

ATME COLLEGE OF ENGINEERING

13th KM Stone, Bannur Road, Mysore - 570 028



DEPARTMENT OF ELECTRICAL & ELECTRONICS ENGINEERING

NOTES

Course Title: High Voltage and Power System Protection

Course CODE: 21EE71

SEMESTER: VII

Academic Year - 2024-25

INSTITUTIONAL VISION AND MISSION

VISION:

- Development of academically excellent, culturally vibrant, socially responsible and globally competent human resources.

MISSION:

- To keep pace with advancements in knowledge and make the students competitive and capable at the global level.
- To create an environment for the students to acquire the right physical, intellectual, emotional and moral foundations and shine as torchbearers of tomorrow's society.
- To strive to attain ever-higher benchmarks of educational excellence.

Department Vision and Mission

Vision:

To create Electrical & Electronics Engineers who excel to be technically competent and fulfill the cultural and social aspirations of the society.

Mission:

- To provide knowledge to students that builds a strong foundation in the basic principles of electrical engineering, problem solving abilities, analytical skills, soft skills and communication skills for their overall development.
- To offer outcome based technical education.
- To encourage faculty in training & development and to offer consultancy through research & industry interaction.

Program Educational Objectives (PEOs)

PEO1: To produce competent and ethical Electrical and Electronics Engineers who will exhibit the necessary technical and managerial skills to perform their duties in society.

PEO2: To make Graduates continuously acquire and enhance their technical and socio-economic skills.

PEO3: To aspire Graduates on R&D activities leading to offering solutions and excel in various career paths.

PEO4: To produce quality engineers who have the capability to work in teams and contribute to real time projects.

Program Outcomes (POs)

Engineering Graduates will be able to:

PO1: Engineering Knowledge: Apply the knowledge of mathematics, science, engineering fundamentals and an engineering specialization to the solution of complex engineering problems.

PO2: Problem Analysis: Identify, formulate, review research literature, and analyze complex engineering problems reaching substantiated conclusions using first principles of mathematics, natural sciences, and engineering sciences.

PO3: Design / Development of solutions: Design solutions for complex engineering problems and design system components or processes that meet the specified needs with appropriate consideration for the public health and safety, and the cultural, societal, and environmental considerations.

PO4: Conduct investigations of complex problems: Use research-based knowledge and research methods including design of experiments, analysis and interpretation of data, and synthesis of the information to provide valid conclusions.

PO5: Modern tool usage: Create, select, and apply appropriate techniques, resources, and modern engineering and IT tools including prediction and modeling to complex engineering activities with an understanding of the limitations.

PO6: The engineer and society: Apply reasoning informed by the contextual knowledge to assess societal, health, safety, legal and cultural issues and the consequent responsibilities relevant to the professional engineering practice.

PO7: Environment and sustainability: Understand the impact of the professional engineering solutions in societal and environmental contexts, and demonstrate the knowledge of, and need for sustainable development.

PO8: Ethics: Apply ethical principles and commit to professional ethics and responsibilities and norms of the engineering practice.

PO9: Individual and team work: Function effectively as an individual and as a member or leader in diverse teams, and in multidisciplinary settings.

PO10: Communication: Communicate effectively on complex engineering activities with the engineering community and with society at large, such as, being able to comprehend and write effective reports and design documentation, make effective presentations, and give and receive clear instructions.

PO11: Project management and finance: Demonstrate knowledge and understanding of the engineering management principles and apply these to one's own work, as a member and leader in a team, to manage projects and in multidisciplinary environments.

PO12: Life-long learning: Recognize the need for and have the preparation and ability to engage in independent and lifelong learning in the broadest context of technological change.

Program Specific Outcomes (PSOs)

The students will develop an ability to produce the following engineering traits:

PSO1: Apply the concepts of Electrical & Electronics Engineering to evaluate the performance of power systems and also to control industrial drives using power electronics

PSO2: Demonstrate the concepts of process control for Industrial Automation, design models for environmental and social concerns and also exhibit continuous self- learning

High Voltage and Power System Protection

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List of Reference Books
<ol style="list-style-type: none">1. High Voltage Engineering Fundamentals, E. Kuffel, W.S. Zaengl, J. Kuffel, Newnes, 2 nd Edition, 20002. High Voltage Engineering, Wadhwa C.L., New Age International, 3 rd Edition, 2012.3. Protection and Switchgear, Bhavesh et al, Oxford, 1st Edition, 2011.4. Power System Switchgear and Protection, N. Veerappan, S.R. Krishnamurthy, S. Chand, 1st Edition, 2009

MODULE -2 Generation of High Voltages and Currents

Syllabus

- 2.1 Generation of High Direct Current Voltages
- 2.2 Generation of High Alternating Voltages
- 2.3 Generation of Impulse Voltages
- 2.4 Tripping and Control of Impulse Generators.
- 2.5 Generation of Impulse Currents

