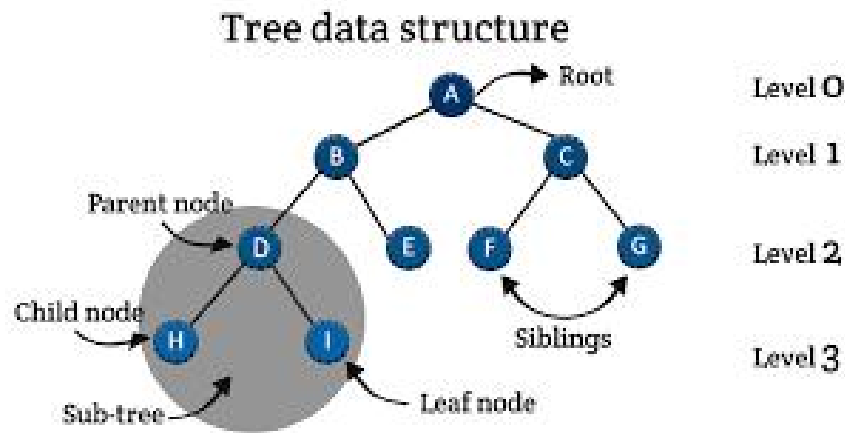
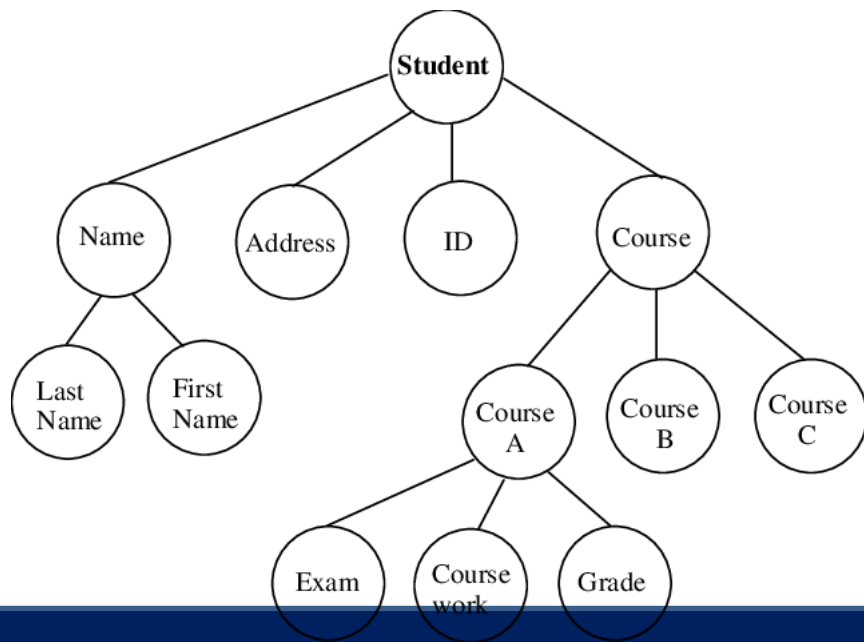
Linked List

A linked list is a linear data structure, in which the elements are not stored at contiguous memory locations. The elements in a linked list are linked using pointers as shown in the below image:



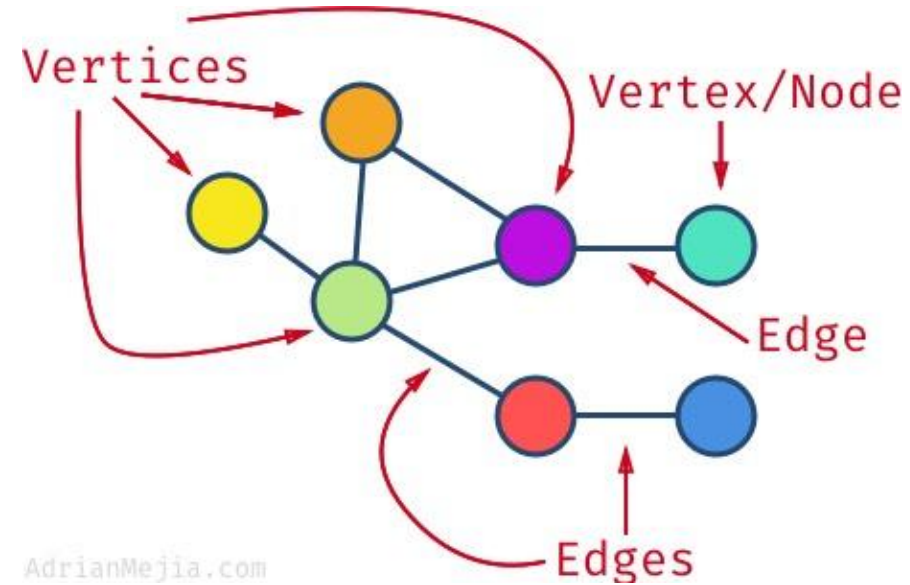
Tree

Data frequently contain a hierarchical relationship between various elements. The data structure which reflects this relationship is called a rooted tree graph or a tree.



Graph

- A Graph is a non-linear data structure consisting of nodes and edges. The nodes are sometimes also referred to as vertices and the edges are lines or arcs that connect any two nodes in the graph.
- A Graph consists of a finite set of vertices (or nodes) and set of Edges which connect a pair of nodes.



Data Structure Operations

Traversing: *Traversing a Data Structure means to visit the element stored in it. This can be done with any type of DS.*

Searching: *Searching means to find a particular element in the given data-structure. It is considered as successful when the required element is found.*

Insertion: *It is the operation which we apply on all the data-structures. Insertion means to add an element in the given data structure.*

Deletion: *It is the operation which we apply on all the data-structures. Deletion means to delete an element in the given data structure.*

Sorting: *Sorting means arranging the data either in ascending or on decending.*

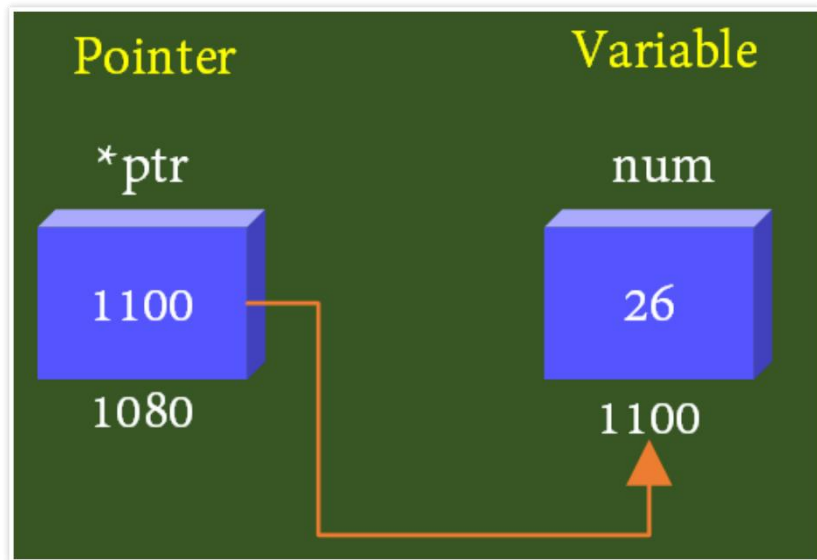
Pointers

-> **Pointer is a variable which can hold the address of another variable**

-> An alternative method to access the content of a memory location

1) Direct method

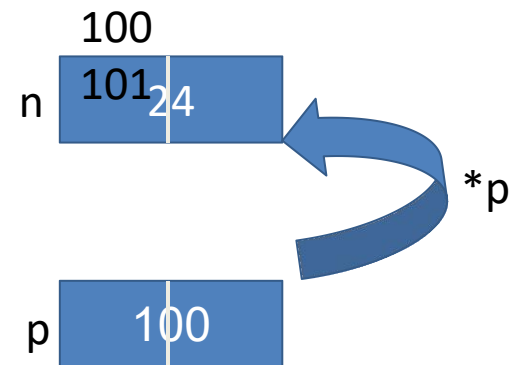
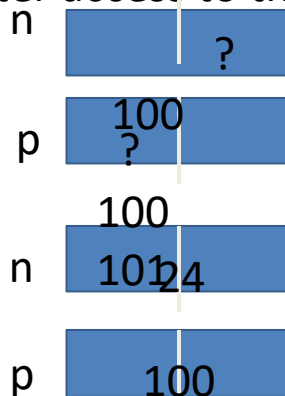
```
int num;
num=26;
printf("the content of the num is %d", num);
Printf("the address of the num is %x", &num); .
```



2. Indirect method (by using a pointer)

- Creation of a pointer (declaration)
- Assigning the created pointer the address
- De-referencing the pointer access to the data

```
int n;  
int *p;  
n=24;  
p=&n;  
printf("%d", *p);
```



Output: 24

Syntax for declaring a pointer

datatype * variable;

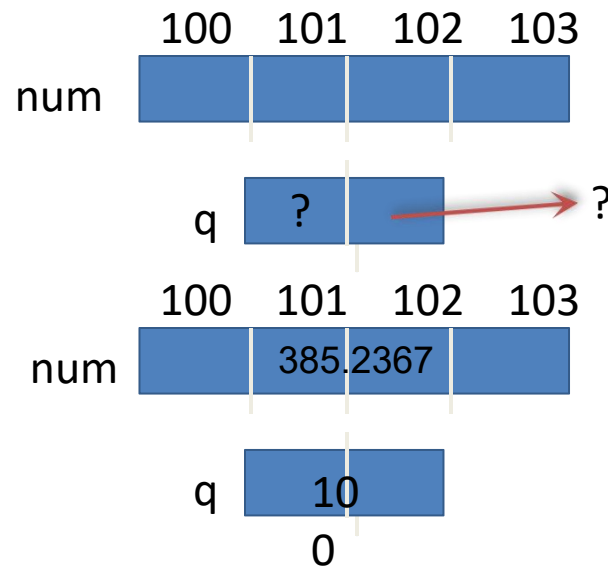
Ex: `int *p;`
`float *q;`
`double *r;`

`float num;`

`float *q;`

`num=385.2367;`

`q=#`



Dangling pointers: Created pointers are not pointing to any particular variable

Pointer can be declared and initialized in the same line

```
int a;  
a=10;
```

```
int a=10;
```

or

```
int *p;  
p=&a;
```

```
int *p=&a;
```

In indirect method * is used for 2 purpose

1) To create a pointer

```
int *p;
```

2) To de reference a pointer

```
*p;
```

In C language * is used for 3 purpose

1) To create a pointer

```
int *p;
```

2) To de reference a pointer

```
*p;
```

3) To multiply 2 variables

```
a * b;
```

1.

```
int n=5;  
int p;  
p=&n;  
printf("%d", *p);
```

2.

```
int n=5;  
int *p;  
p=n;  
printf("%d", *p);
```

3.

```
int n=5;  
int *p;  
p=&n;  
printf("%d", p);
```

4.

```
int n=5;  
float *p;  
p=&n;  
printf("%d", *p);
```

Accessing variables through pointer

```
#include <stdio.h>
```

```
void main()
```

```
{
```

```
    int a,b,c;
```

```
    int *p, *q;
```

```
    a=5;
```

```
    b=10;
```

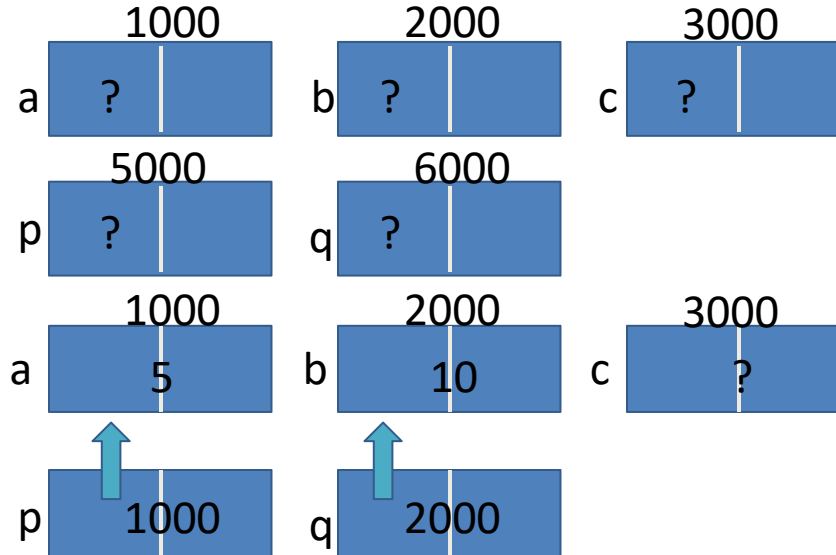
```
    p=&a;
```

```
    q=&b;
```

```
    c=*p+*q;
```

```
    printf("c is:%d",c);
```

```
}
```



Output:
c is: 15

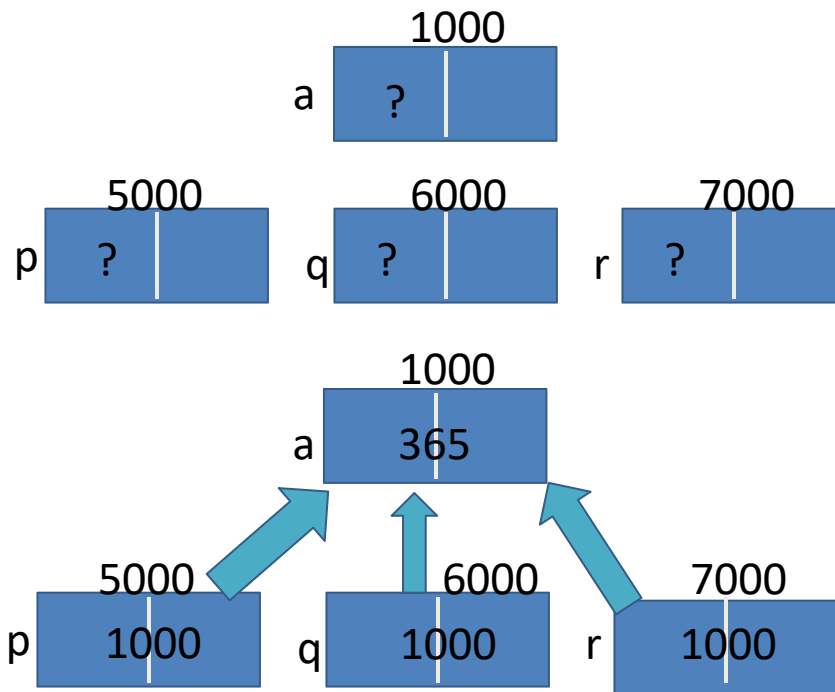
Can there be more than one pointer to a variable?

```
#include <stdio.h>
void main()
{
    int a;
    int *p,*q,*r;

    a=365;

    p=&a;
    q=&a;
    r=&a;

    printf("the value of a is:%d\n", a);
    printf("the value of p is:%d\n",*p);
    printf("the value of q is:%d\n",*q);
    printf("the value of r is:%d\n",*r);
}
```



Difference between pointer variable and normal variable

Pointer Variable	Normal Variable
1. Pointer Variable holds the address	1. A normal variable holds data
2. <code>int *p;</code>	2. <code>int a;</code>
3. We must de-reference a pointer to access data	3. There is no need to de-reference a normal variable to access data

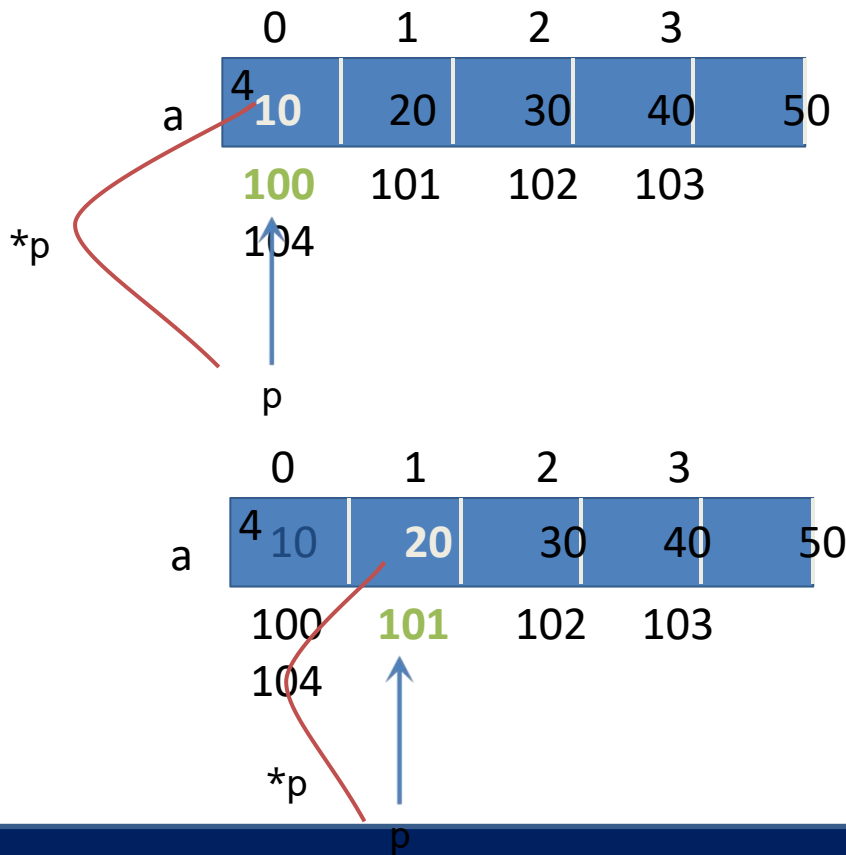
Pointers and Arrays

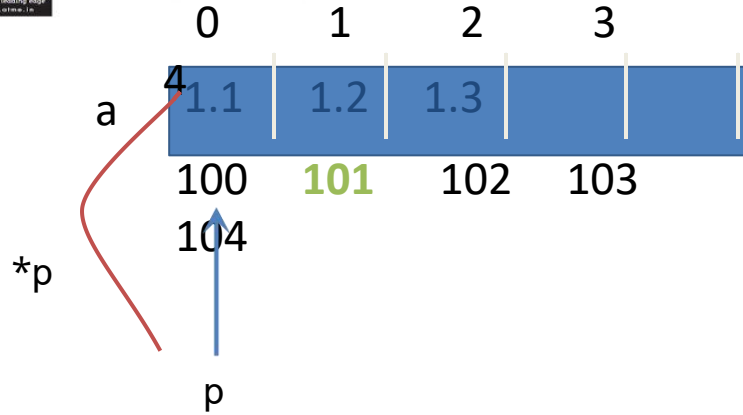
```
int a[5]={10,20,30,40,50};
```

```
int *p;
```

```
p=&a[0]; or p=a;
```

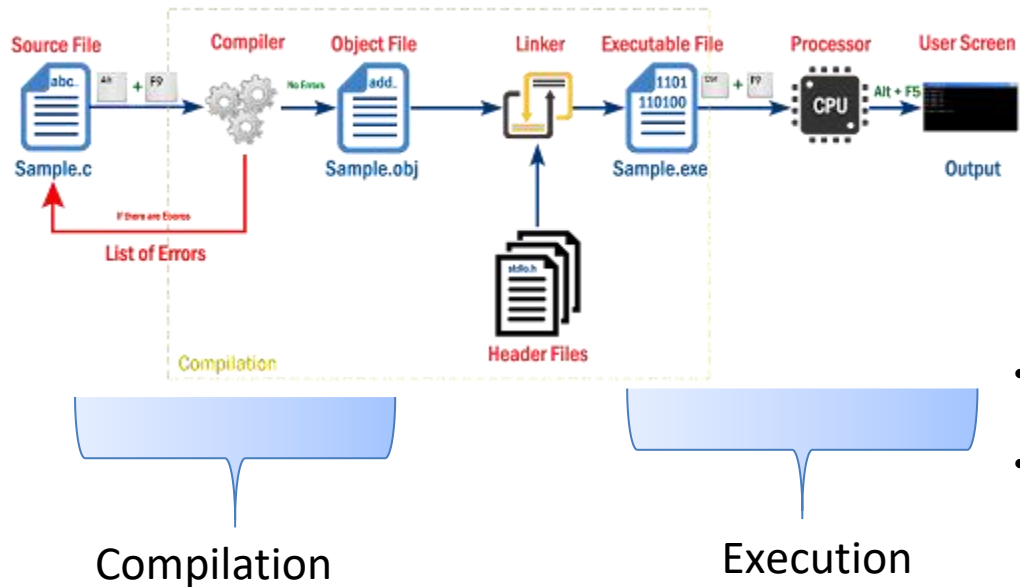
```
for(int i=0; i<4; i++)
{
    printf("%d\t", *p);
    p++;
}
```