Course Objectives

To discuss generation of high voltages and currents and their measurement

2. Introduction

Need for HV Generation

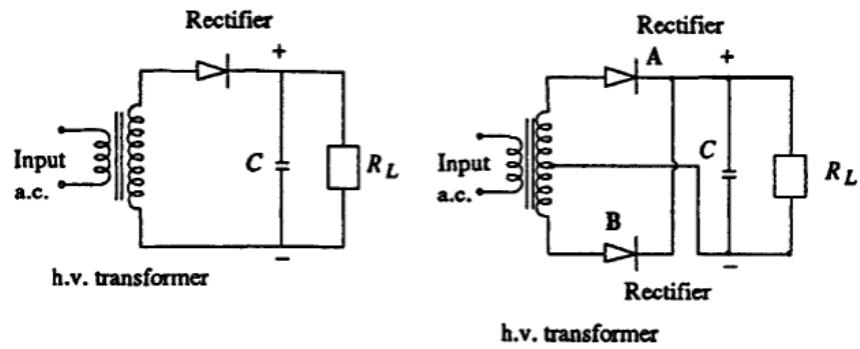
- Importance of High voltage DC & AC: High voltage dc require for industry, medical sciences, HVDC transmission etc.
- Applications of high voltage DC: Electrostatic precipitator (EPS) in thermal power plant for the ash handling unit, electrostatic paint, cement industry etc.
- Applications of high voltage AC: Power transmission.

2.1 Generation of High voltage DC

1. Rectifier circuits
2. Van de Graff generators
3. Cockcroft- Walton type high voltage DC set

1. Rectifier circuits for producing high DC voltages from AC sources.

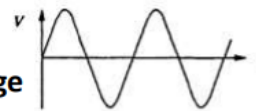
- (a) Half wave rectifiers.
- (b) Full wave rectifiers.
- (c) Voltage doubler type rectifiers.