$\text{sum} = \text{sum} + *(p+i)$
 $\text{Sum} = 0.0 + 1.1 = 1.1$
 $\text{Sum} = 1.1 + 1.2 = 2.3$
 $\text{sum} = 2.3 + 1.3 = \text{dfkdj}$

Dynamic memory allocation



- Conversion from HLL to MLL
- Decision to allocate memory to variable

- Execution of machine level instructions
- Decision to allocate memory to variable

Static Memory Allocation

Dynamic Memory Allocation

- **Static Memory Allocation**

- Wastage of memory
- Reediting is a time consuming process

Dynamic Memory Allocation

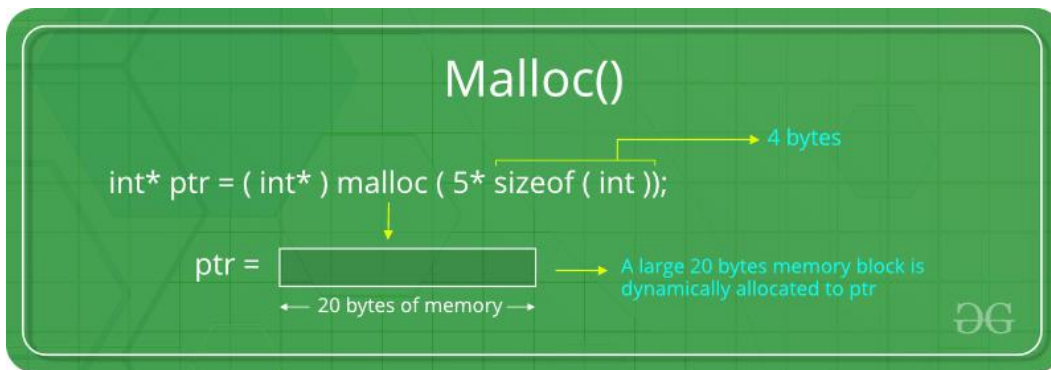
- malloc()
- calloc()
- realloc()
- free()

malloc()

- malloc stands for Memory allocation
- General form of memory allocation using malloc is,

datatype *ptr = (datatype *) malloc(RequiredAmountOfMemory * sizeof(datatype));

If malloc() is unable to find the required amount of memory, it returns **NULL**



```
void main()
{
    int n,i;
    printf("enter the
number of elements\n");
    scanf("%d",&n);

    int *p = (int
*)malloc(n*sizeof(int));

    if(p == NULL)
    {
        printf("enough
memory not available");
        exit(0);
    }
}
```

```
printf("enter array elements\n");
for(i=0; i<n; i++)
{
    scanf("%d", p+i);
}

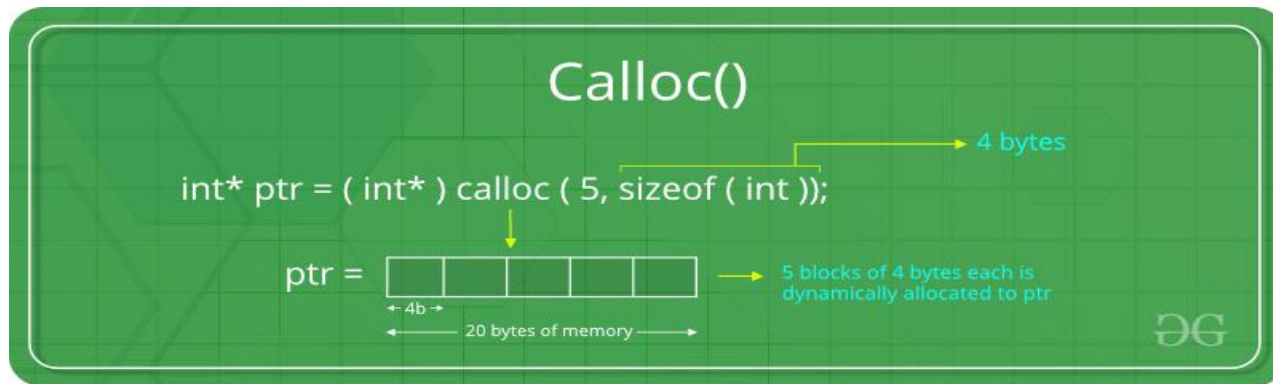
printf("array elements are\n");
for(i=0; i<n; i++)
{
    printf("%d\t", *(p+i));
}
}
```

calloc()

- calloc stands for Contiguous allocation
- General form of memory allocation using calloc is,

datatype *ptr = (datatype *) calloc(RequiredAmountOfMemoryForElements, sizeof(datatype));

If calloc() is unable to find the required amount of memory, it returns **NULL**



```
void main()
{
    int n,i;
    printf("enter the number of
elements\n");
    scanf("%d",&n);
    int *p = (int
*)calloc(n,sizeof(int));

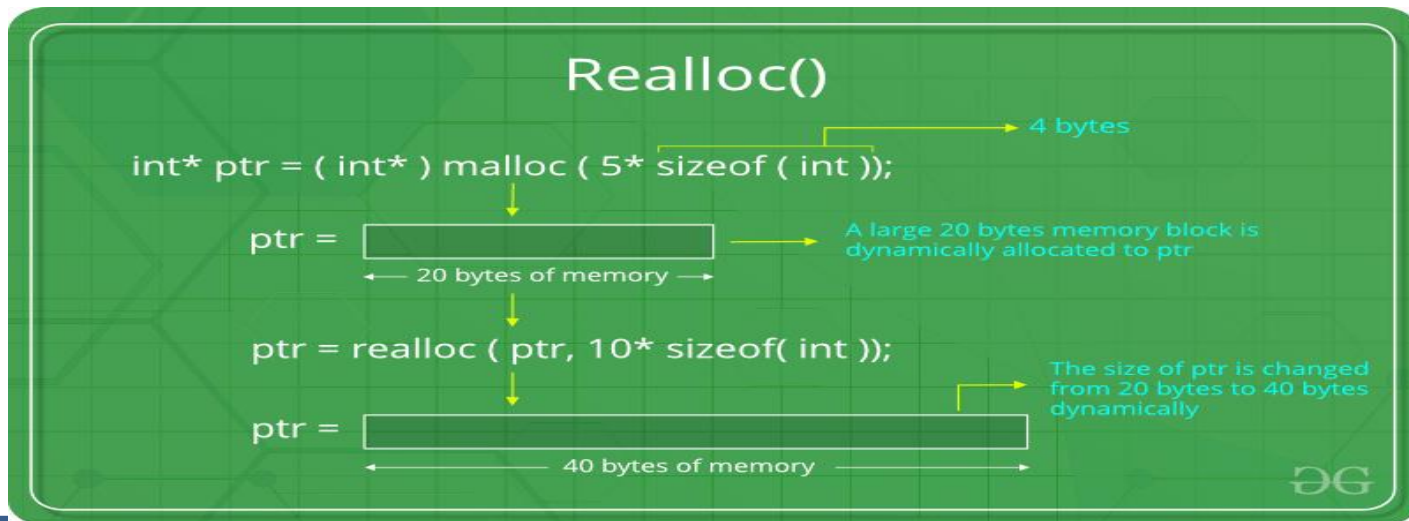
    if(p == NULL)
    {
        printf("enough memory not
available");
        exit(0);
    }
```

```
printf("enter array elements\n");
for(i=0; i<n; i++)
{
    scanf("%d", p+i);
}
printf("array elements are\n");
for(i=0; i<n; i++)
{
    printf("%d\t", *(p+i));
}
}
```

realloc()

- realloc stands for re allocation
- General form of memory allocation using realloc is,

`ptr = (datatype *) realloc(p, newsize*sizeof(datatype));`





void main()

```
{
    int n,i,new;
    printf("enter the number of elements\n");
    scanf("%d",&n);
    int *p = (int *)malloc(n*sizeof(int));
    if(p == NULL)
    {
        printf("enough memory not available");
        exit(0);
    }
    printf("enter array elements\n");
    for(i=0; i<n; i++)
    {
        scanf("%d", p+i);
    }
    printf("array elements are\n");
```

```
for(i=0; i<n; i++)
{
    printf("%d\t", *(p+i));
}
printf("\nenter the new number of elements\n");
scanf("%d",&new);
p=(int *)realloc(p,new*sizeof(int));
printf("enter array elements\n");
for(i=0; i<new; i++)
{
    scanf("%d", p+i);
}
printf("array elements are\n");
for(i=0; i<new; i++)
{
    printf("%d\t", *(p+i)); }}
```



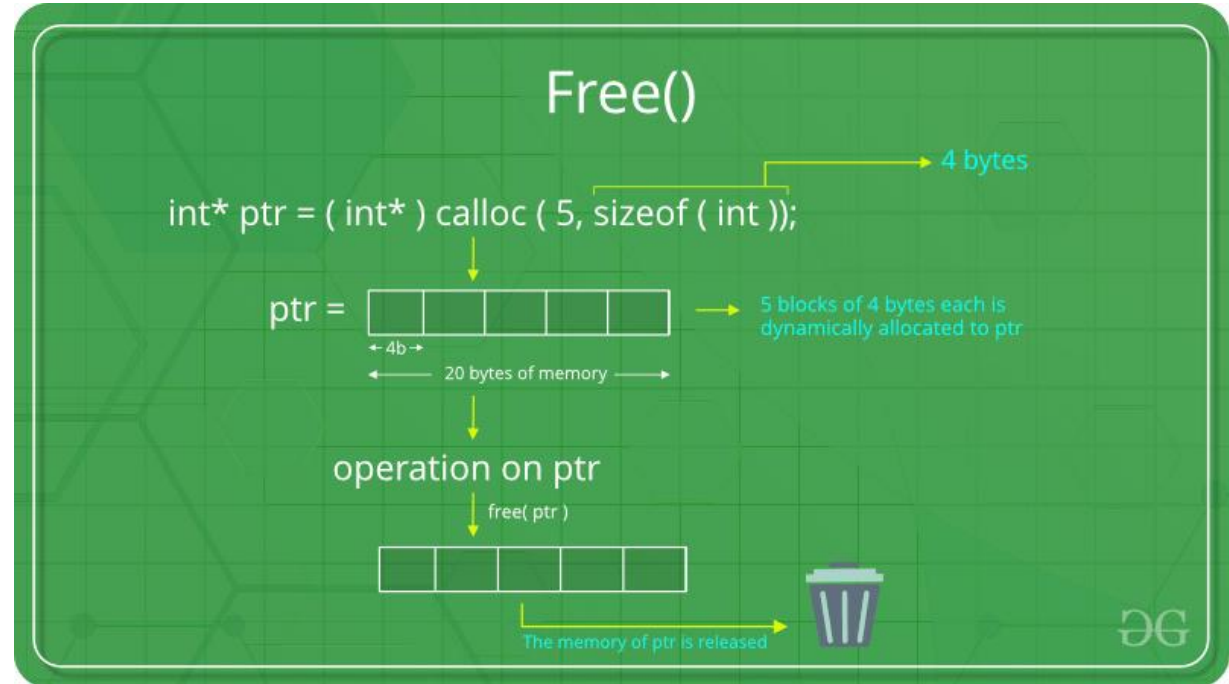
Dynamically allocated memory from `calloc()` or `malloc()` should be freed(released) using `free()`.

General format:

`void free(void *ptr);`

Or

`free(ptr);`




```
void main()
{
    int n,i;
    printf("enter the number of
elements\n");
    scanf("%d",&n);
    int *p = (int
*)malloc(n*sizeof(int));
    if(p == NULL)
    {
        printf("enough memory
not available");
        exit(0);
    }
    printf("enter array
elements\n");
```

```
for(i=0; i<n; i++)
{
    scanf("%d", p+i);
}
printf("array elements are\n");
for(i=0; i<n; i++)
{
    printf("%d\t", *(p+i));
}
free(p);
}
```

Dynamically allocated Arrays

```
#include <stdio.h>
#include <stdlib.h>
void main()
{
    int r = 3, c = 4, i; //Taking number of Rows and Columns
    int *ptr; //creating pointer
    ptr = (int *)malloc((r * c) * sizeof(int)); //Dynamically Allocating Memory (12*2=24)
    for(i = 0; i < r * c; i++)
    {
        ptr[i] = i + 1; //Giving value to the pointer and simultaneously printing it.
        printf("%d ", ptr[i]);
        if ((i + 1) % c == 0)
        {
            printf("\n");
        }
    }
    free(ptr);
}
```

Review of Arrays



Tree



Array of trees



Student



Array of students

35

23

45

20

100

70

35.5

11.5

34.3

15.9

90.6

46.7

m

a

t

u

w

r

**Array means, a series of entities or a sequence of entities of the same type (homogeneous).
In C language entities can be char, int, float and double type data**

Declaration of 1-D array

Syntax:

datatype arrayname[size];

Ex: int a[5];

float b[5];

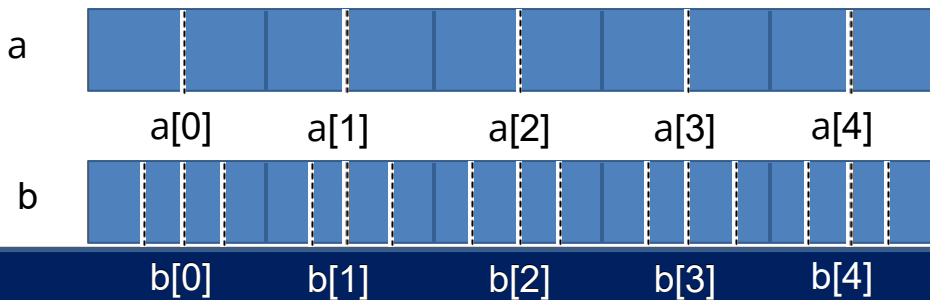
A declaration statement tells the compiler,

->data type of the array

->name of the array

->size of the array

Compiler then allocate memory depending upon the declaration.



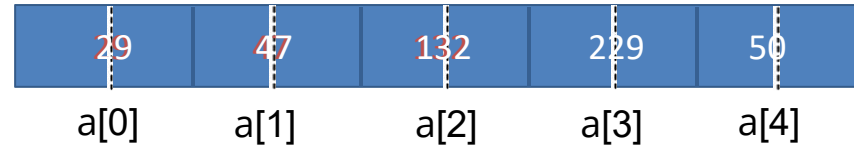
Initialization of 1-D array

1) Direct Initialization (Compile time initialization)

2) Initialization using a for loop (Run time initialization)

1) **Direct Initialization** : Mentioning array size is not compulsory.

Ex: `int a[5] = {29, 47, 132, 229, 50};`



Ex: `float b[5] = {29.3, 47.1, 132.4, 229.6, 50.3};`

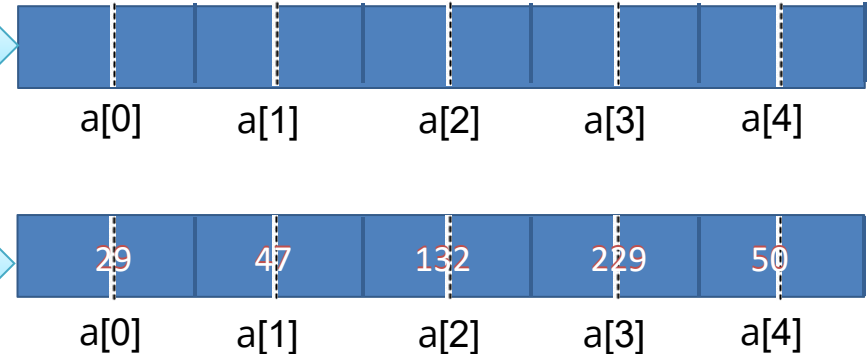


2) Initialization using a for loop:

->Using a for loop to initialize the array blocks

->Mentioning array size is compulsory

```
int a[5];
int i;
printf(" Enter an integer");
for(i=0; i<=4; i++)
{
    scanf("%d", &a[i]);
}
```



How do we store single integer in memory and how do we store array of integers in memory?

To store single integer,

```
int a = 35;
```

a

35

To store array of integers,

```
int a[5] = {35,39,87,53,28};
```

a

35	39	87	53	28
----	----	----	----	----

a[0] a[1] a[2] a[3] a[4]

Note: Array is a Indexed Data Structure

Total size of the array = size of the array * number of bytes per block
= 5 * 2
= 10 bytes

To find the number of elements in an array
 $ub - lb + 1$

To find the location of a particular index
 $Loc(a[i] = base(a) + w * (i - lb)$

Where, w is the word length

$w = 2$ or 4 or 8 for integers

$w = 4$ for float point values

$w = 8$ for double values

1. A car manufacturing company uses an array car to record number of cars sold each year starting from 1965 to 2015

i) Find the total number of years(elements)

ii) Suppose base address = 500, word length (w) = 4, find address of $\text{car}[1967]$, $\text{car}[1969]$ and $\text{car}[2015]$

2. Consider the linear arrays $\text{AAA}(5:50)$, $\text{BBB}(-5:10)$ and $\text{CCC}(1:18)$

i) Find the total number of elements in each array

ii) Suppose the $\text{Base}(\text{AAA}) = 300$ and $w=4$ for AAA. Find the address of $\text{AAA}[15]$, $\text{AAA}[35]$, $\text{AAA}[55]$

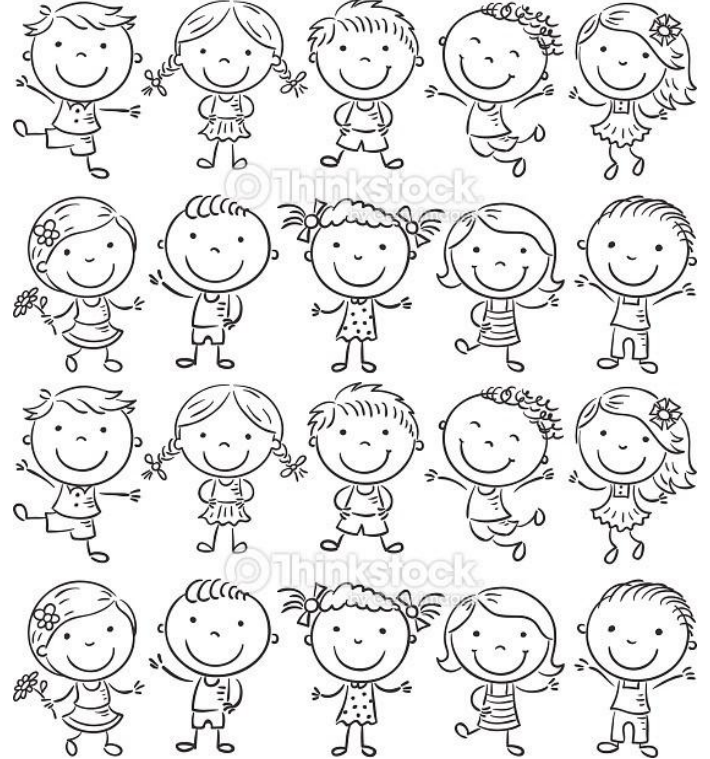
Two Dimensional Array



Student



1-D array of Students



2-D array of Student

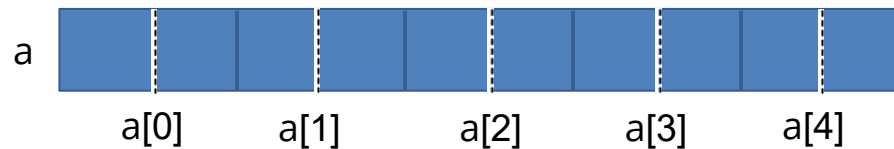
Why we need 2-D array?