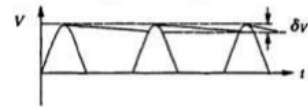
Half wave rectifier

Full wave rectifier

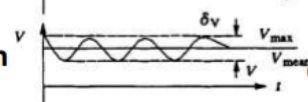
Sinusoidal Input voltage



Half wave rectifier



Full wave rectifier

Ripple voltage, V_{max} & V_{mean} 

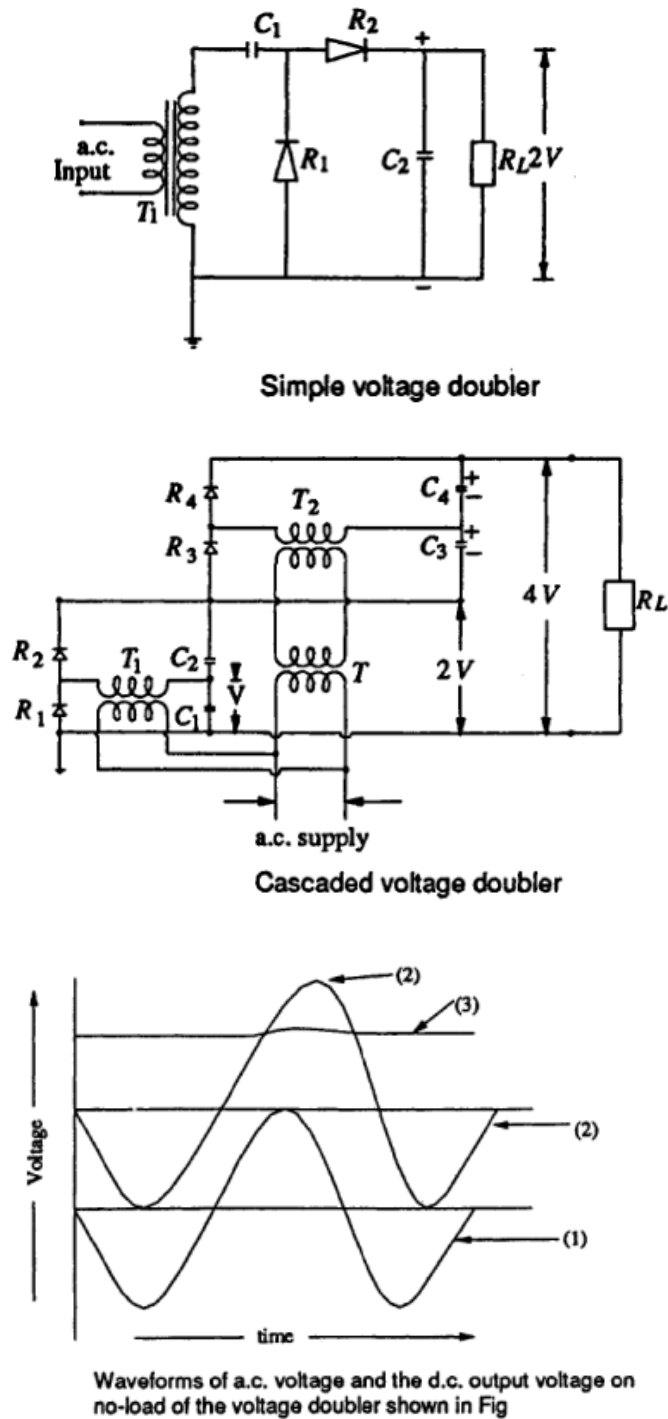


Fig2.1: 1. AC input voltage waveform 2.AC output voltage waveform without condenser filter

3.AC Output voltage waveform with condenser filter

2.1.1 Van de Graff generators

- It is a type of electrostatic generator
- It generates high potential differences

- Then the generated potential differences are used to speed up the particles like ions etc. So it is a “**particle accelerator**”
- **Application:** Nuclear physics experiments
- The potential difference achieved in modern Van de Graaff generators can reach 5 megavolts.
- A Van de Graaff generator operates by transferring electric charge from a moving belt to a terminal.
- The high voltages generated by the Van de Graaff generator can be used for accelerating subatomic particles to high speeds, making the Van de graaff generator a useful tool for fundamental Nuclear physics research.

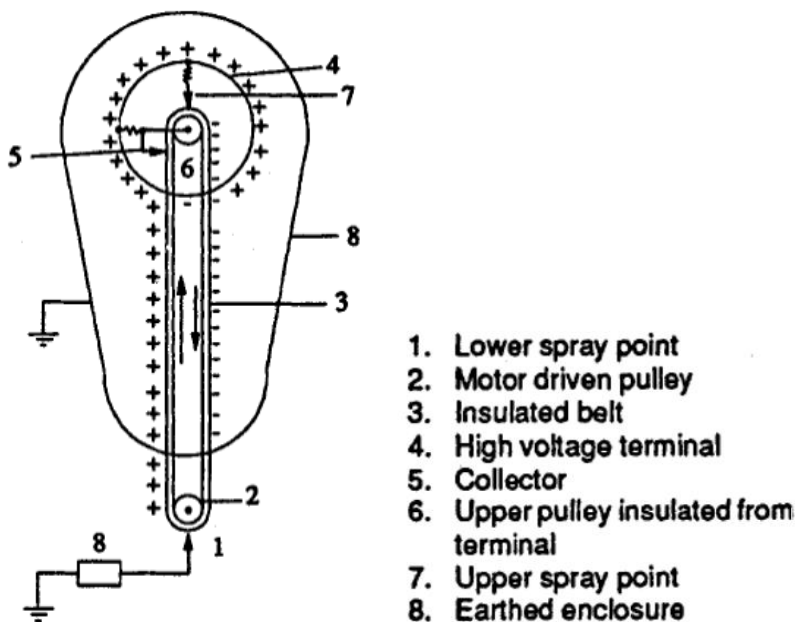
Working of the generator is based on two principles:

1. Discharging action of sharp points, ie., electric discharge takes place in air or gases readily, at pointed conductors.
2. If the charged conductor is brought in to internal contact with a hollow conductor, all of its charge transfers to the surface of the hollow conductor no matter how high the potential of the latter may be.

Applications

1. Accelerating electrons to sterilize food and process materials,
2. Accelerating protons for nuclear physics experiments,
3. Driving X-ray tubes, etc.

Construction



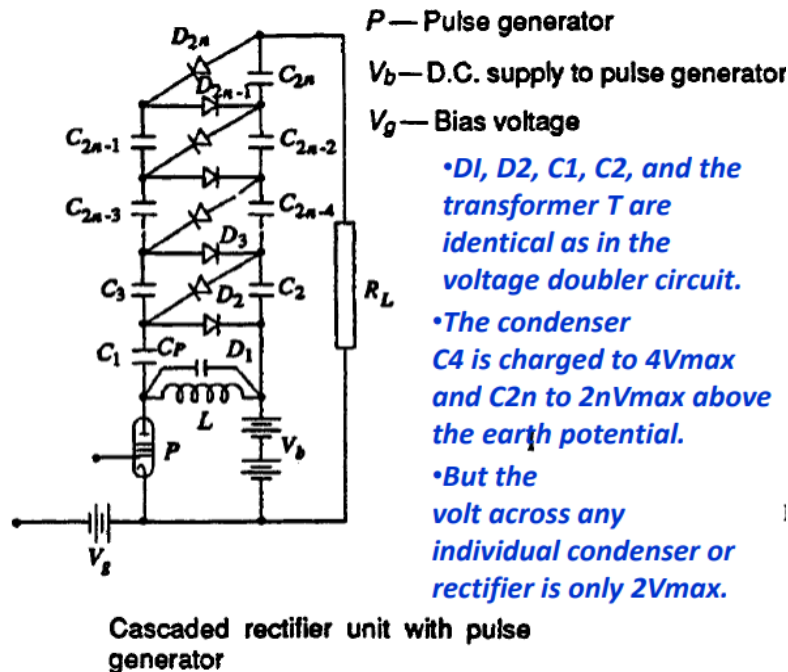
1. A simple Van de Graaff-generator consists of a belt of silk, or a similar flexible dielectric material, running over two metal pulleys etc
2. The generator is usually enclosed in an earthed metallic cylindrical vessel and is operated under pressure or in vacuum.
3. Charge is sprayed on to an insulating moving belt from corona points
4. Require the potential of 10 to 100 kV
5. The belt is driven by an electric motor at a speed of 1000 to 2000 rpm
6. Potential of high voltage electrode rises in the rate of

$$\frac{dV}{dt} = \frac{I}{C} \frac{dQ}{dt} = \frac{I}{C} \quad \text{where } I \text{ is the net charging current.}$$

7. The shape of electrodes are spherical
8. The charging of the belt is done by the lower spray points which are sharp needles and connected to a DC source of about 10 to 100 kV, so that the corona is maintained between the moving belt and the needles.
9. Belt has self charging system

2.1.2Cock croft Walton type high voltage DC set.

1. Cascaded voltage multiplier circuits (Voltage Doubler circuit) for higher voltages are cumbersome(difficult) and require too many supply and isolating transformers.
2. It is possible to generate very high DC voltages from single supply transformers by extending the simple voltage doubler circuits.
3. This is simple and compact when the load current requirement is less than one milli ampere, such as for cathode ray tubes, etc.
4. Valve type pulse generators may be used instead of conventional AC supply.
5. The circuit becomes compact



D_1, D_3, D_{2n-1} conduct:
 positive half
 Cycle.
 D_2, D_4, D_{2n} conduct:
 Negative half cycle.

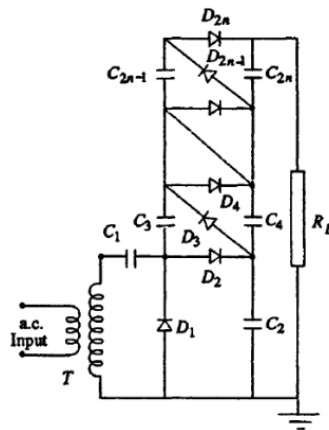


Fig 2.2 :Cockcroft Walton voltage multiplier circuit

1. A DC power supply of about 500V applied to the pulse generator, is sufficient to generate a high voltage DC of 50 to 100 kV with suitable number of stages.
2. D_1, D_2, C_1, C_2 , and the transformer T are identical as in the voltage doubler circuit.
3. The condenser C_4 is charged to $4V_{max}$ and C_{2n} to $2nV_{max}$ above the earth potential.
4. But the volt across any individual condenser or rectifier is only $2V_{max}$.
5. D_1, D_3, D_{2n-1} conduct: Positive half Cycle. • D_2, D_4, D_{2n} conduct: Negative half cycle.

1. Calculation of output voltage

- The pulses generated in the anode circuit of the valve P are rectified and the voltage is cascaded to give an output of across the load RL.

$$\text{Output} = 2nV_{\max}$$

- A trigger voltage pulse of triangular waveform (ramp) is given to make the valve switched on and off.

Ripple content & Voltage drop in cockcroft- Walton type dc set

2. Calculation of ripple voltage

$$\delta V = \text{the ripple} = \frac{I_1}{fC_2}$$

I_1 = load current from the rectifier

f = supply frequency,

In general the expression for ripple voltage is given by $\frac{nI_1}{fC}$.

n stages the total ripple will be

$$\delta V_{\text{total}} = \frac{I_1}{fC} [1 + 2 + 3 \dots + n] = \frac{I_1}{fC} \frac{n(n+1)}{2}$$

3. Calculation of % ripple

$$\% \text{ ripple} = \frac{\delta V \times 100}{2nV_{\max}}$$

Where $2nV_{\max}$ is the output voltage.