To store matrices in the memory of a computer.

Int a;



Int a[50];



Int a[3][4];

	Column 0	Column 1	Column 2	Column 3
Row 0	a[0][0]	a[0][1]	a[0][2]	a[0][3]
Row 1	a[1][0]	a[1][1]	a[1][2]	a[1][3]
Row 2	a[2][0]	a[2][1]	a[2][2]	a[2][3]

Declaration of 2-D array

General Syntax:

datatype array name[no.of rows][no.of columns];

Declaration statement tell the compiler that

->the datatype of the array

->the name of the array

->the number of rows in the array

->the number of columns in the array

Ex:

int a[4][3];

	Col 0	Col 1	Col 2
row 0			
row 1			
row 2			
row 3			


Initialization of 2-D array

- > Direct Initialization
- > Using for-loops

1.Direct Initialization:

```
int a[4][3] = {{10,80,60},{30,5,19},{20,3,16},{18,15,100}};
```

	Col 0	Col 1	Col 2
row 0			
row 1			
row 2			
row 3			



10	80	60
30	5	19
20	3	16
18	15	100

```
int a[4][3] = {10,80,60,30,5,19,20,3,16,18,15,100};
```

```
int a[ ][3] = {10,80,60,30,5,19,20,3,16,18,15,100};
```

10	80	60
30	5	19
20	3	16
18	15	100

Mentioning the column dimension is important whereas row is optional

Illegal:

```
int a[4][ ] = {10,80,60,30,5,19,20,3,16,18,15,100};
```

```
int a[ ][ ] = {10,80,60,30,5,19,20,3,16,18,15,100};
```

2. Using a for loop to initialize the array blocks

```
int a[4][3];
for(i=0;i<4;i++)
{
    for(j=0;j<3;j++)
    {
        scanf("%d", &a[i][j]);
    }
}
```

	Col 0	Col 1	Col 2
row 0	[0][0]	[0][1]	[0][2]
row 1	[1][0]	[1][1]	[1][2]
row 2	[2][0]	[2][1]	[2][2]
row 3	[3][0]	[3][1]	[3][2]

C program to read 2 matrices A (mxn) and B (mxn) and perform addition or subtraction and print the matrices A,B and output matrix

5	10	15
1	3	9
6	2	8

+

3	5	1
7	2	9
5	3	5

=

8	15	16
8	5	18
11	5	13

5	10	15
1	3	9
6	2	8

-

3	5	1
7	2	9
5	3	5

=

2	5	14
-6	1	0
1	-1	3

```
#include<stdio.h>
void main()
{
    int i,j,a[3][3],b[3][3],c[3][3];

    printf("enter the elements for array A:\n");
    for(i=0;i<3;i++)
    {
        for(j=0;j<3;j++)
        {
            scanf("%d",&a[i][j]);
        }
    }
    printf("enter the elements for array B:\n");
    for(i=0;i<3;i++)
    {
        for(j=0;j<3;j++)
        {
            scanf("%d",&b[i][j]);
        }
    }
}
```

```
//printing matrix A
printf("array A is :\n");
for(i=0;i<3;i++)
{
    for(j=0;j<3;j++)
    {
        printf("%d\t",a[i][j]);
    }
    printf("\n");
}
//printing matrix B
printf("array B is :\n");
for(i=0;i<3;i++)
{
    for(j=0;j<3;j++)
    {
        printf("%d\t",b[i][j]);
    }
    printf("\n");
}
```

```
//adding 2 matrices
for(i=0;i<3;i++)
{
    for(j=0;j<3;j++)
    {
        c[i][j]=a[i][j]+b[i][j];
    }
}

//printing resultant matrix
printf("array after addition :\n");
for(i=0;i<3;i++)
{
    for(j=0;j<3;j++)
    {
        printf("%d\t",c[i][j]);
    }
    printf("\n");
}
}
```

Structures

int a;

Student:

Name

Age

Marks

USN

float b;

Tree:

Name

No. of branches

height

struct student

{

char name[5];

int age;

int marks;

char USN;

};

struct tree

{

char name[5];

int No.of branches;

float height;

};

Structures

Structure provides a mechanism for the programmer to create his/her own data type called **"user defined data type"**

Keyword for
creating
structure

struct student

{

char name[20];

int age;

int marks;

float height;

};

Name of the
structure

Structure
members/d
ata

Syntax

struct structure_name

```
{  
    datatype member variable 1;  
    datatype member variable 2;  
    datatype member variable 3;  
    datatype member variable 4;  
};
```

Ex. 1

```
struct student  
{  
    char name[20];  
    int age;  
    int marks;  
    float height;  
};
```

Ex. 2

```
struct tree  
{  
    char name[5];  
    int No.of  
    branches;  
    float height;  
};
```

Structures

```
struct student  
{  
    char name[5];  
    int age;  
    int marks;  
    float height;  
};
```

```
struct tree  
{  
    char name[5];  
    int No.of branches;  
    float height;  
};
```

To access members of a structure, a structure variable has to be created

```
struct student s1;
```

```
struct tree t1;
```

```
struct student
{
    char name[5];
    int age;
    int marks;
    float height;
};
```

struct student s1;

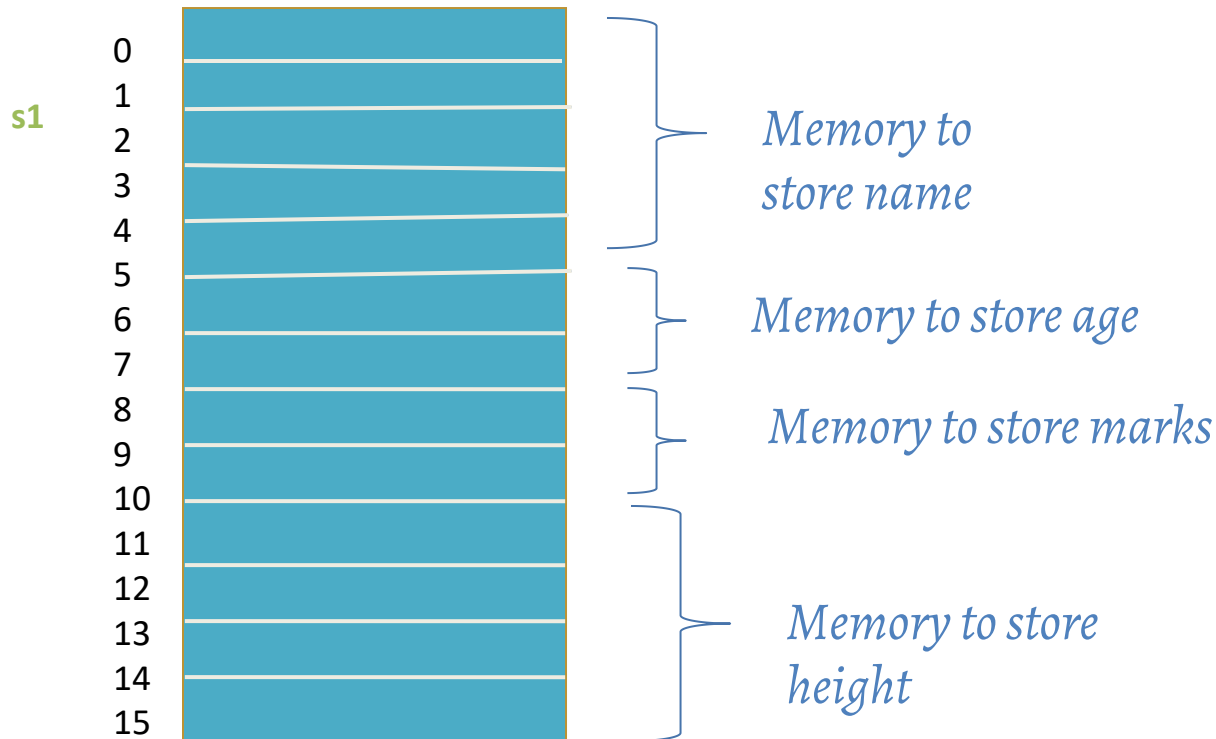


Fig: Memory for structure member

t1

struct tree

```
{
    char name[5];
    int noofbranches;
    float height;
};
```

struct tree t1;

t1.name="teak";

t1.noofbranches=23;

t1.height=31.71;

.(dot) -> Member access operator

0	t
1	e
2	a
3	k
4	/0
5	
6	
7	23
8	
9	
10	
11	31.71
12	
13	
14	
15	



//program to read and display student details using structures
#include <stdio.h>

struct student

```
{  
    char name[20];  
    int age;  
    int marks;  
    float height;  
};
```

void main()

```
{  
    struct student s1;  
    printf("Enter Student Details\n");  
    printf("enter the name of the student\n");  
    scanf("%s", s1.name);  
    printf("enter student age\n");  
    scanf("%d", &s1.age);  
    printf("enter student marks\n");  
    scanf("%d", &s1.marks);  
    printf("enter student height\n");  
    scanf("%f", &s1.height);  
    printf("Student details you entered:\n");  
    printf("Student name is: %s\n", s1.name);  
    printf("Student age is: %d\n", s1.age);  
    printf("Student marks is: %d\n", s1.marks);  
    printf("student height is: %.2f\n", s1.height);  
}
```



```
//program to read and display tree details using structures
#include <stdio.h>
struct tree
{
    char name[20];
    float height;
    int noofbranches;
};
void main()
{
    struct tree t1;

    printf("enter the name of the tree\n");
    scanf("%s", t1.name);
    printf("enter tree height\n");
    scanf("%f", &t1.height);
    printf("enter number of noofbranches\n");
    scanf("%d", &t1.noofbranches);

    printf("the tree name is: %s\n",t1.name);
    printf("the tree height is: %f\n",t1.height);
    printf("noofbranches in the tree are: %d\n",t1.noofbranches);

}
```

<i>Array</i>	<i>Structure</i>
<i>Array is a collection of related data elements of same data type. (homogeneous data)</i>	<i>Structure is collection of logically related data elements of different data types. (heterogeneous data)</i>
<i>Array data are accessed using index</i>	<i>Structure data are accessed using structure name and dot operator</i>
<i>No key word is used to create array</i>	<i>Struct keyword is used create structure</i>
<i>Each element will be of same size</i>	<i>Size of the elements can be different</i>



```
#include <stdio.h>
```

```
struct tree
```

```
{
```

```
    char name[20];
```

```
    float height;
```

```
    int noofbranches;
```

```
};
```

```
void disp(struct tree tr)
```

```
{
```

```
    printf("the tree name is: %s\n",tr.name);
```

```
    printf("the tree height is: %f\n",tr.height);
```

```
    printf("noofbranches in the tree are:
```

```
%d\n",tr.noofbranches);
```

```
}
```

```
void main()
```

```
{
```

```
    struct tree t1;
```

```
    printf("enter the name of the tree\n");
```

```
    scanf("%s", t1.name);
```

```
    printf("enter tree height\n");
```

```
    scanf("%f", &t1.height);
```

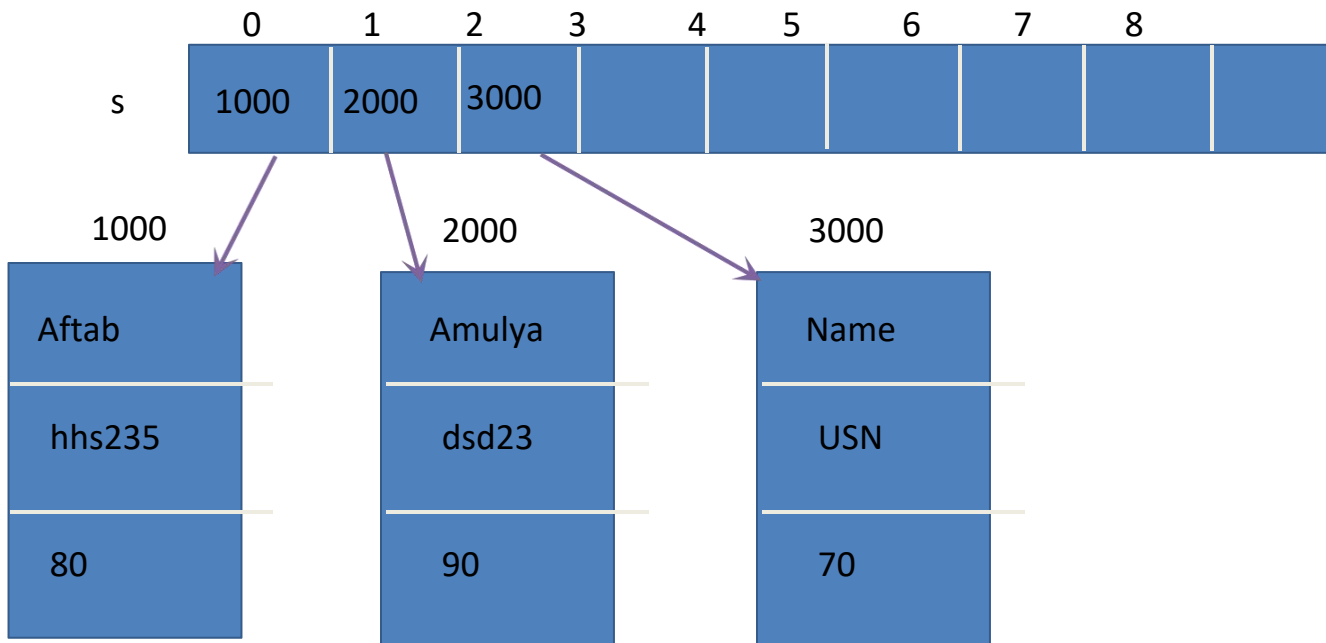
```
    printf("enter number of noofbranches\n");
```

```
    scanf("%d", &t1.noofbranches);
```

```
    disp(t1);
```

```
}
```

Array of Structures



Array of Structures

```
#include <stdio.h>
struct tree
{
    char name[20];
    float height;
    int noofbranches;
};
```

```
void main()
{
    struct tree t1[2];

    for(int i=0; i<=1; i++)
    {
        printf("enter the name of the tree\n");
        scanf("%s", t1[i].name);
        printf("enter tree height\n");
        scanf("%f", &t1[i].height);
        printf("enter number of noofbranches\n");
        scanf("%d", &t1[i].noofbranches);
    }

    for(int i=0; i<=1; i++)
    {
        printf("the tree name is: %s\n", t1[i].name);
        printf("the tree height is: %f\n", t1[i].height);
        printf("noofbranches in the tree are: %d\n", t1[i].noofbranches);
    }
}
```

Typedefing a Structures

```
typedef struct  
{
```

```
    char name[10];  
    int usn;  
}student;
```

```
#include<stdio.h>  
typedef struct  
{  
    char name[10];  
    int usn;  
}student;  
void main()  
{  
    student s1;  
    printf("enter student name:\n");  
    scanf("%s", s1.name);  
    printf("enter student usn:\n");  
    scanf("%d", &s1.usn);  
    printf("student name is %s",s1.name);  
    printf("student usn is %d", s1.usn);  
}
```


Different ways of writing a program using structure

```
#include<stdio.h>
struct student
{
    char name[10];
    int usn;
};
```

```
void main()
{
    struct student s1;
    printf("enter student name:\n");
    scanf("%s", s1.name);
    printf("enter student usn:\n");
    scanf("%d", &s1.usn);
    printf("student name is
%s\n",s1.name);
    printf("student usn is %d", s1.usn);
}
```

```
#include<stdio.h>
struct student
{
    char name[10];
    int usn;
}s1;
```

```
void main()
{
    printf("enter student name:\n");
    scanf("%s", s1.name);
    printf("enter student usn:\n");
    scanf("%d", &s1.usn);
    printf("student name is
%s\n",s1.name);
    printf("student usn is %d",
s1.usn);
}
```

```
#include<stdio.h>
typedef struct
{
    char name[10];
    int usn;
}student;
```

```
void main()
{
    student s1;
    printf("enter student name:\n");
    scanf("%s", s1.name);
    printf("enter student usn:\n");
    scanf("%d", &s1.usn);
    printf("student name is
%s\n",s1.name);
    printf("student usn is %d", s1.usn
}
```

Structure within a structure

```
typedef struct {  
    int month;  
    int day;  
    int year;  
}date;
```

```
typedef struct {  
    char name[10];  
    int age;  
    float salary;  
    date dob;  
} humanBeing;
```

OR

```
typedef struct {  
    char name[10];  
    int age;  
    float salary;  
    struct {  
        int month;  
        int day;  
        int year;  
    } date;  
} humanBeing;
```

```
humanBeing person1;
```

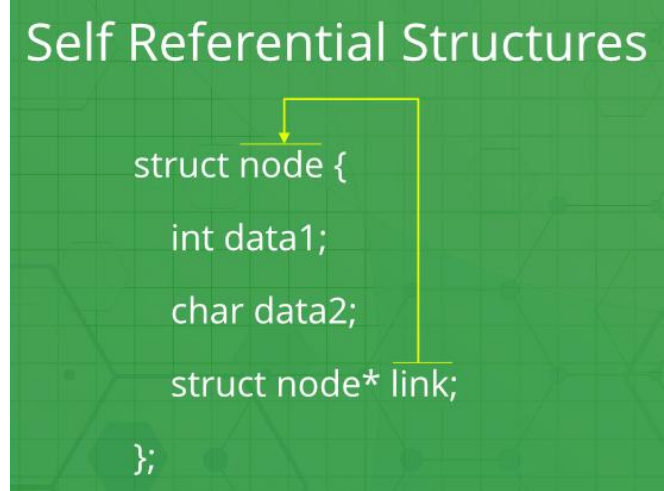
```
#include<stdio.h>
struct address
{
    char city[20];
    int pin;
    char phone[14];
};
struct employee
{
    char name[20];
    struct address add;
};
void main ()
{
    struct employee emp;
    printf("Enter employee information?\n");
    scanf("%s %s %d %s",emp.name,emp.add.city, &emp.add.pin, emp.add.phone);
    printf("Printing the employee information....\n");
    printf("name:%s\nCity:%s\nPincode:%d\nPhone:%s",emp.name,emp.add.city,emp.add.pin,emp.add.phone);
}
```

A self-referential structure is one in which one or more of its components is a pointer to itself. Self referential structures usually require dynamic storage management routines (malloc and free) to explicitly obtain and release memory.

```
typedef struct {  
  
    char data;  
    struct list *link ;  
  
} list;
```

Self Referential Structures

```
struct node {  
    int data1;  
    char data2;  
    struct node* link;  
  
};
```



Each instance of the structure list will have two components data and link.

- Data: is a single character,
- Link: link is a pointer to a list structure. The value of link is either the address in memory of an instance of list or the null pointer.