4. Calculation of voltage regulation

$$\text{Voltage drop, } \Delta V = \frac{I}{fC} \left(\frac{2}{3}n^3 + \frac{n^2}{2} - \frac{n}{6} \right)$$

$$\text{Voltage regulation} = \left(\frac{\Delta V}{2nV_{\max}} \right)$$

5. Optimum number of stages for minimum voltage drop

- In addition to the ripple δV , there is a voltage drop Δv which is the difference between the theoretical no load and the on load voltage.
- optimum number of stages for the minimum voltage drop may be expressed as

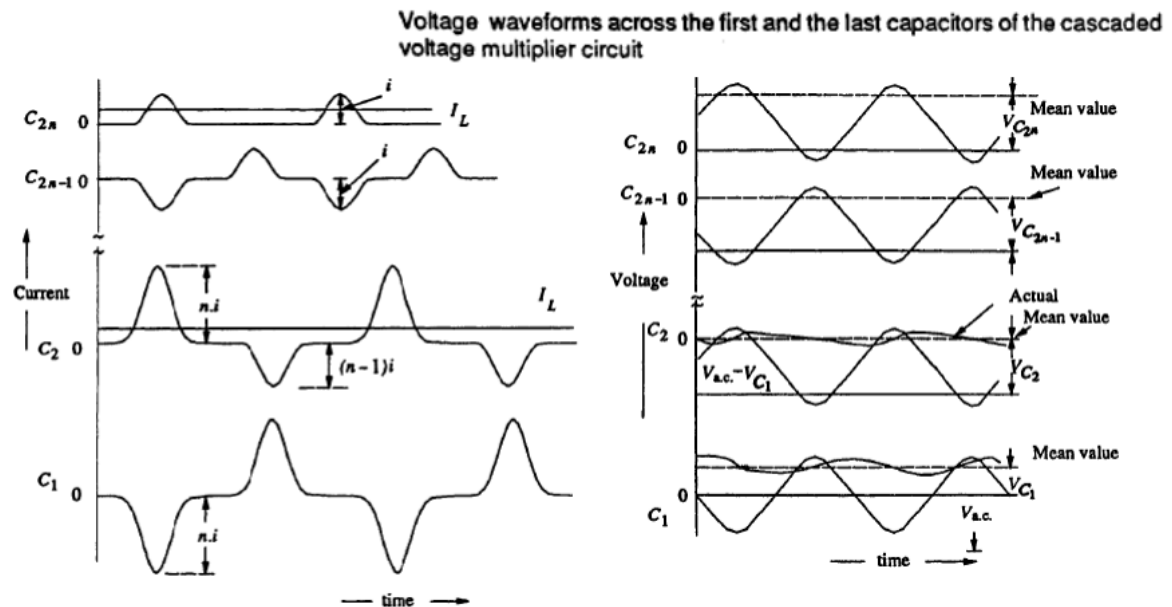
$$n_{\text{optimum}} = \sqrt{\frac{V_{\text{max}} f C}{I}}$$

where I is the load current.

Eg Thus, for a multiplier or a cascaded circuit with

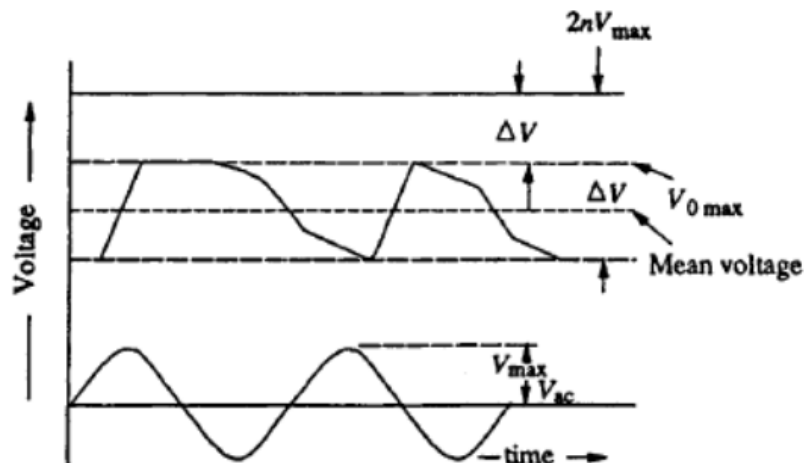
$f = 50 \text{ Hz}$, $C = 0.1 \text{ micro Farad}$, $V_{\text{max}} = 100 \text{ kV}$ and $I = 5 \text{ mA}$, the number of stages = 10.

Current and voltage waveforms of cock croft- Walton type high voltage DC Set



Schematic current waveforms across the first and the last capacitors of the cascaded voltage multiplier circuit

Ripple content & Voltage drop in cock croft- Walton type dc set



Ripple voltage δV and the voltage drop ΔV in a cascaded voltage multiplier circuit

2.1.3.Numerical on Cockroft Walton type high voltage DC set

A Cockcroft-Walton type voltage multiplier has eight stages with capacitances, all equal to $0.05 \mu\text{F}$. The supply transformer secondary voltage is 125 kV at a frequency of 150 Hz. If the load current to be supplied is 5 mA, find (a) the percentage ripple, (b) the regulation, and (c) the optimum number of stages for minimum regulation or voltage drop.