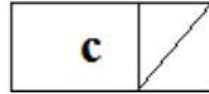
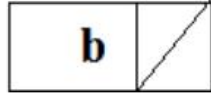
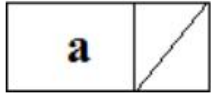
```
list item1, item2, item3;
```

```
item1.data = 'a';
```

```
item2.data = 'b';
```

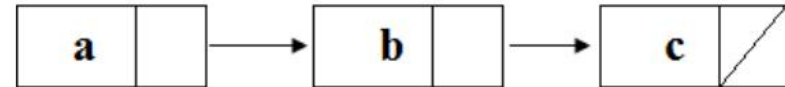
```
item3.data = 'c';
```

```
item1.link = item2; item2.link = item3; item3.link = NULL;
```



```
item1.link = &item2;
```

```
item2.link = &item3;
```



A union is similar to a structure, it is collection of data similar data type or dissimilar.

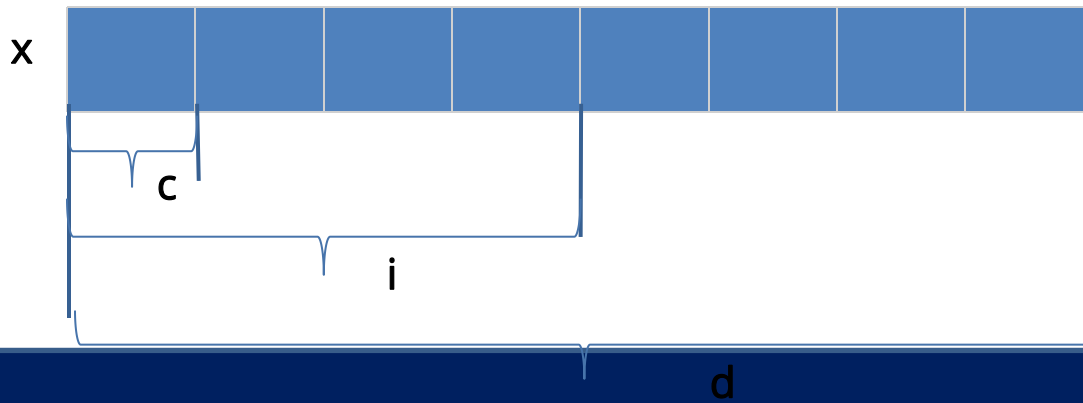
Syntax:

```
union tag_name{  
    data_type member 1;  
    data_type member 2;  
    .....  
    .....  
    data_type member n;  
}variable_name;
```

```
typedef union
{
    int i;
    double d;
    char c;
}item;
```

```
union item
{
    int i;
    double d;
    char c;
};
```

item x;



Difference between Structure and Union

	STRUCTURE	UNION
Keyword	The keyword struct is used to define a structure	The keyword union is used to define a union.
Size	When a variable is associated with a structure, the compiler allocates the memory for each member. The size of structure is greater than or equal to the sum of sizes of its members.	when a variable is associated with a union, the compiler allocates the memory by considering the size of the largest memory. So, size of union is equal to the size of largest member.
Memory	Each member within a structure is assigned unique storage area of location.	Memory allocated is shared by individual members of union.
Value Altering	Altering the value of a member will not affect other members of the structure.	Altering the value of any of the member will alter other member values.
Accessing members	Individual member can be accessed at any time	Only one member can be accessed at a time.
Initialization of Members	Several members of a structure can initialize at once.	Only the first member of a union can be initialized.



```
#include<stdio.h>
void main()
```

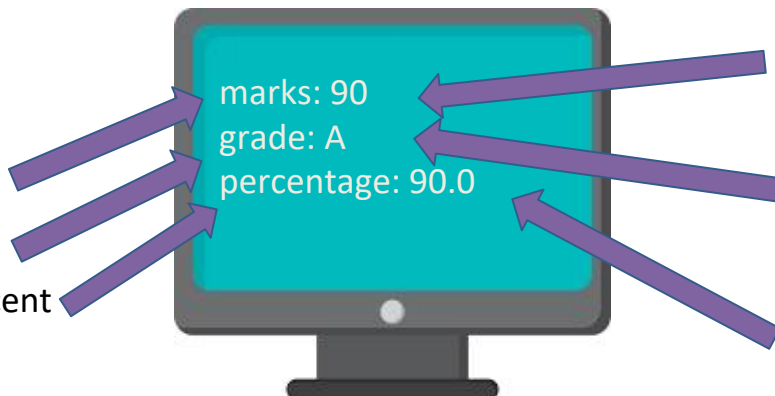
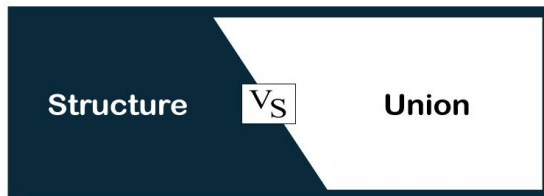
```
{
    typedef union
    {
        int marks;
        char grade;
        float percentage;
    }student;
```

```
student s;
```

```
s.marks=90;
printf("marks:%d\n",s.marks);
```

```
s.grade='A';
printf("Grade:%c\n",s.grade);
```

```
s.percentage=90.0;
printf("percentage:%f\n",s.percentage);
}
```



```
s.marks=90;
s.grade='A';
s.percentage=90.0;

printf("marks:%d\n",s.marks);
printf("Grade:%c\n",s.grade);
printf("percentage:%f\n",s.percent
age);
}
```

Bubble Sort Program

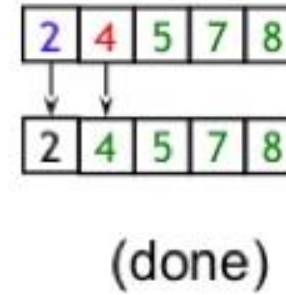
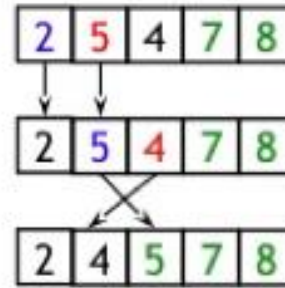
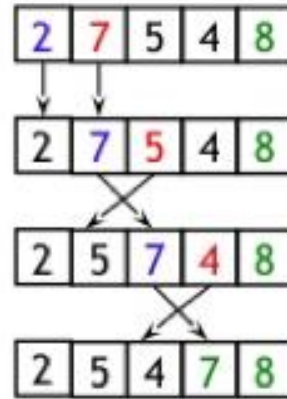
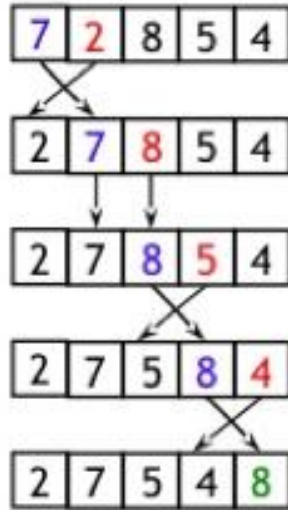
Bubble Sort is the simplest sorting algorithm that works by repeatedly swapping the adjacent elements if they are in wrong order.

Input array

0	1	2	3	4
7	2	8	5	4

Output array

0	1	2	3	4
2	4	5	7	8



```

for() //for the passes
{
    for() //for the operation
    {
        If(no. on left > no. on right)
        {
            Exchange or swap the numbers
        }
    }
}
    
```

```
for()           //for the passes
{
    for()       //for the operation
    {
        If(no. on left > no. on right)
        {
            Exchange or swap the numbers
        }
    }
}
```

If there are 5 elements in array then it will take 4 cycles to sort the array

If there are n elements then it will take n-1 cycles to sort the array

i.e from cycle 1 to less than n

Example to swap 2 numbers

a=10, b=20

```
temp=a;
a=b;
b=temp;
```

```
for(j=1; j<n; j++)
{
    for(i=0; i<n-j; i++)
    {
        If(a[i] > a[i+1])
        {
            temp=a[i];
            a[i]=a[i+1];
            a[i+1]=temp;
        }
    }
}
```

```
#include<stdio.h>
```

```
void main()
```

```
{
    int a[10], n, i;
    printf("Enter the number of elements\n");
    scanf("%d",&n);
    printf("Enter the array elements\n");
    for(i=0; i<n; i++)
    {
        scanf("%d", &a[i]);
    }

    bubble_sort(a,n);

    printf("The sorted array is\n");
    for(i=0; i<n; i++)
    {
        printf("%d\t", a[i]);
    }
}
```

```
void bubble_sort(int a[],int n)
```

```
{
    Int i,j,temp;
    for(j=1; j<n; j++)
    {
        for(i=0; i<n-j; i++)
        {
            if(a[i]> a[i+1])
            {
                temp=a[i];
                a[i]=a[i+1];
                a[i+1]=temp;
            }
        }
    }
}
```



#include<stdio.h>

```
void main()
{
    int a[100], n, i, pos, key;
    printf("\nEnter the number of elements\n");
    scanf("%d",&n);
    printf("\nEnter the elements in ascending order\n");
    for(i=0; i<n; i++)
    {
        scanf("%d", &a[i]);
    }
    printf("\nEnter the key element\n");
    scanf("%d", &key);
    pos = binary_search(key, a, n);
    if(pos == -1)
    printf("Key element not found\n");
    else
    printf("\nKey element %d found at position %d\n", key, pos);
}
```

```
int binary_search(int key, int a[], int n)
{
    int low = 0;
    int high = n-1;
    while(low <= high)
    {
        mid = (low+high)/2;
        if(key == a[mid])
            return mid;
        else if(key < a[mid])
            high = mid-1;
        else
            low = mid+1;
    }
    return -1;
}
```

Advantages:

- * Simple Technique
- * Very efficient searching technique

Disadvantages

- * The list of elements to be searched should be sorted.
- * It is necessary to obtain the middle element which is possible only if elements are stored in the array. If the elements are stored in linked list, this method can not be used.

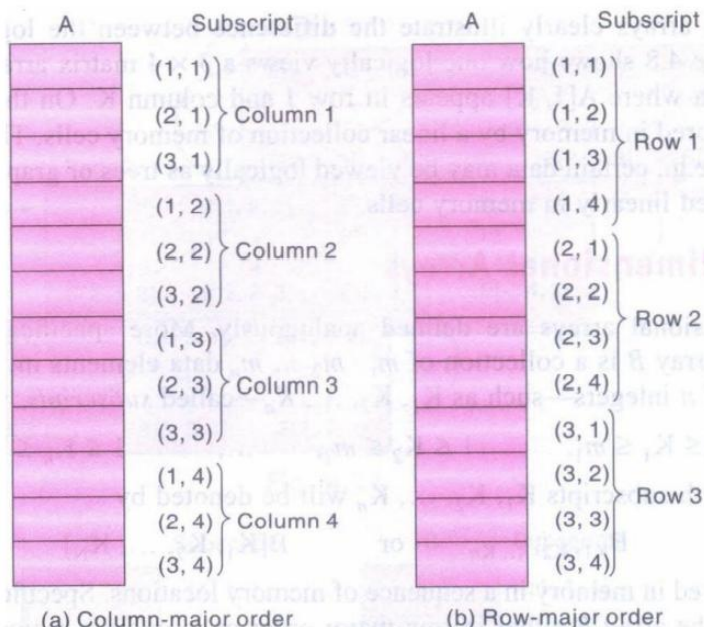
Two-dimensional arrays are called matrices in mathematics and tables in business applications. There is a standard way of drawing a two-dimensional $m \times n$ array A where the elements of A form a rectangular array with m rows and n columns and where the element $A[J, K]$ appears in row J and column K .

		Columns			
		1	2	3	4
Rows	1	$A[1, 1]$	$A[1, 2]$	$A[1, 3]$	$A[1, 4]$
	2	$A[2, 1]$	$A[2, 2]$	$A[2, 3]$	$A[2, 4]$
	3	$A[3, 1]$	$A[3, 2]$	$A[3, 3]$	$A[3, 4]$

Fig. Two-Dimensional 3×4 Array A

Let A be a two-dimensional $m \times n$ array. Although A is pictured as a rectangular array of elements with m rows and n columns, the array will be represented in memory by a block of $m \cdot n$ sequential memory locations.

The programming language will store the array A either (1) column by column, is called **column-major order**, or (2) row by row, in **row-major order**.



	Columns			
	1	2	3	4
Rows	1 $A[1, 1]$	$A[1, 2]$	$A[1, 3]$	$A[1, 4]$
2	$A[2, 1]$	$A[2, 2]$	$A[2, 3]$	$A[2, 4]$
3	$A[3, 1]$	$A[3, 2]$	$A[3, 3]$	$A[3, 4]$

Fig. Two-Dimensional 3×4 Array A

(Column-major order) $LOC(A[J, K]) = Base(A) + w[M(K - 1) + (J - 1)]$

(Row-major order) $LOC(A[J, K]) = Base(A) + w[N(J - 1) + (K - 1)]$

- A polynomial is a sum of terms, where each term has a form ax^e , where x is the variable, a is the coefficient and e is the exponent

$$A(x) = 3x^{20} + 2x^5 + 4$$

$$B(x) = x^4 + 10x^3 + 3x^2 + 1$$

The largest (or leading) exponent of a polynomial is called its degree. Coefficients that are zero are not displayed. The term with exponent equal to zero does not show the variable since x raised to a power of zero is 1.

Polynomial Representation

One way to represent polynomials in C is to use typedef to create the type polynomial as below:

```
#define MAX_TERMS 100 /*size of terms array*/
```

```
typedef struct
```

```
{
```

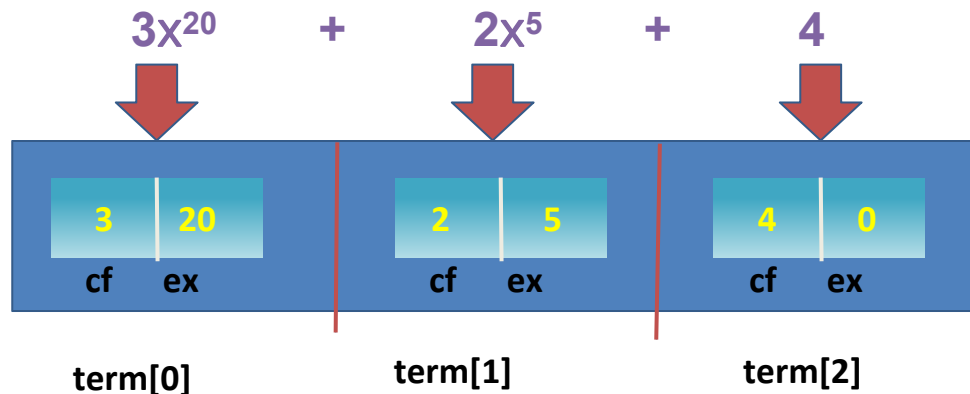
```
    float coef;
```

```
    int expon;
```

```
} polynomial;
```

```
polynomial terms[MAX_TERMS];
```

```
int avail = 0;
```



$$A(x) = 2x^{1000} + 1$$

$$B(x) = x^4 + 10x^3 + 3x^2 + 1$$

	startA	finishA	startB		finishB	avail
	↓	↓	↓		↓	↓
coef	2	1	1	10	3	1
exp	1000	0	4	3	2	0
	0	1	2	3	4	5
						6

The above figure shows how these polynomials are stored in the array terms. The index of the first term of **A** and **B** is given by startA and startB, while finishA and finishB give the index of the last term of **A** and **B**.

- The index of the next free location in the array is given by avail.
- For above example, startA=0, finishA=1, startB=2, finishB=5, & avail=6.



```
#include<stdio.h>
```

```
typedef struct
```

```
{
```

```
    int cf; //used to hold coefficient
```

```
    int px; //used to hold power of x
```

```
}poly;
```

```
//function to read a polynomial with n terms
```

```
void read_poly(poly p[], int n)
```

```
{
```

```
    int i,cf,px;
```

```
    for(i=0; i<n; i++)
```

```
    {
```

```
        printf("enter Coefficient and exponent:");
```

```
        scanf("%d%d", &p[i].cf, &p[i].px);
```

```
    }
```

```
}
```

```
{
```

```
    int i;
```

```
    for(i=0; i<n; i++)
```

```
    {
```

```
        if(p[i].cf < 0)
```

```
            printf("%d",p[i].cf);
```

```
        else
```

```
            printf("+%d",p[i].cf);
```

```
        if(p[i].px != 0)
```

```
            printf("x^%d",p[i].px);
```

```
    }
```

```
    printf("\n");
```

```
}
```

```
void main()
```

```
{
```

```
    int n;
```

```
    poly p[10];
```

```
    printf("enter number of terms:\n");
```

```
    scanf("%d", &n);
```

```
    read_poly(p, n);
```

```
    print_poly(p,n);
```

```
}
```

```
#include<stdio.h>
typedef struct
{
    int cf; //used to hold coefficient
    int px; //used to hold power of x
}poly;
```

```
void main()
{
    int m, n, k;
    poly p1[20], p2[20], p3[40];

    printf("enter number of terms in polynomial 1:\n");
    scanf("%d", &m);
    read_poly(p1, m); //function call to read a polynomial with n terms

    printf("enter number of terms in polynomial 2:\n");
    scanf("%d", &n);
    read_poly(p2, n); //function call to read a polynomial with n terms

    printf("Poly 1: \n");
    Print_poly(p1,m); //function call to display a polynomial with n terms

    printf("poly 2: \n");
    Print_poly(p2,n); //function call to display a polynomial with n terms

    printf("\n*****\n");
    k = add_poly(p1, m, p2, n, p3); //Function call to add 2 polynomials
    printf("polynomial 3: ");
    print_poly(p3, k); //function call to display a polynomial with n terms
}
```

//function to read a polynomial with n terms

```
void read_poly(poly p[], int n)
```

```
{
```

```
    int i,cf,px;
```

```
    for(i=0; i<n; i++)
```

```
    {
```

```
        printf("enter Coefficient and exponent:")for(i=0; i<n; i++)
```

```
        scanf("%d%d", &p[i].cf, &p[i].px);
```

```
    }
```

```
}
```

//function to display a polynomial with n terms

```
void print_poly(poly p[], int n)
```

```
{
```

```
    int i;
```

```
    for(i=0; i<n; i++)
```

```
    {
```

```
        if(p[i].cf < 0)
```

```
            printf("%d",p[i].cf);
```

```
        else
```

```
            printf("+%d",p[i].cf);
```

```
        if(p[i].px != 0)
```

```
            printf("x^%d",p[i].px);
```

```
    }
```

```
    printf("\n");
```

```
}
```

//Function to search for term of poly 1 in poly2

```
int search(int px1, poly p2[], int n)
{
    int j, px2;
    for(j=0; j<n; j++)
    {
        px2 = p2[j].px;
        if(px1 == px2)
            return j;
    }
    return -1;
}
```

//Function to add 2 polynomials

```
int add_poly(poly p1[], int m, poly p2[], int n, poly p3[])
{
```

```
    int i, k, cf1, px1, pos, sum;
```

```
    k=0;
```

```
    for(i=0; i<m; i++)
```

```
    {
```

```
        cf1 = p1[i].cf;
```

```
        px1 = p1[i].px;
```

```
        pos = search(px1, p2, n); //function call to search for term of poly 1 in poly 2
```

```
        if(pos>0)
```

```
        {
```

```
            sum = cf1 + p2[pos].cf;
```

```
            p3[k].cf = sum;
```

```
            p2[pos].cf = -999;
```

```
        }
```

```
        else
```

```
            p3[k].cf = cf1;
```

```
            p3[k].px = px1;
```

```
            k++;
```

```
        }
```

```
        k = copy_poly(p3, k, p2, n); //function call to copy remaining terms of poly 2 into poly 3
```

```
        return k;
```

```
    }
```


//Function to copy remaining terms of poly 2 into poly 3

```
int copy_poly(poly p3[], int k, poly p2[], int n)
{
    int j;
    for(j=0; j<n; j++)
    {
        if(p2[j].cf != -999)
        {
            p3[k].cf = p2[j].cf;
            p3[k].px = p2[j].px;
            k++;
        }
    }
    return k;
}
```

What is Sparse Matrix?

A matrix which contains many zero entries or very few non-zero entries is called as **Sparse matrix**. In the figure B contains only 8 of 36 elements are nonzero and that is sparse.

	col0	col1	col2
row 0	-27	3	4
row 1	6	82	-2
row 2	109	-64	11
row 3	12	8	9
row 4	48	27	47

Figure A

	col0	col1	col2	col3	col4	col 5
row0	15	0	0	22	0	-15
row1	0	11	3	0	0	0
row2	0	0	0	-6	0	0
row3	0	0	0	0	0	0
row4	91	0	0	0	0	0
row5	0	0	28	0	0	0

Figure B

A sparse matrix can be represented in 1-Dimension, 2- Dimension and 3- Dimensional array. When a sparse matrix is represented as a two-dimensional array as shown in Figure B, more space is wasted.

- An element within a matrix can characterize by using the triple **<row, col, val>** This means that, an array of triples is used to represent a sparse matrix.
- Organize the triples so that the row indices are in ascending order.
- The operations should terminate, so we must know the number of rows and columns, and the number of nonzero elements in the matrix.

```
#define MAX_TERMS 100 /* maximum number of terms */  
typedef struct  
{  
    int col;  
    int row;  
    int value;  
} TERM;
```

```
//1- dimensional array representing array of triples<row,col,val>  
TERM a[MAX_TERMS];
```

The below figure shows the representation of matrix in the array “a” a[0].row contains the number of rows, a[0].col contains the number of columns and a[0].value contains the total number of nonzero entries.

	col0	col1	col2	col3	col4	col5
row0	15	0	0	22	0	-15
row1	0	11	3	0	0	0
row2	0	0	0	-6	0	0
row3	0	0	0	0	0	0
row4	91	0	0	0	0	0
row5	0	0	28	0	0	0

Figure B

	Row	Col	Val	
a[0]	6	6	8	→ 6X6 is the size and 8 non zero values in given matrix
[1]	0	0	15	
[2]	0	3	22	→ Row 0
[3]	0	5	-15	
[4]	1	1	11	→ Row 1
[5]	1	2	3	
[6]	2	3	-6	→ Row 2
[7]	4	0	91	→ Row 4
[8]	5	2	28	→ Row 5

Fig (a): Sparse matrix stored as triple

```
void read_sparse_matrix(TERM a[], int m, int n)
{
    int i,j,k,item;
    a[0].row=m, a[0].col=n, k=1;
    for(i=0; i<m; i++)
    {
        for(j=0; j<n; j++)
        {
            scanf("%d",&item);
            if(item==0)
                continue;
            a[k].row=i, a[k].col=j, a[k].val=item;
            k++;
        }
    }
    a[0].val=k-1;
}
```

	col0	col1	col2	col3	col4	col 5
row0	15	0	0	22	0	-15
row1	0	11	3	0	0	0
row2	0	0	0	-6	0	0
row3	0	0	0	0	0	0
row4	91	0	0	0	0	0
row5	0	0	28	0	0	0

Figure B

	Row	Col	Val	
a[0]	6	6	8	→ 6X6 is the size and 8 non zero values in given matrix
[1]	0	0	15	
[2]	0	3	22	→ Row 0
[3]	0	5	-15	
[4]	1	1	11	→ Row 1
[5]	1	2	3	
[6]	2	3	-6	→ Row 2
[7]	4	0	91	→ Row 4
[8]	5	2	28	→ Row 5

Fig (a): Sparse matrix stored as triple

	col0	col1	col2	col3	col4	col5
row0	15	0	0	22	0	-15
row1	0	11	3	0	0	0
row2	0	0	0	-6	0	0
row3	0	0	0	0	0	0
row4	91	0	0	0	0	0
row5	0	0	28	0	0	0

Figure B

Row	Col	Val
a[0]	6	6
[1]	0	0
[2]	0	3
[3]	0	5
[4]	1	1
[5]	1	2
[6]	2	3
[7]	4	0
[8]	5	2

Fig (a): Sparse matrix stored as triple

	Row	Col	Val
b[0]	6	6	8
[1]	0	0	15
[2]	0	4	91
[3]	1	1	11
[4]	2	1	3
[5]	2	5	28
[6]	3	0	22
[7]	3	2	-6
[8]	5	0	-15

6X6 is the size and 8 non zero values in given matrix

Col 0

Col 1

Col 2

Col 3

Col 5

Fig (b): Transpose matrix stored as triple

```
void transpose(TERM a[], TERM b[])
```

```
{
```

```
    int i,j,k;
```

```
    b[0].row=a[0].col;
```

```
    b[0].col=a[0].row;
```

```
    b[0].val=a[0].val;
```

```
    k=1;
```

```
    for(i=0; i<a[0].col; i++)
```

```
    {
```

```
        for(j=1; j<a[0].val; j++)
```

```
        {
```

```
            if(a[j].col==i)
```

```
            {
```

```
                b[k].row=a[j].col;
```

```
                b[k].col=a[j].row;
```

```
                b[k].val=a[j].val;
```

```
                k++;
```

```
            }
```

```
        }
```

```
    }
```

```
}
```

	Row	Col	Val
a[0]	6	6	8
[1]	0	0	15
[2]	0	3	22
[3]	0	5	-15
[4]	1	1	11
[5]	1	2	3
[6]	2	3	-6
[7]	4	0	91
[8]	5	2	28

Fig (a): Sparse matrix stored as triple

	Row	Col	Val
b[0]	6	6	8
[1]	0	0	15
[2]	0	4	91
[3]	1	1	11
[4]	2	1	3
[5]	2	5	28
[6]	3	0	22
[7]	3	2	-6
[8]	5	0	-15

Fig (b): Transpose matrix stored as triple

Character array - Strings

Array which has character in it is called as **String**

Strings end with special character called null character(`\0`).

Declaration:

```
char a[8];
```

	0	1	2	3	4	5	6	7
a								

Initialization:

```
char a[8] = {'H','e','l','l','o','\0'};
```

	0	1	2	3	4	5	6	7
a	H	e	l	l	o	\0		

Or

```
char a[]="HelloHi";
```

	0	1	2	3	4	5	6	7
a	H	e	l	l	o	H	i	\0

String in C

```
char str[] = "Geeks"
```

index	0	1	2	3	4
str	G	e	e	k	s
Address					

GG

String: A finite sequence S of zero or more Characters is called string.

Length: The number of characters in a string is called length of string.

Empty or Null String: The string with zero characters.

Concatenation: Let S_1 and S_2 be the strings. The string consisting of the characters of S_1 followed by the character S_2 is called Concatenation of S_1 and S_2 .

Ex: 'THE' // 'END' = 'THEEND'

'THE' // ' ' // 'END' = 'THE END'

Substring: A string Y is called substring of a string S if there exist string X and Z such that $S = X // Y // Z$

If X is an empty string, then Y is called an Initial substring of S , and Z is an empty string then Y is called a terminal substring of S .

Ex: 'BE OR NOT' is a substring of 'TO BE OR NOT TO BE'

'THE' is an initial substring of 'THE END'

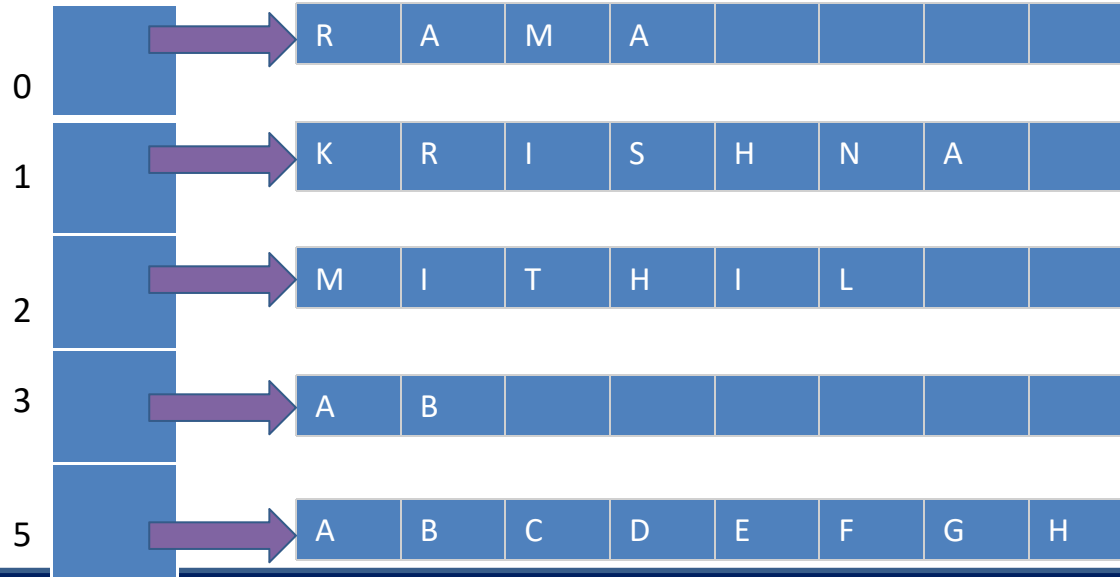
STORING STRINGS - How strings are stored in memory?

Strings are stored in three types of structures

1. Fixed length storage structures
2. Variable length structures
3. Linked storage structures

1. Fixed length storage structures

In this storage structure, each line of text to be manipulated is viewed as a record where all records have same length.



Disadvantages:

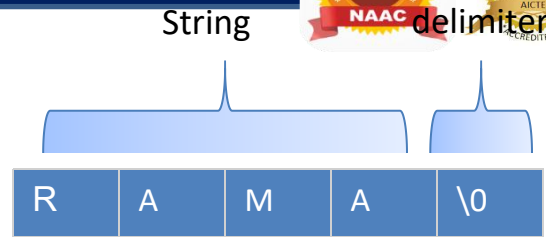
1. Time wasted in reading entire record if more spaces are present
2. Certain records may require more space than available to store a string
3. If the length reserved for string is too small, it is not possible to store larger data
4. If the length reserved for string is too large, too much memory is wasted
5. Once the string is defined, the length of the string can't be changed

2. Variable length structures

->The storage structure for a string can expand or shrink to accommodate any size of data.

->But there should be a mechanism to indicate the end of the data

->In C language strings end with a special character called NULL (denoted by \0)



5 bytes



String

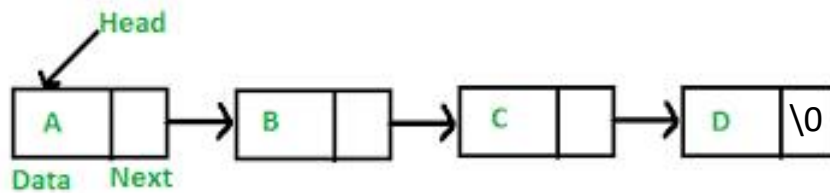
delimiter

8 bytes

```
char a[]="RAMA";
```

```
char a[]="KRISHNA";
```

3. Linked storage structures





String Operations:



Substring

Indexing

Concatenation

Length

Substring

Accessing a substring from a given string requires three pieces of information:

- (1) The name of the string or the string itself
- (2) The position of the first character of the substring in the given string
- (3) The length of the substring or the position of the last character of the substring.

Syntax: **SUBSTRING** (string, initial, length)

The syntax denote the substring of a string **S** beginning in a position **K** and having a length **L**.

Ex: **SUBSTRING** ('TO BE OR NOT TO BE', 4, 7) = 'BE OR N'

SUBSTRING ('THE END', 4, 4) = 'END'

Indexing

Indexing also called pattern matching, refers to finding the position where a string pattern **P** first appears in a given string text **T**. This operation is called **INDEX**

Syntax: **INDEX** (text, pattern)

If the pattern **P** does not appears in the text **T**, then **INDEX** is assigned the value 0.



Let S1 and S2 be string. The concatenation of S1 and S2 which is denoted by $S1 \parallel S2$, is the string consisting of the characters of S1 followed by the character of S2.

Ex:

(a) Suppose S1 = 'MARK' and S2= 'TWIN' then

$S1 \parallel S2 = \text{'MARKTWIN'}$

Concatenation is performed in C language using strcat function as shown below

strcat (S1, S2);

Concatenates string S1 and S2 and stores the result in S1

strcat () function is part of the string.h header file; hence it must be included at the time of pre- processing

Length

The number of characters in a string is called its length.

Syntax: **LENGTH** (string)

Ex: **LENGTH** ('computer') = 8

Printing and Reading Strings

Formatted - printf (for output)
- scanf (for input)

Un formatted - puts (for output)
- gets (for input)

Ex. for reading string using
formatted input function:

```
char c[20];  
scanf("%s", c);
```

```
#include<stdio.h>  
  
Void main()  
{  
    char name[20];  
    Printf("enter your name:");  
    Scanf("%s", name);  
    Printf("your name is %s:", name);  
}
```

O/p:
enter your name: Sachin Tendulkar
your name is: Sachin

```
#include<stdio.h>
```

```
Void main()
```

```
{
```

```
    char name[20];
```

```
    printf("enter your name:");
```

```
    gets(name);
```

```
    printf("your name is:");
```

```
    puts(name);
```

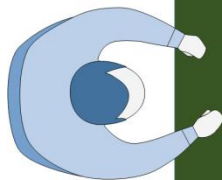
```
}
```

O/p:

enter your name: Sachin Tendulkar

your name is: Sachin Tendulakar

Function	Description
<code>char *strcat(char *dest, char *src)</code>	concatenate <i>dest</i> and <i>src</i> strings; return result in <i>dest</i>
<code>char *strncat(char *dest, char *src, int n)</code>	concatenate <i>dest</i> and <i>n</i> characters from <i>src</i> ; return result in <i>dest</i>
<code>char *strcmp(char *str1, char *str2)</code>	compare two strings; return < 0 if <i>str1</i> < <i>str2</i> ; 0 if <i>str1</i> = <i>str2</i> ; > 0 if <i>str1</i> > <i>str2</i>
<code>char *strncmp(char *str1, char *str2, int n)</code>	compare first <i>n</i> characters; return < 0 if <i>str1</i> < <i>str2</i> ; 0 if <i>str1</i> = <i>str2</i> ; > 1 if <i>str1</i> > <i>str2</i>
<code>char *strcpy(char *dest, char *src)</code>	copy <i>src</i> into <i>dest</i> ; return <i>dest</i>
<code>char *strncpy(char *dest, char *src, int n)</code>	copy <i>n</i> characters from <i>src</i> string into <i>dest</i> ; return <i>dest</i> ;
<code>size_t strlen(char *s)</code>	return the length of a <i>s</i>
<code>char * strchr(char *s, int c)</code>	return pointer to the first occurrence of <i>c</i> in <i>s</i> ; return <i>NULL</i> if not present
<code>char * strrchr(char *s, int c)</code>	return pointer to last occurrence of <i>c</i> in <i>s</i> ; return <i>NULL</i> if not present
<code>char * strtok(char *s, char *delimiters)</code>	return a token from <i>s</i> ; token is surrounded by <i>delimiters</i>
<code>char * strstr(char *s, char *pat)</code>	return pointer to start of <i>pat</i> in <i>s</i>
<code>size_t strspn(char *s, char *spanset)</code>	scan <i>s</i> for characters in <i>spanset</i> ; return length of span
<code>size_t strcspn(char *s, char *spanset)</code>	scan <i>s</i> for characters not in <i>spanset</i> ; return length of span
<code>char * strpbrk(char *s, char *spanset)</code>	scan <i>s</i> for characters in <i>spanset</i> ; return pointer to first occurrence of a character from <i>spanset</i>



all string handling functions under
<string.h>
 “ **strcat(), strlen(), strcpy() ,.....**”

Design Functions to implement following string functions

- i) strlen()
- ii) strcmp()
- iii) strcat()
- iv) strcpy()
- v) strrev()

char str[6] = "Hello";

index	0	1	2	3	4	5
value	H	e	l	l	o	\0
address	1000	1001	1002	1003	1004	1005

```
#include<stdio.h>
```

```
void main()
```

```
{
```

```
    char str[6]="Hello";
```

```
    int len = my_strlen(str);
```

```
    printf("length of str is %d",len);
```

```
}
```

```
int my_strlen(char str[])
```

```
{
```

```
    int i=0;
```

```
    while(str[i] != '\0')
```

```
    {
```

```
        i++;
```

```
    }
```

```
    return i;
```

```
}
```

```
#include<stdio.h>
```

```
#include<string.h>
```

```
void main()
```

```
{
```

```
    char str[6]="Hello";
```

```
    int len = strlen(str);
```

```
    printf("length of str is %d",len);
```

```
}
```

h e l l o \0
Index 0 1 2 3 4 5 6

```
#include<stdio.h>
void main()
{
    char str1[6]="HELLO";
    char str2[6];
    My_strcpy(str1, str2);
}
```

```
void my_strcpy(char str1[], char str2[])
{
    int i=0;
    while(str1[i] != '\0')
    {
        str2[i]=str1[i];
        i++;
    }
    str2[i]='\0';
}
```

strcpy(str1, str2)

str2 =

Memory
h e l l o \0
Index 0 1 2 3 4 5 6

```
#include<stdio.h>
#include<string.h>
void main()
{
    char str1[6]="HELLO";
    char str2[6];
    strcpy(str1,str2);
    printf("string 2 is %s",str2);
}
```

```
#include<stdio.h>
```

```
void main()
```

```
{
```

```
    char str1[6]="HELLO";
```

```
    char str2[6]="WORLD";
```

```
    My_strcat(str1, str2);
```

```
}
```

```
void my_strcat(char str1[], char str2[])
```

```
{
```

```
    int i,j;
```

```
    i=0,j=0;
```

```
    while(str1[i] != '\0')
```

```
    {
```

```
        i++;
```

```
    }
```

```
    while(str2[j]!='\0')
```

```
    {
```

```
        str1[i++]=str2[j++];
```

```
    }
```

```
    str1[i++] = '\0';
```

```
}
```

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
str1	t	r	y	t	o	\0									

str2	p	r	o	g	r	a	m	\0			
------	---	---	---	---	---	---	---	----	--	--	--

```
strcat( str1, str2 );
```

str1	t	r	y	t	o	p	r	o	g	r	a	m	\0		
------	---	---	---	---	---	---	---	---	---	---	---	---	----	--	--



Null character (\0) of **str1** is replaced by the first character of **str2**

```
#include<stdio.h>
```

```
#include<string.h>
```

```
void main()
```

```
{
```

```
    char str1[6]="HELLO";
```

```
    char str2[6]="WORLD";
```

```
    strcat(str1,str2);
```

```
    printf("str1 is %s",str1);
```

```
}
```


If 2 strings are equal, the function returns 0

If string 1 is greater than string 2, a positive value is returned.

If String 1 is less than string 2, a negative value is returned.

```
#include<stdio.h>
void main()
{
    char str1[6]="Hello";
    char str2[6]="Hello";
    int res = my_strcmp(str1, str2);
    if(res==0) { printf("strings are equal\n"); }
    else if(res < 0) { printf("string 1 is smaller than string 2"); }
    else { printf("string 1 is greater than string 2"); }
}

Int my_strcmp(char str1[], char str2[])
{
    int i;
    i=0;
    while(str1[i] == str2[i])
    {
        if(str1[i] == '\0')
            break;
        i++;
    }
    return str1[i] - str2[i];
}
```

str1 =



strcmp()

str2 =



```
#include<stdio.h>
#include<string.h>
void main()
{
    char str1[6]="Hello";
    char str2[6];
    my_strrev(str1, str2);
}
void my_strrev(char str1[], char str2[])
{
    int i,n;
    n = strlen(str1)
    for(i=0; i<n; i++)
    {
        str2[n-1-i] = str1[i];
    }
    str2[n] = '\0';
}
```



Reverse a string in C



->Pattern matching is the problem of deciding whether or not a given string pattern P appears in a string text T . The length of P does not exceed the length of T .