Solution: (a) Calculation of Percentage Ripple

$$\text{The ripple voltage } \delta V = \frac{I}{fC} \frac{(n)(n+1)}{2}$$

$$I = 5 \text{ mA}, f = 150 \text{ Hz}, C = 0.05 \mu\text{F}, \text{ and } n = 8,$$

$$\therefore \delta V = \frac{5 \times 10^{-3}}{150 \times 0.05 \times 10^{-6}} \times \frac{8 \times 9}{2}$$

$$= 24 \text{ kV}$$

$$\% \text{ ripple} = \frac{\delta V \times 100}{2nV_{\max}} = \frac{24 \times 100}{2 \times 125 \times 8}$$

(b) Calculation of Regulation

$$\text{Voltage drop, } \Delta V = \frac{I}{fC} \left(\frac{2}{3}n^3 + \frac{n^2}{2} - \frac{n}{6} \right)$$

$$= \frac{5 \times 10^{-3}}{150 \times 0.05 \times 10^{-6}} \left[\left(\frac{2}{3} \times 8^3 \right) + \left(\frac{1}{2} \times 8^2 \right) - \frac{8}{6} \right]$$

$$= 248 \text{ kV}$$

$$\therefore \text{regulation} \left(\frac{V}{2nV_{\max}} \right) = \frac{248}{2 \times 8 \times 125} = \frac{124}{1000}$$

$$= 12.4\%$$

(c) Calculation of Optimum Number of Stages (n_{optimum})

Since $n > 5$,

$$n_{\text{optimum}} = \sqrt{V_{\max} fC / I}$$

$$= \sqrt{\frac{125 \times 150 \times 0.05 \times 10^{-6} \times 10^3}{5 \times 10^{-3}}}$$

$$= \sqrt{125 \times 1.5}$$

$$= 13.69$$

$$= 14 \text{ stages}$$

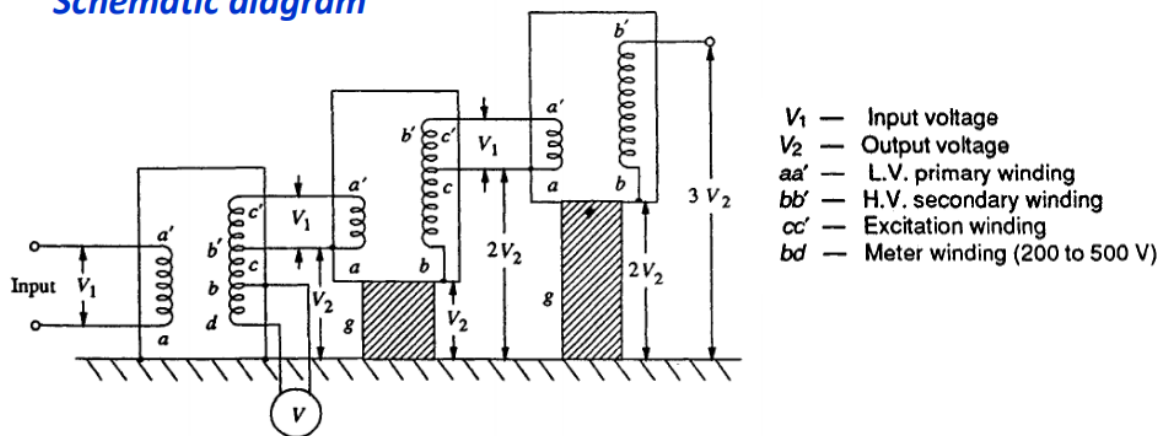
2.2 Generation of HV AC Voltage

Need for Cascade transformer connection

1. When test voltage requirements are less than about 300 kV, a single transformer can be used for test purposes.
2. The impedance of the transformer should be generally less than 5%
3. Transformer must be capable of giving the short circuit current for one minute or more depending on the design.
4. Third winding known as meter winding is provided to measure the output voltage.
5. For higher voltage requirements, a single unit construction becomes difficult and costly due to insulation problems.
6. Transportation and arranging of large transformers become difficult.
7. These drawbacks are overcome by series connection or cascading of the several identical units of transformers, wherein the high voltage windings of all the units effectively come in series.