Brute Force Algorithm

The first pattern matching algorithm is one in which comparison is done by a given pattern P with each of the substrings of T , moving from left to right, until a match is found.

$WK = \text{SUBSTRING}(T, K, \text{LENGTH}(P))$

- Where, WK denote the substring of T having the same length as P and beginning with the K th character of T .
- First compare P , character by character, with the first substring, $W1$. If all the characters are the same, then $P = W1$ and so P appears in T and $\text{INDEX}(T, P) = 1$.
- Suppose it is found that some character of P is not the same as the corresponding character of $W1$. Then $P \neq W1$
- Immediately move on to the next substring, $W2$ That is, compare P with $W2$. If $P \neq W2$ then compare P with $W3$ and so on.
- The process stops, When P is matched with some substring WK and so P appears in T and $\text{INDEX}(T, P) = K$ or When all the WK 'S with no match and hence P does not appear in T .
- The maximum value MAX of the subscript K is equal to $\text{LENGTH}(T) - \text{LENGTH}(P) + 1$.

Algorithm: (Pattern Matching_Brute Force)

P and T are strings with lengths R and S, and are stored as arrays with one character per element. This algorithm finds the INDEX of P in T.

1. [Initialize.] Set $K := 1$ and $MAX := S - R + 1$
2. Repeat Steps 3 to 5 while $K \leq MAX$
3. Repeat for $L = 1$ to R : [Tests each character of P]
 If $P[L] \neq T[K + L - 1]$, then: Go to Step 5
 [End of inner loop.]
4. [Success.] Set $INDEX = K$, and Exit
5. Set $K := K + 1$
 [End of Step 2 outer loop]
6. [Failure.] Set $INDEX = 0$
7. Exit

Algm PatternMatching_KMP(s, p) return int

```
{
    k=1, s1=q0, n=length(s)
    While(k<=n && sk!=p)
    {
        Read tk
        sk+1 = F(sk, tk)
        k=k+1
    }
    If(k>n)
    {
        index=0
    }
    else
    {
        Index=k-length(p)
    }
    return index
}
```

1 2 3 4 5 6 7 8 9 10 11

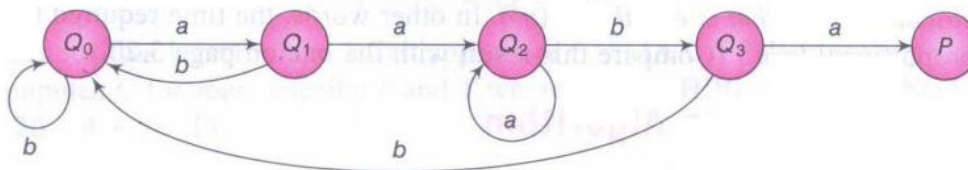
String s: a a a a a a a a a b

Pattern p: a a a b

	a	b	x
Q ₀	Q ₁	Q ₀	Q ₀
Q ₁	Q ₂	Q ₀	Q ₀
Q ₂	Q ₂	Q ₃	Q ₀
Q ₃	P	Q ₀	Q ₀

(a) Pattern matching table

Pattern p: a a b a



b Pattern matching graph

Stacks and Queues

Stacks: Definition, Stack Operations, Array Representation of Stacks, Stacks using Dynamic Arrays, Stack Applications: Polish notation, Infix to postfix conversion, evaluation of postfix Expression

Recursion - Factorial, GCD, Fibonacci Sequence, Tower of Hanoi, Ackerman's Function.

Queues: Definition, Array Representation, Queue Operations, Circular Queues, Circular queues using Dynamic arrays, Dequeues, Priority Queues, A Mazing Problem. Multiple Stacks and Queues. Programming Examples.

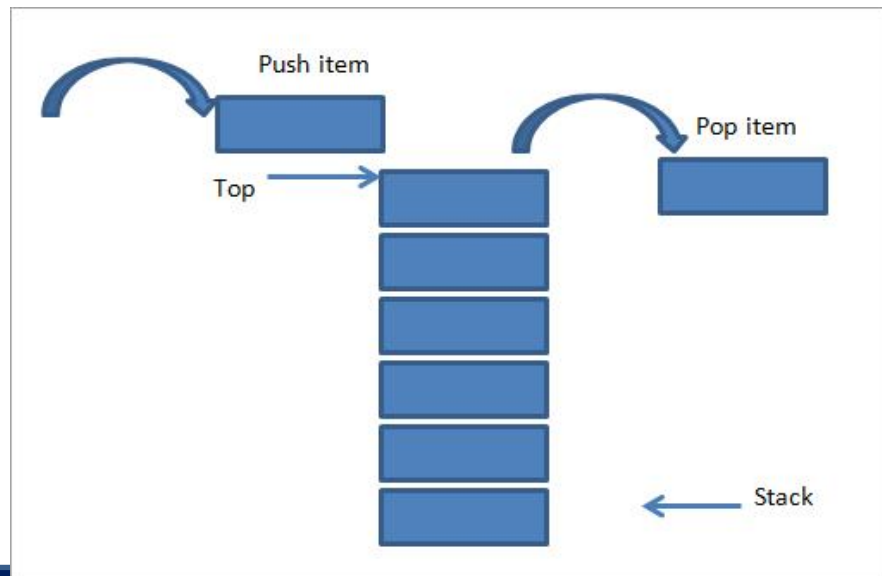
-> Stack is a linear data structure which follows a particular order in which the operations are performed.

->The order may be LIFO(Last In First Out) or FILO(First In Last Out).

-> A stack can be implemented by means of Array, Structure, Pointer, and Linked List.

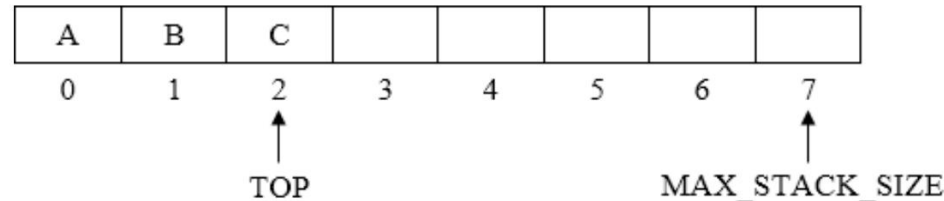
-> Here, we are going to implement stack using arrays, which makes it a fixed size stack implementation.

->At any given time, we can only access the top element of a stack.



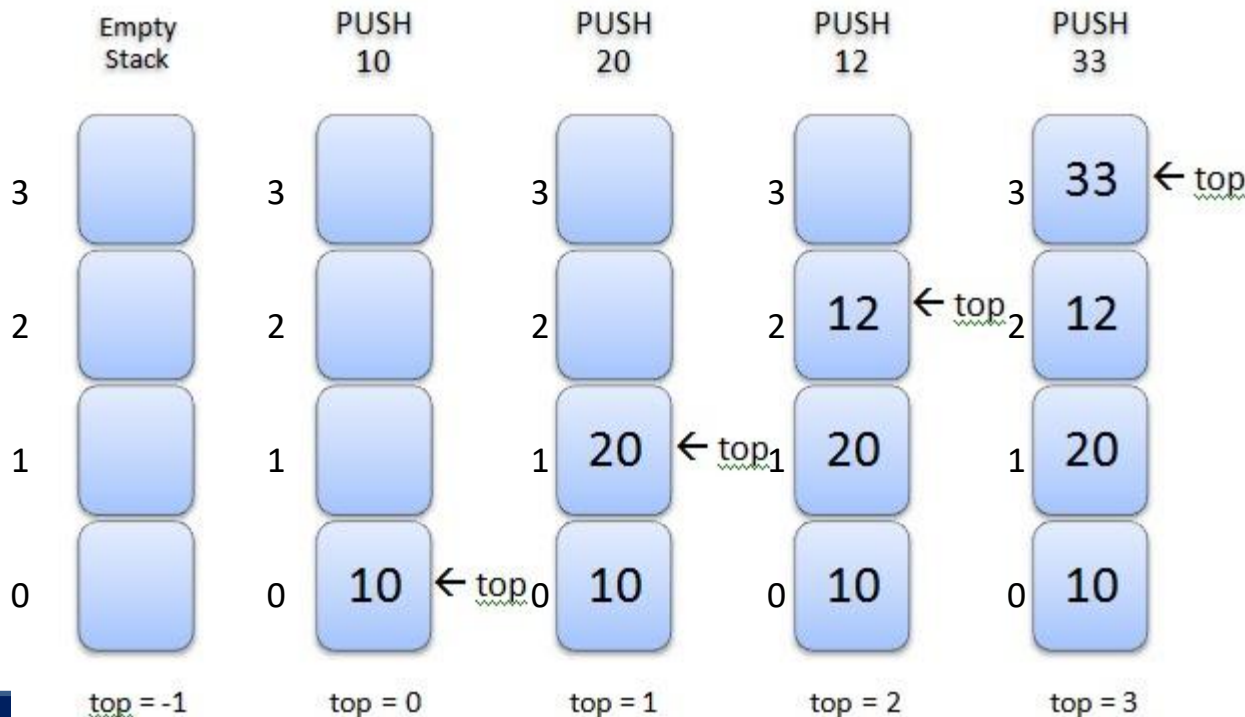
- Stacks may be represented in the computer in various ways such as one-way linked list (Singly linked list) or linear array.
- Stacks are maintained by the two variables such as **TOP** and **MAX_STACK_SIZE**.
- TOP** which contains the location of the top element in the stack. If **TOP = -1**, then it indicates stack is empty.
- MAX_STACK_SIZE** which gives maximum number of elements that can be stored in stack.

Stack can be represented using linear array as shown below



push() - Pushing (storing) an element on the stack

- > Check for overflow condition i.e $top = Max_Size - 1$
- > Increment top by 1
- > Push an element



```
#define Max_Size 4
void push()
{
    if (top >= Max_Size-1)
        Stack overflow
    Else
        top++;
        stack[top] = item;
}
```



Function to push an integer item (using global variables)

```
void push()
{
    If(top == Max_Size - 1)
    {
        printf("Stack Overflow");
        exit(0);
    }
    top++;
    s[top] = item;
}
```



Function to push an integer item (by passing parameter)

```
void push(int item, int top, int s[])
{
    If(top == Max_Size - 1)
    {
        Printf("Stack Overflow");
        Return;
    }
    top++;
    s[top] = item;
}
```

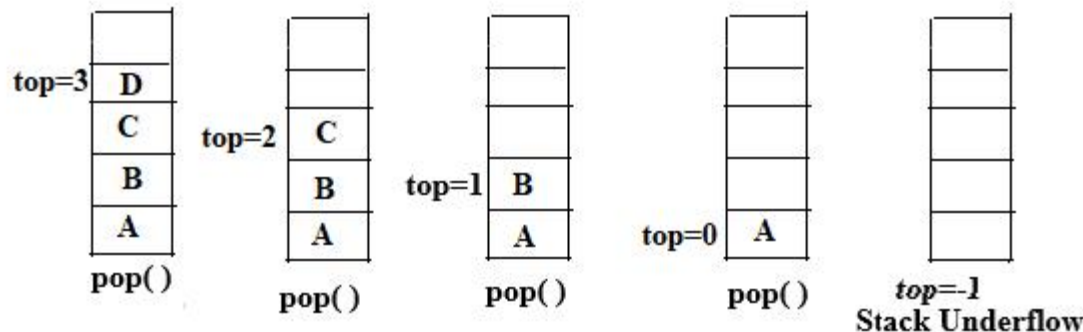
Deleting an element from the stack is called **pop** operation. The element is deleted only from the top of the stack and only one element is deleted at a time.

Removing an element from the stack.

Check underflow condition i.e $top = -1$

Item = $s[top]$

Decrement top by 1



Function to pop an integer item (using global variables)

```
int pop()
{
    int item_deleted;

    If(top== -1)
        Return 0;

    item_deleted=s[top--];
    Return item_deleted;
}
```

Function to pop an integer item (by passing parameter)

```
int pop(int top, int s[])
{
    int item_deleted;

    If(top== -1)
        Return 0;

    item_deleted=s[(top)--];
    Return item_deleted;
}
```

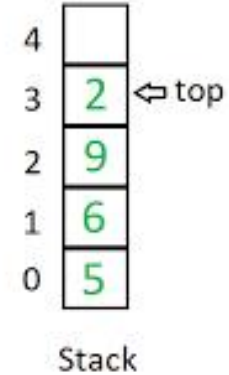
- >Display the elements of stack
- >Check for underflow condition
- >Display using for loop

Display Stack content using global variables

```
void display()
{
    Int i;
    If(top== -1)
    {
        Printf("stack is empty\n");
        Return;
    }
    Printf("Contents of the stack are:\n");
    For(i=0; i<=top; i++)
    {
        Printf("%d\n",s[i]);
    }
}
```

Display Stack content by pass by parameter

```
void display(int top, int s[])
{
    Int i;
    If(top== -1)
    {
        Printf("stack is empty\n");
        Return;
    }
    Printf("Contents of the stack are:\n");
    For(i=0; i<=top; i++)
    {
        Printf("%d\n",s[i]);
    }
}
```



- Stacks can be used for expression evaluation.
- Stacks can be used to check parenthesis matching in an expression
- Stacks can be used for Conversion from one form of expression to another.
- Stacks can be used for Memory Management

Expression can be represented in in different format such as

- Prefix Expression or Polish notation
- Infix Expression
- Postfix Expression or Reverse Polish notation

Infix Expression: In this expression, the binary operator is placed in-between the operand.
The expression can be parenthesized or un- parenthesized.

Example: $A + B$

Here, **A & B** are operands and **+** is operator

Prefix or Polish Expression: In this expression, the operator appears before its operand.

Example: $+ A B$

Here, **A & B** are operands and **+** is operator

Postfix or Reverse Polish Expression: In this expression, the operator appears after its operand.

Example: $A B +$

Here, **A & B** are operands and **+** is operator

Step 1: If operand - push

Step2: If operator -

- * Pop the top of the stack and make it operand 2**
- * Pop the next top of the stack and make operand 1**
- * Perform operation**
- * Push the result**

Infix -> $4 + 2 * 3$

postfix -> $4\ 2\ 3\ *\ +$

Infix -> $(8 + 5) * (6 / 3)$

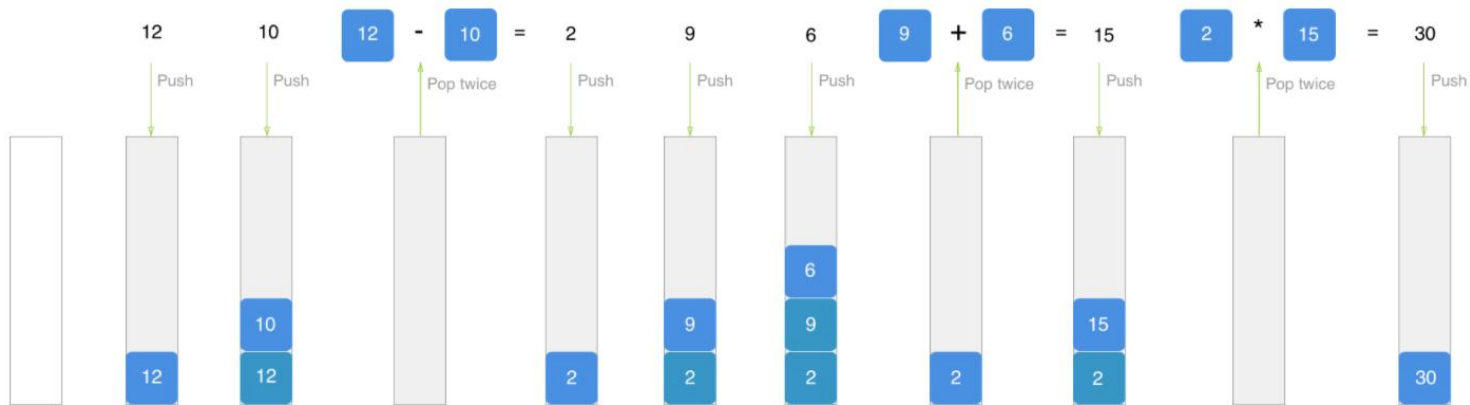
postfix -> $8\ 5\ +\ 6\ 3\ /\ *$

Infix -> $4\ \$\ 2\ *3 - 3 + 8 / 4 / (1 + 1)$

postfix -> $4\ 2\ \$\ 3\ * 3 - 8\ 4 / 1\ 1\ + / +$

Postfix Evaluation Example

Example : 12 10 - 9 6 + *



Step 1: If operand - send it to postfix expression

Step2: If operator -

Check the Priority of current operator (PCO) VS Priority of top of stack(POTS)

If(PCO > POTS) then PUSH

If(PCO = POTS) then POP

If(PCO < POTS) then POP

Step3: Parenthesis

If (PUSH

If) PUSH














Permitted to push any symbol above the brackets

POP all the symbols between (and)

Priorities:

1. \$, ^
2. *, /
3. +, -

Example : $((4 + (8 * 2)) - 10)$

S.No	Scanned element	Input Expression	Operator Stack	Output Expression	Description
1	($(4 + (8 * 2)) - 10)$			Push '(' to stack
2	($4 + (8 * 2)) - 10)$			Push '(' to stack
3	4	$+(8 * 2)) - 10)$		4	Output value
4	+	$(8 * 2)) - 10)$		4	Push '+' to stack
5	($8 * 2)) - 10)$		4	Push '(' to stack
6	8	$* 2)) - 10)$		4 8	Output value
7	*	$2)) - 10)$		4 8	Push '*' to stack
8	2	$) - 10)$		4 8 2	Output value
9)	$) - 10)$		4 8 2 *	Pop till '(' is found
10)	$- 10)$		4 8 2 * +	Pop till '(' is found
11	-	10)		4 8 2 * +	Push '-' to stack
12	10)		4 8 2 * + 10	Output value
13)			4 8 2 * + 10 -	Pop till '(' is found is_empty()



#define SIZE 50

```
char s[SIZE];
int top=-1;
void push(char elem)
```

```
{
    s[++top]=elem;
}
```

```
char pop()
{
    return s[top--];
}
```

```
int pr(char elem)
{
    switch(elem) {
        case '#':return 0;
        case '(':return 1;
        case '+':
        case '-':return 2;
        case '*':
        case '/':
        case '%':return 3;
        case '^':return 4;
    }
```

```
}
```

```
void main() {
```

```
char infix[50],postfix[50],ch,elem;
int i=0,k=0;
printf("enter the infix expression\n");
push('#');
while((ch=infix[i++])!='\0')
{
    if(ch=='(')
        push(ch);
    else if(isalnum(ch))
        postfix[k++]=ch;
    else if(ch=='')
    {
        while(s[top]!='(')
            postfix[k++]=pop();
        elem=pop();
    }
    else
    {
        while(pr(s[top])>=pr(ch))
            postfix[k++]=pop();
        push(ch);
    }
}
while(s[top]!='#')
    postfix[k++]=pop();
postfix[k]='\0';
printf("infix expression is %s\n postfix expression is %s\n",infix,postfix);
```

```
}
```



Enumeration (or enum) is a user defined data type in C. It is mainly used to assign names to integral constants, the names make a program easy to read and maintain.

```
typedef enum { lparen, rparen, plus,  
minus, times, divide, mod, eos,  
operand } precedence;
```