Schematic diagram of cascade transformer for HVAC generation

Schematic diagram



Cascade transformer connection (schematic)

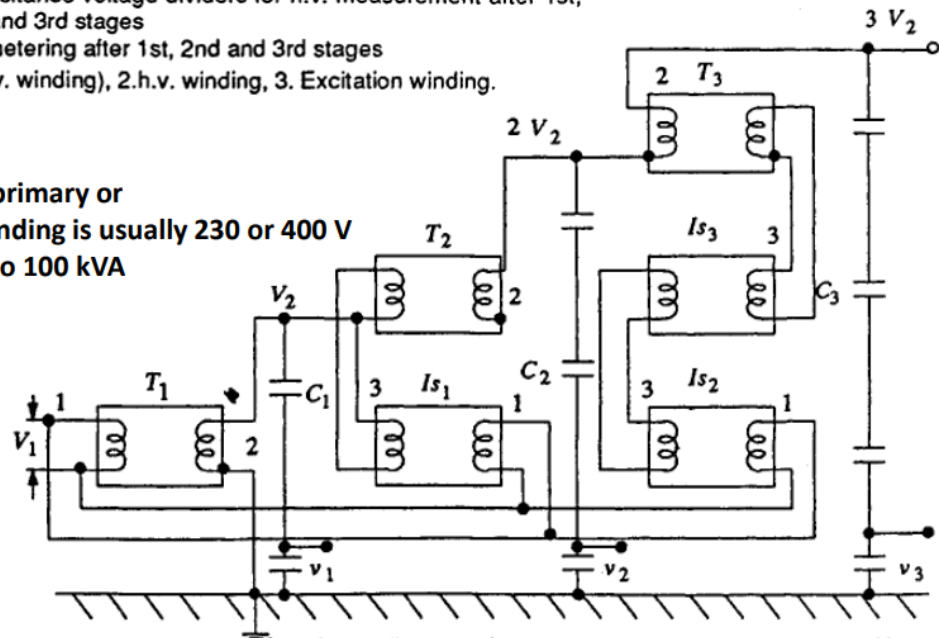
1. The first transformer is at the ground potential along with its tank.
2. The second transformer is kept on insulators and maintained at a potential of V_2 , the output voltage of the first unit above the ground.
3. The high voltage winding of the first unit is connected to the tank of the second unit.
4. The low voltage winding of this unit is supplied from the excitation winding of the first transformer, which is in series with the high voltage winding of the first transformer at its high voltage end.
5. The rating of the excitation winding is almost identical to that of the primary or the low voltage winding

- T_1, T_2, T_3 — Cascade transformer units
 Is_1, Is_2, Is_3 — Isolation transformer units
 C_1, C_2, C_3 — Capacitance voltage dividers for h.v. measurement after 1st, 2nd and 3rd stages
 V_1, V_2, V_3 — For metering after 1st, 2nd and 3rd stages
 1. Primary (l.v. winding), 2. h.v. winding, 3. Excitation winding.

•The rating of the primary or the low voltage winding is usually 230 or 400 V for small units up to 100 kVA

For

•larger outputs the rating of the low voltage winding may be 3.3kV, 6.6 kV or 11 kV.



- Supply to the units can be obtained from a motor-generator set or through an induction regulator for variation of the output voltage.
- Isolating transformers Is_1, Is_2 and Is_3 & are 1:1 ratio transformers
- They are insulated to their respective tank potentials and are meant for supplying the excitation for the second and the third stages at their tank potentials
- Power supply to the isolating transformers is also fed from the same AC input.

Advantages of cascade connection

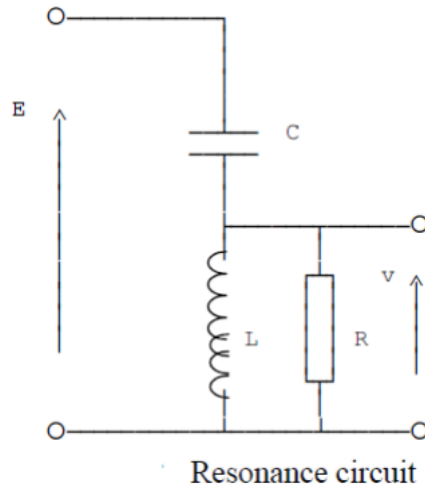
- Natural cooling is sufficient
- Transformers are light and compact
- Ease of transportation & assembly
- Construction is similar to the isolating transformer & cascaded unit
- Either star or delta connection are possible

Draw backs

- More space requirement and expensive

2.2.1 Resonant Circuit

The resonance principle of a series tuned L-C circuit can be made use of to obtain a higher voltage with a given transformer.



Basic principle of Resonant circuit

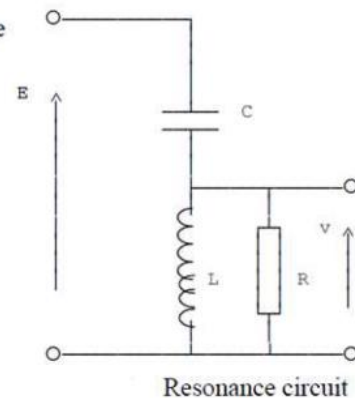
The resonance principle of a series tuned L-C circuit can be made use of to obtain a higher voltage with a given transformer.