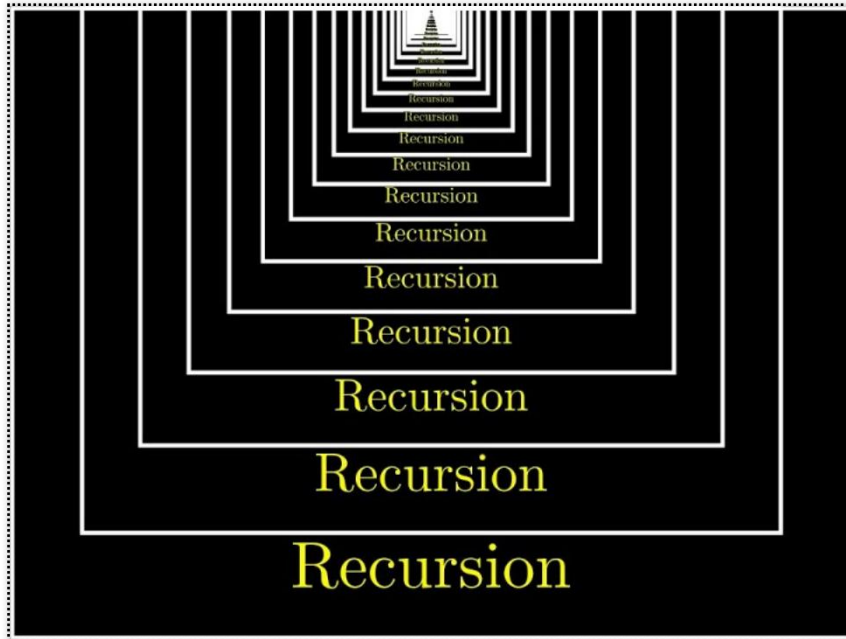
```
precedence getToken(char *symbol, int *n)  
{  
    *symbol = expr[(*n)++];  
    switch (*symbol)  
    {  
        case '(' : return lparen;  
        case ')' : return rparen;  
        case '+' : return plus;  
        case '-' : return minus;  
        case '/' : return divide;  
        case '*' : return times;  
        case '%' : return mod;  
        case ' ' : return eos;  
        default: return operand;  
    }  
}
```



```
int eval(void)
{
    precedence token;
    char symbol;
    int opl,op2, n=0;
    int top= -1;
    token = getToken(&symbol, &n);
    while(token!= eos)
    {
        if (token == operand)
            push(); /* stack insert */
        else
        {
            op2 = pop(); /* stack delete */
            opl = pop();
            switch(token)
            {
                case plus: push(opl+op2);      break;
                case minus: push(opl-op2);      break;
                case times: push(opl*op2);      break;
                case divide: push(opl/op2);     break;
                case mod: push(opl%op2);        break;
            }
        }
        token = getToken(&symbol, &n);
    }
    return pop(); /* return result */
}
```

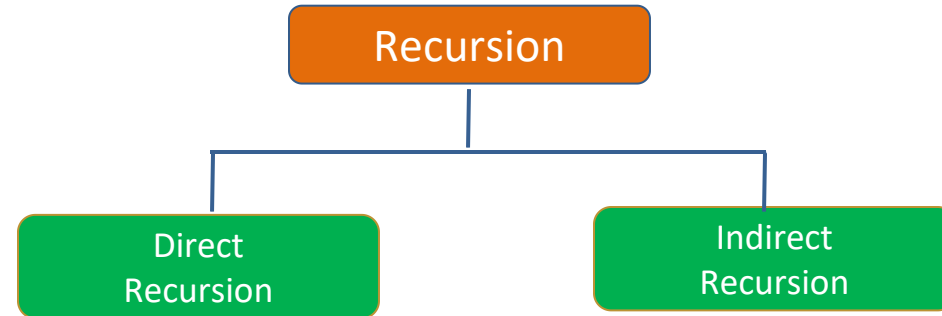
```
precedence token;
int n = 0, top = 0; /* place eos on stack */
stack[0] = eos;
for (token = getToken(&symbol, &n); token != eos; token = getToken(&symbol, &n))
{
    if (token == operand)
        printf("%c", symbol);
    else if (token == rparen)
    {
        while (stack[top] != lparen)
            printToken(pop());
        pop();
    }
    else
    {
        while (isp[stack[top]] >= icp[token])
            printToken(pop());
        push(token);
    }
}
while ((token = pop()) != eos)
    printToken(token);
printf("\n");
}
```

Recursion



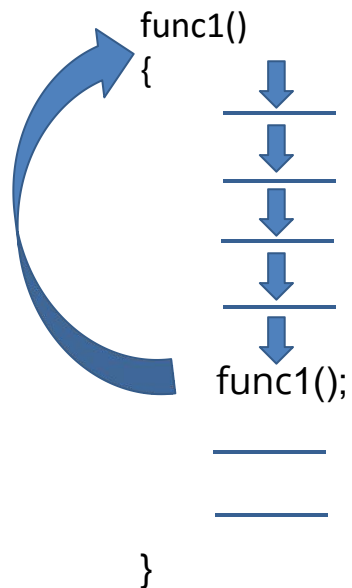
A process of a function calling itself is what is called Recursion

Recursion refers to the process where a function calls itself directly or indirectly

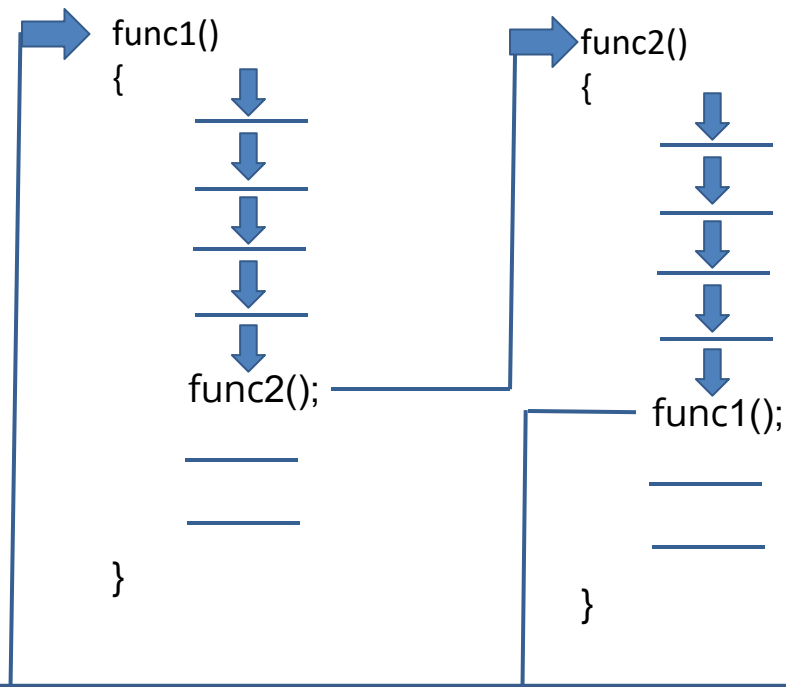


Direct Recursion

Function calls itself directly




Indirect Recursion



Direct Recursion

Example:

```
#include<stdio.h>
void main()
{
    printf("I LOVE MY COUNTRY\n");
    main();
}
```



Output:

I LOVE MY COUNTRY

I LOVE MY COUNTRY

...

...

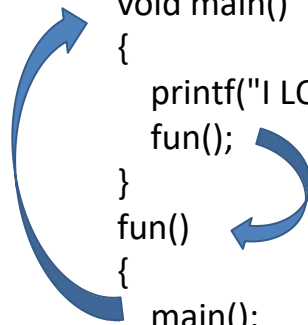
...

(infinte number of times I LOVE MY COUNTRY will printed)

Indirect Recursion

Example:

```
#include<stdio.h>
void fun(void);
void main()
{
    printf("I LOVE MY COUNTRY\n");
    fun();
}
fun()
{
    main();
}
```



Output:

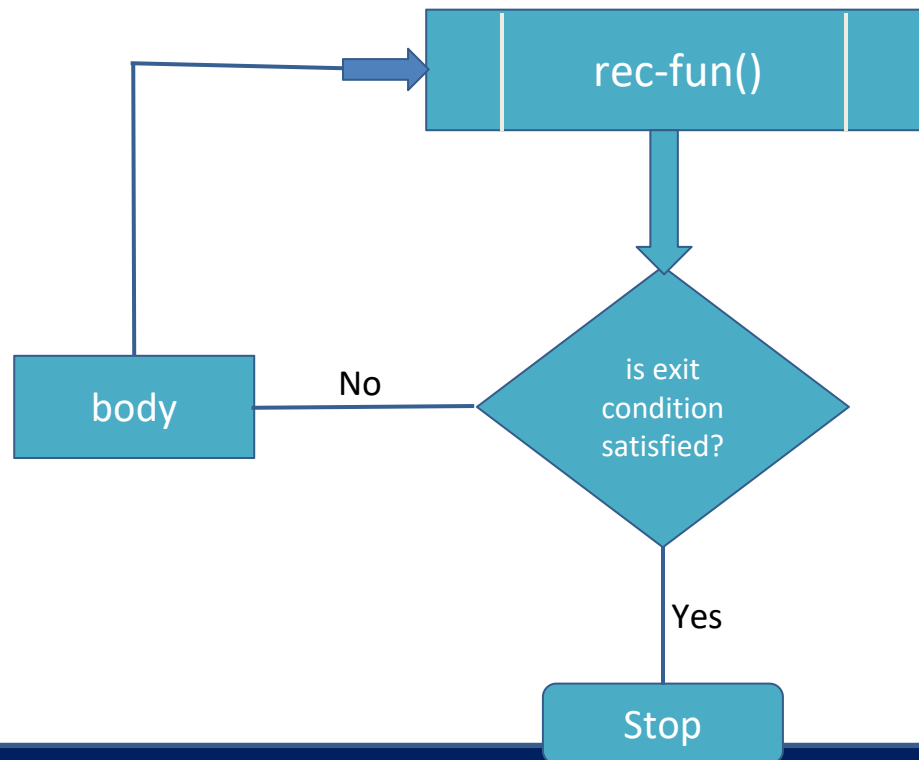
I LOVE MY COUNTRY

I LOVE MY COUNTRY

...

(infinte number of times I LOVE MY COUNTRY will printed)

General format of recursive function:



Factorial of a number $5!=5*4*3*2*1=120$

```
#include<stdio.h>
void main()
{
    fact=1;
    Printf("enter the no\n");
    Scanf("%d",&n);
    For(i=1;i<=n;i++)
    {
        fact=fact*i;
    }
    printf("factorial of a number is %d", fact);
}
```

Write a program to compute the factorial of a given number n using recursion.

$0! = 1$
 $1! = 1 * (1-1)! = 1 * 1 = 1$
 $2! = 2 * (2-1)! = 2 * 1 = 2$
 $3! = 3 * (3-1)! = 3 * 2 = 6$
 $4! = 4 * (4-1)! = 4 * 6 = 24$
 .
 .
 .
 $n! = n * (n-1)!$

$$\text{fact}(n) = \begin{cases} 1 & \text{if } n==0 \\ n * \text{fact}(n-1) & \text{if } n>0 \end{cases}$$

```
#include<stdio.h>
```

```
int fact(int);
```

```
void main()
```

```
{
```

```
    int n,ans;
```

```
    printf("enter the value of n\n");
```

```
    scanf("%d",&n);
```

```
    ans=fact(n);
```

```
    printf("answer is %d",ans);
```

```
}
```

```
int fact(int n)
```

```
{
```

```
    if(n==0)
```

```
    {
```

```
        return 1;
```

```
    }
```

```
    else
```

```
    {
```

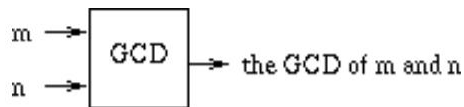
```
        return n*fact(n-1);
```

```
    }
```

```
}
```



The greatest common divisor (GCD) of two integers m and n is the greatest integer that divides both m and n with no remainder.



For $m \geq n \geq 0$, $\text{gcd}(m, n) = \begin{cases} n & \text{If } n \text{ divides } m \text{ with no remainder} \\ \text{gcd}(n, \text{remainder of } \frac{m}{n}) & \text{Otherwise} \end{cases}$

Procedure: GCD (M, N)

1. If $(M \% N) = 0$, then set $\text{GCD} = N$ and RETURN
2. Call GCD (N, $M \% N$)
3. Return

#include<stdio.h>

int gcd(int a, int b)

{

if(b==0)

return a;

elseif(a<b)

return gcd(b,a);

else

return gcd(b, a%b);

}

Void main()

{

Int a,b;

Printf("enter a and b\n");

Scanf("%d%d", &a,&b);

Result=gcd(a,b);

Printf("result is = %d", Result);

}

a series of numbers in which each number (*Fibonacci number*) is the sum of the two preceding numbers.


n	1	2	3	4	5	6	7	8	9	10
fib(n)	0	1	1	2	3	5	8	13	21	34

$$F_0 = 0, \quad F_1 = 1,$$

$$F_n = F_{n-1} + F_{n-2}$$

0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144, ...

Default



$$\begin{aligned}
 0 + 1 &= 1 \\
 1 + 1 &= 2 \\
 1 + 2 &= 3 \\
 2 + 3 &= 5
 \end{aligned}$$

$$\text{fib}(n) = \begin{cases} 0 & \text{if } n=1 \\ 1 & \text{if } n=2 \\ \text{fib}(n-1) + \text{fib}(n-2) & \text{if } n > 2 \end{cases}$$



```
#include<stdio.h>
```

```
int fib(int);
```

```
void main()
```

```
{
```

```
    int n,ans;
```

```
    printf("enter the value of n\n");
```

```
    scanf("%d",&n);
```

```
    ans=fib(n);
```

```
    printf("answer is %d",ans);
```

```
}
```

```
int fib(int n)
```

```
{
```

```
    if(n==1)
```

```
    {
```

```
        return 0;
```

```
    }
```

```
    if(n==2)
```

```
    {
```

```
        return 1;
```

```
    }
```

```
    if(n>2)
```

```
    {
```

```
        return fib(n-1)+fib(n-2);
```

```
    }
```

```
}
```

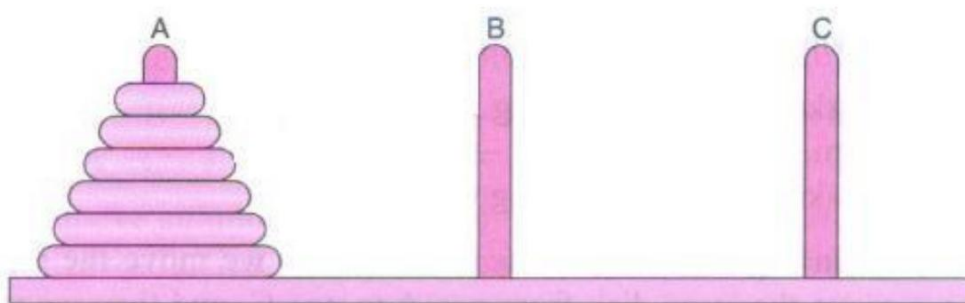


Suppose three pegs, labeled **A**, **B** and **C**, are given, and suppose on peg **A** a finite number n of disks with decreasing size are placed.

The objective of the game is to move the disks from peg **A** to peg **C** using peg **B** as an auxiliary.

The rules of the game are as follows:

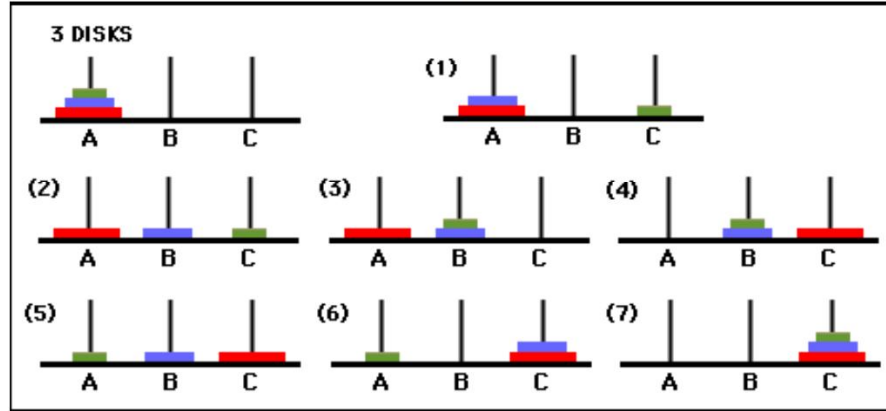
1. Only one disk may be moved at a time. Only the top disk on any peg may be moved to any other peg.
2. At no time can a larger disk be placed on a smaller disk



Initial Setup of Towers of Hanoi with $n = 6$

Example: Towers of Hanoi problem for $n = 3$.

Solution: Observe that it consists of the following seven moves



1. Move top disk from peg A to peg C.
2. Move top disk from peg A to peg B.
3. Move top disk from peg C to peg B.
4. Move top disk from peg A to peg C.
5. Move top disk from peg B to peg A.
6. Move top disk from peg B to peg C.
7. Move top disk from peg A to peg C.

In other words,

$n=3$: $A \rightarrow C$, $A \rightarrow B$, $C \rightarrow B$, $A \rightarrow C$, $B \rightarrow A$, $B \rightarrow C$,
 $A \rightarrow C$

the solution to the Towers of Hanoi problem for $n = 1$ and $n = 2$

$n=1$: $A \rightarrow C$

$n=2$: $A \rightarrow B$, $A \rightarrow C$, $B \rightarrow C$



The Towers of Hanoi problem for $n > 1$ disks may be reduced to the following sub-problems.



- (1) Move the top $n - 1$ disks from peg A to peg B
- (2) Move the top disk from peg A to peg C: $A \rightarrow C$.
- (3) Move the top $n - 1$ disks from peg B to peg C

The general notation

- **TOWER (N, BEG, AUX, END)** to denote a procedure which moves the top n disks from

the initial peg **BEG** to the final peg **END** using the peg **AUX** as an auxiliary.

- When $n = 1$, the solution:

TOWER (1, BEG, AUX, END) consists of the single instruction **BEG \rightarrow END**

- When $n > 1$, the solution may be reduced to the solution of the following three sub problems:

(a) **TOWER (N - 1, BEG, END, AUX)**

(b) **TOWER (1, BEG, AUX, END)** or **BEG \rightarrow END**

(c) **TOWER (N - 1, AUX, BEG, END)**

Procedure: TOWER (N, BEG, AUX, END)

This procedure gives a recursive solution to the Towers of Hanoi problem for N disks.

1. If $N=1$, then:

(a) Write: $BEG \rightarrow END$.

(b) Return.

[End of If structure.]

2. [Move N - 1 disks from peg BEG to peg AUX.]

Call TOWER (N - 1, BEG, END, AUX).

3. Write: $BEG \rightarrow END$.

4. [Move N - 1 disks from peg AUX to peg END.]

Call TOWER (N - 1, AUX, BEG, END).

5. Return.

#include<stdio.h>

void tower(int n,char frompeg,char topeg,char auxpeg);

int n;

void main()

{

printf("Enter the no. of discs: \n");

scanf("%d",&n);

printf("the number of moves in tower of henoi problem\n");

tower(n,'A','C','B');

}

void tower(int n,char frompeg,char topeg,char auxpeg)

{

if(n==1)

{

printf("move disk1 from %C to %C\n ",frompeg,topeg);

return;

}

tower(n-1,frompeg,auxpeg,topeg);

printf("move disk%d from %C to %C\n",n,frompeg,topeg);

tower(n-1,auxpeg,topeg,frompeg);

}

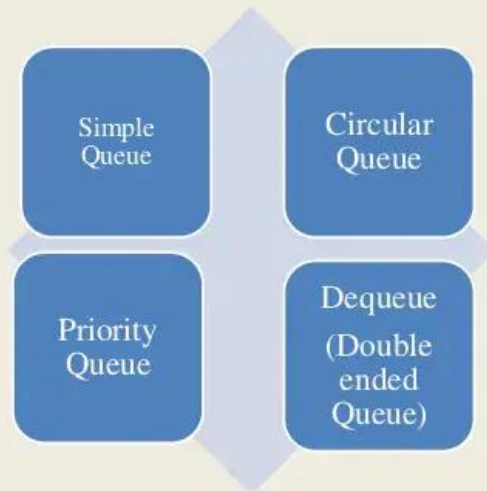
- A Queue is a special type of data structure where elements are inserted from one end and deleted from other end.
- The end at which elements are added is called rear
- The end at which elements are deleted is called front
- The first element inserted is the first element to be deleted out. Hence it is **First In First Out (FIFO)** or **Last In Last Out (LILO)** data structure.



FIFO/LILO

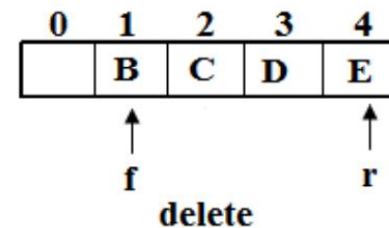
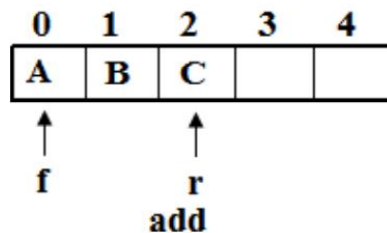
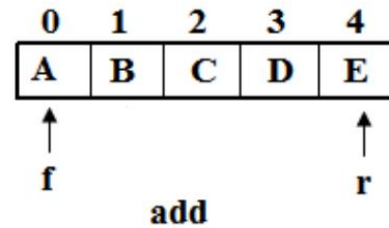
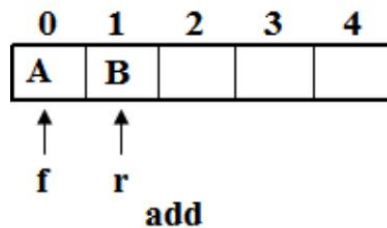
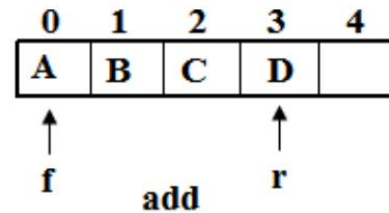
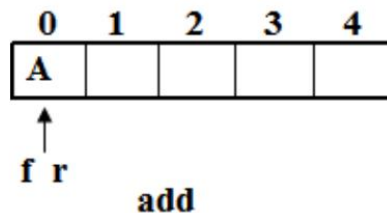
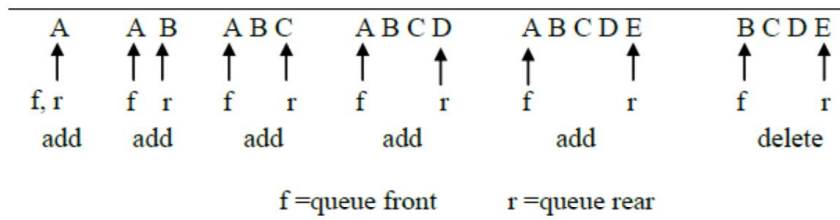
Type of queue

Or ordinary or
linear



Array Representation

$F = -1, r = -1$



1. Queue Create

Queue CreateQ(maxQueueSize) ::=

```
#define MAX_QUEUE_SIZE 100 /* maximum queue size */  
typedef struct  
{  
    int key; /* other fields */  
} element;  
element queue[MAX_QUEUE_SIZE];  
int rear = -1;  
int front = -1;
```

2. Boolean IsEmptyQ(queue) ::= front == -1 || front > rear

3. Boolean IsFullQ(queue) ::= rear == MAX_QUEUE_SIZE-1

4. addq(item)

```
void addq(element item)
{ /* add an item to the queue */
    if (rear == MAX_QUEUE_SIZE-1)
        queueFull();
    queue [++rear] = item;
}
```

5. deleteq()

```
element deleteq()
{ /* remove element at the front of the queue */
    if (front == -1 || front > rear)
        return queueEmpty( ); /* return an error key */
    return queue[++front];
}
```

6. queueFull()

The queueFull function which prints an error message and terminates execution

```
void queueFull()  
{  
    printf("Queue is full, cannot add element");  
    exit(0);  
}
```

```
#define MAX 10
```

```
int queue[MAX];
```

```
int f=-1;
```

```
int r=-1;
```

```
void insert()
```

```
{
```

```
    if(rear==MAX-1)
```

```
        printf("overflow");
```

```
    else
```

```
        if(f== -1)
```

```
        {
```

```
            f++;
```

```
        }
```

```
        printf("enter element to be inserted");
```

```
        scanf("%d", &ele);
```

```
        Queue[++r]=ele;
```

```
}
```

```
void delete()
```

```
{
```

```
    if(front== -1 || front>rear)
```

```
        printf("underflow");
```

```
    else
```

```
        Printf("element deleted is %d", queue[front]);
```

```
        front++;
```

```
}
```

```
void display()
```

```
{
```

```
    if(front== -1 || front>rear)
```

```
        Printf("display not possible");
```

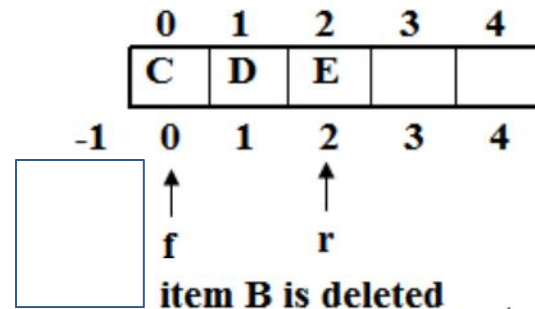
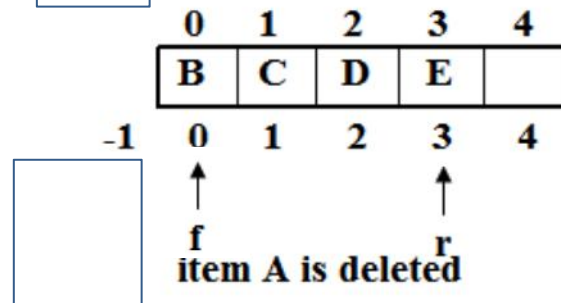
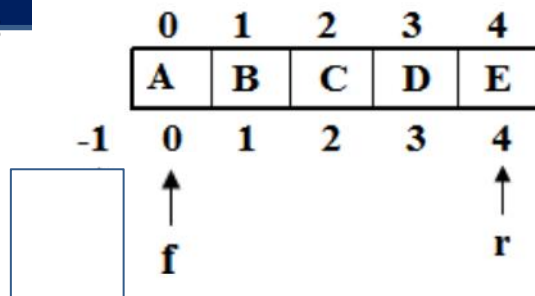
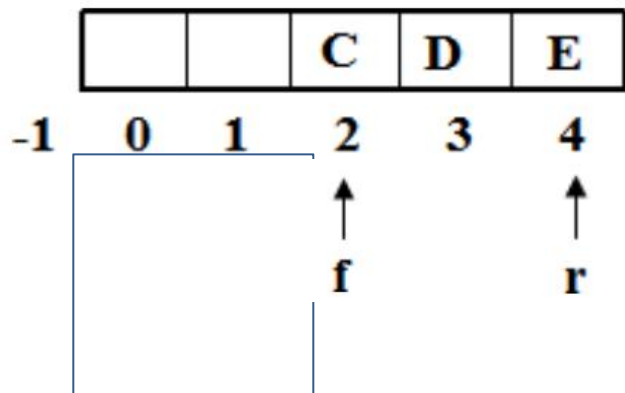
```
    else
```

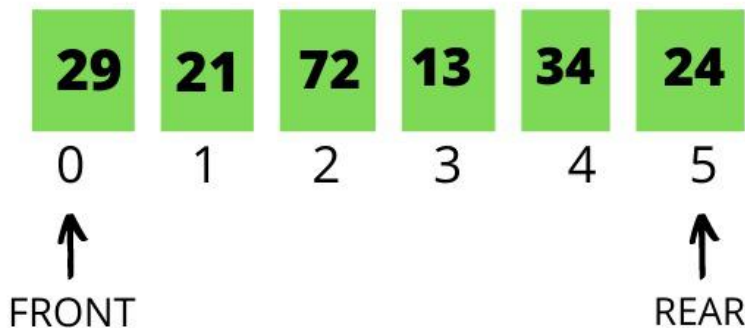
```
        Printf("queue elements are:");
```

```
        For(int i=f; i<=r; i++)
```

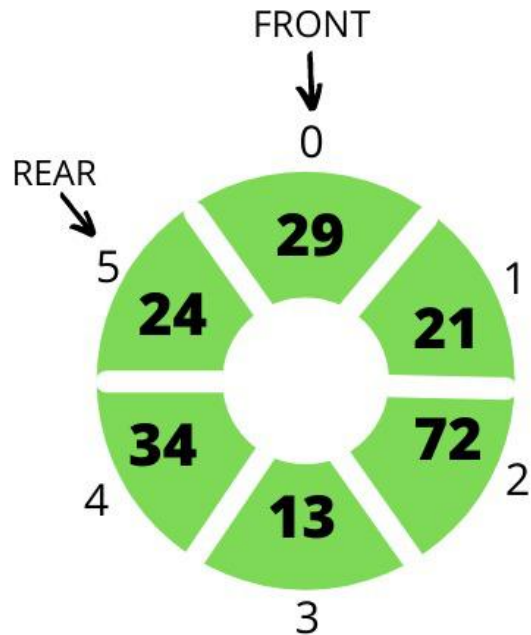
```
            Printf("%d\t", queue[i]);
```

```
}
```





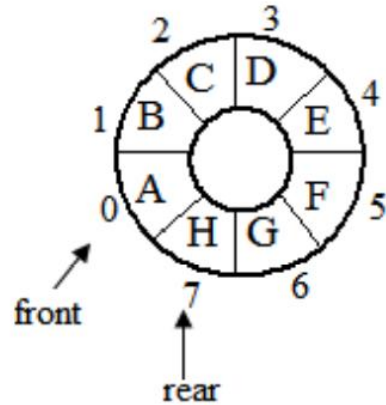
LINEAR QUEUE



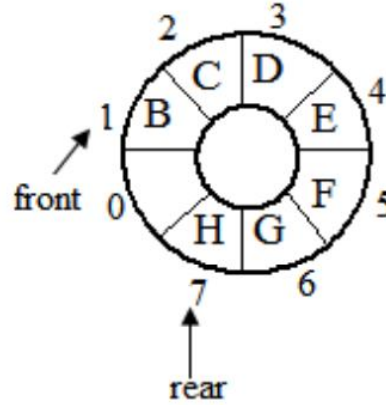
CIRCULAR QUEUE

$(\text{front} + 1) \% \text{MAX_QUEUE_SIZE}$

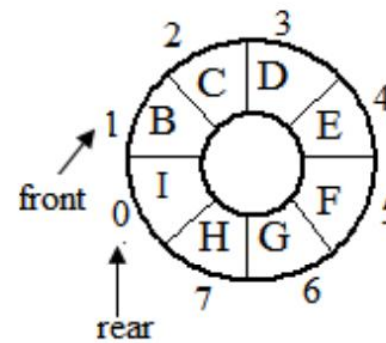
$(\text{rear} + 1) \% \text{MAX_QUEUE_SIZE}$



(a)



(b)



(c)


```
#define MAX 10
```

```
int queue[MAX];
```

```
int f=-1;
```

```
int r=-1;
```

```
void enqueue(int n)
```

```
{
```

```
    If(f== -1 && r== -1)
```

```
        f=r=0;
```

```
        queue[r]=n;
```

```
    r=(r+1)%MAX;
```

```
    If(r==f)
```

```
        Printf("queue is full");
```

```
    Else
```

```
        queue[rear]=n;
```

```
void dequeue()
```

```
{
```

```
    If(f== -1 && r== -1)
```

```
        Printf("queue is empty")
```

```
    Else
```

```
        Printf(element deleted %d", queue[f]);
```

```
        f=(f+1)%MAX;
```

```
void display()
```

```
{
```

```
    If(f== -1 && r== -1)
```

```
        Printf("queue is empty")
```

```
    else
```

```
        Printf("Queue elements are:");
```

```
        for(i=f; i!=r; (i+1)%MAX)
```

```
            printf("%d\t", queue[i]);
```

```
}
```

```
Printf("%d", queue[i]);
```

Operations performed on dequeues:

- > insert an item from front end
- > insert an item from rear end
- > delete an item from front end
- > delete an item from rear end
- > display the contents of queue

Insert At Front

Insert At Rear

Deque Data Structure



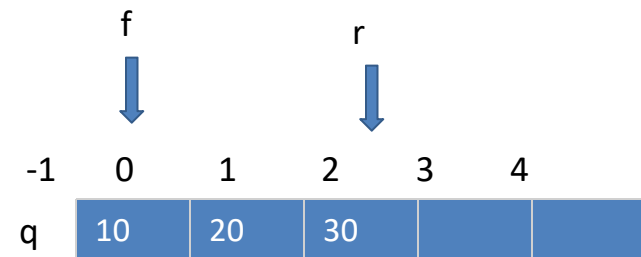
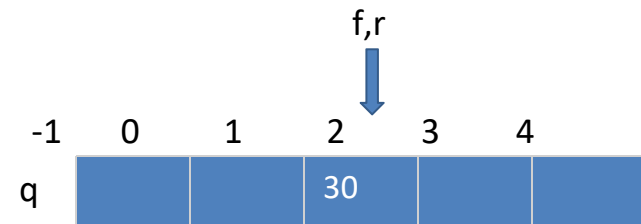
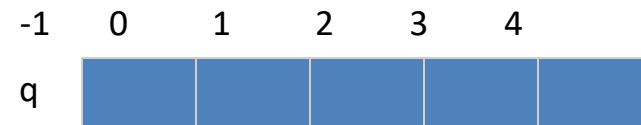
Remove from Front

Remove from Back

```
void insertfront()
{
    If(f==-1 && r==-1)
        f++;
        q[++rear]=item;

    Else If(f!=-1)
        q[--f]=item;

    Else
        Printf("front insertion not possible");
}
```



f,r



-1

0

1

2

3

4

q



void deleterear()

{

if(f== -1 && r== -1)

Printf("no items");

Else

Printf("item deleted is %d", q[r]);

r--;

}

f



r



-1

0

1

2

3

4

q



There are two variations of a deque

1. **Input-restricted deque** is a deque which allows insertions at only one end of the list but allows deletions at both ends of the list
2. **Output-restricted deque** is a deque which allows deletions at only one end of the list but allows insertions at both ends of the list.

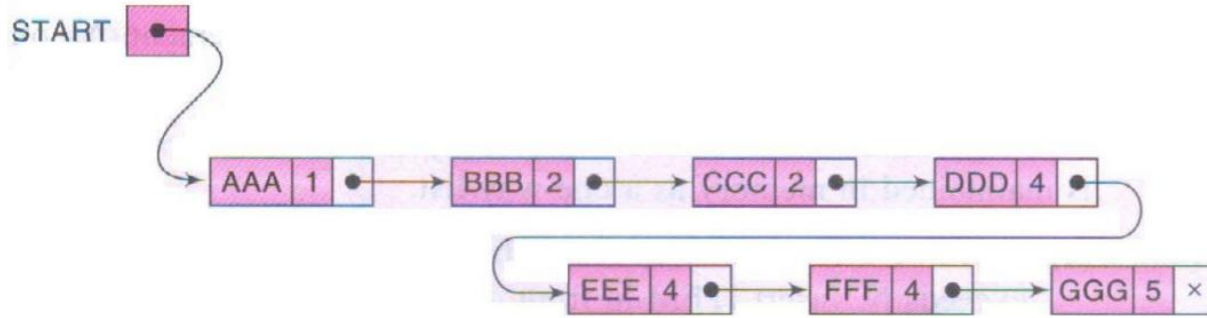
A queue in which we are able to insert items or remove items from any position based on some priority is often referred to as priority queue.

(1) An element of higher priority is processed before any element of lower priority.

(2) Two elements with the same priority are processed according to the order in which they were added to the queue.

One way to maintain a priority queue in memory is by means of a **one-way list**, as follows:

1. Each node in the list will contain three items of information: an information field INFO, a priority number PRN and a link number LINK.
2. A node X precedes a node Y in the list
 - a. When X has higher priority than Y
 - b. When both have the same priority but X was added to the list before Y. This means that the order in the one-way list corresponds to the order of the priority queue.



Algorithm to delete and process the first element in a priority queue

Algorithm: This algorithm deletes and processes the first element in a priority queue which

appears in memory as a one-way list.

1. Set ITEM:= INFO[START] [This saves the data in the first node.]
2. Delete first node from the list.
3. Process ITEM.
4. Exit.

Algorithm to add an element to priority queue

Algorithm: This algorithm adds an ITEM with priority number N to a priority queue which is maintained in memory as a one-way list.

1. Traverse the one-way list until finding a node X whose priority number exceeds N. Insert ITEM in front of node X.
2. If no such node is found, insert ITEM as the last element of the list.

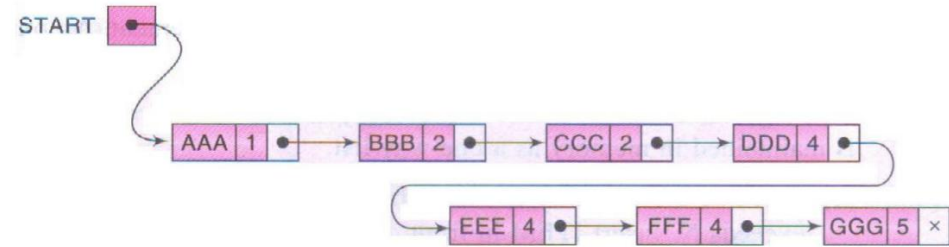
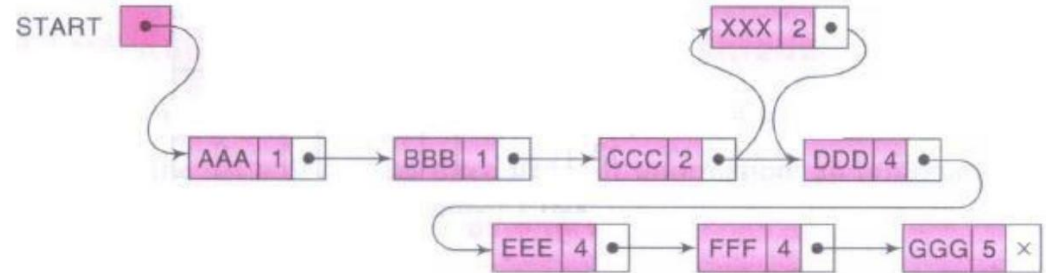


Fig (a)



Fig(b)

Array Representation of Priority Queue

- Another way to maintain a priority queue in memory is to use a separate queue for each level of priority (or for each priority number).
- Each such queue will appear in its own circular array and must have its own pair of pointers, FRONT and REAR.
- If each queue is allocated the same amount of space, a two-dimensional array QUEUE can be used instead of the linear arrays.

	FRONT	REAR
1	2	2
2	1	3
3	0	0
4	5	1
5	4	4

	1	2	3	4	5	6
1		AAA				
2	BBB	CCC	XXX			
3						
4	FFF				DDD	EEE
5				GGG		

Algorithm: This algorithm deletes and processes the first element in a priority queue maintained by a two-dimensional array QUEUE.

1. [Find the first non-empty queue.]

Find the smallest K such that $FRONT[K] \neq NULL$.

2. Delete and process the front element in row K of QUEUE.

3. Exit.

Algorithm: This algorithm adds an ITEM with priority number M to a priority queue maintained by a two-dimensional array QUEUE.

1. Insert ITEM as the rear element in row M of QUEUE.

2. Exit.