Let R represent the equivalent parallel resistance across the coil and the device under test. The current i would be given by

$$i = \frac{E}{\frac{1}{j\omega C} + \frac{j\omega L R}{R + j\omega L}}$$

so that $v = i \cdot \frac{j\omega L R}{R + j\omega L}$

i.e. $v = \frac{-\omega^2 L C R \cdot E}{R + j\omega L - \omega^2 L C R} = -\frac{E \cdot R}{j\omega L}$ at resonance



Since R is usually very large, the Q factor of the circuit ($Q = R/L\omega$) would be very large, and the output voltage would be given by

$$|v| = E \cdot \frac{R}{L\omega} = E \cdot Q$$

It can thus be seen that a much larger value than the input can be obtained across the device under test in the resonant principle.

$$\text{at resonance } \omega = 2\pi f = \frac{1}{\sqrt{LC}}$$

2.2.2 Resonant Transformers

1. resonant transformer, an electrical component which consists of two high Q coils wound on the same core with capacitors connected across the windings to make two coupled LC circuits.
2. Resonant transformer is one of the best choice for high voltage generation which operates on resonance phenomenon ($X_L = X_C$).
3. In resonance condition, the current through test object is very large and that is limited only by the resistance of the circuit.

- The waveform of the voltage across the test object will be purely sinusoidal.

Applications of Resonant Transformer:

- This principle is utilized in testing at very high voltages and on occasions requiring large current outputs such as cable testing, dielectric loss measurements, partial discharge measurements, etc.

Series Resonant Transformers

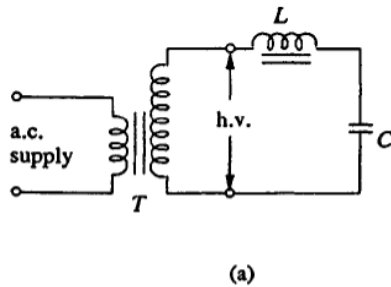


Fig. 6.12a Transformer

- T** — Testing transformer
L — Choke
C — Capacitance of h.v. terminal and test object
L₀ — Magnetizing inductance

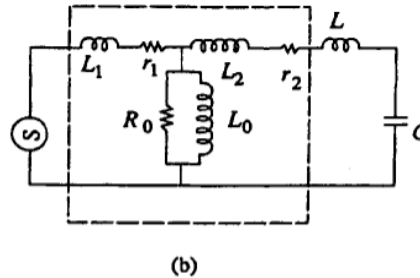


Fig. 6.12b Equivalent circuit

- L₁, L₂** — Leakage inductances of the transformer
r₁, r₂ — Resistances of the windings
R₀ — Resistance due to core loss

- The equivalent circuit of HV testing circuit consists of a) leakage reactance of the winding, b) winding resistance, c) magnetizing reactance, d) shunt capacitance across the output
- It is possible to have a series resonance at power frequency ω , if

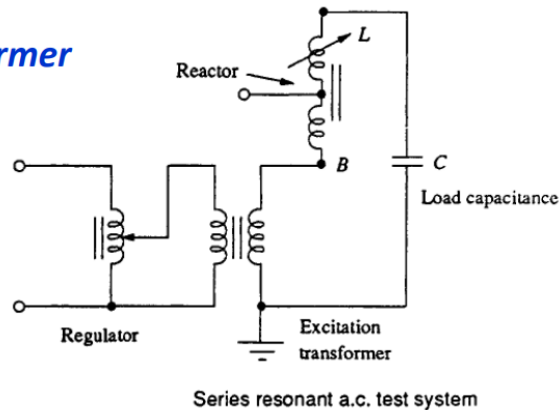
$$(L_1 + L_2) = 1/\omega C$$

- During the resonance condition current in the test object is very large and is limited only by the resistance of the circuit.
- The magnitude of the voltage across the capacitance C of the test object will be

$$V_C = \left| \frac{-jVX_C}{R + j(X_L - X_C)} \right| = \frac{V}{R} X_C = \frac{V}{\omega CR}$$

- Q factor of the circuit and gives the magnitude of the voltage multiplication across the test object under resonance conditions.
- The input voltage required for excitation is reduced by a factor 1/2, and the output kVA required is also reduced by a factor 1/Q.
- The secondary power factor of the circuit is unity.

Series Resonant transformer



Ratings: Regulator : 10 – 100 kVA
 Excitation transformer : 10 – 100 kVA with an output voltage of about 10 kV.
 Reactor voltage – each unit up to 300 kV.

1. A voltage regulator of either the auto-transformer type or the induction regulator type is connected to the supply mains.
2. The secondary winding of the exciter transformer is connected across the H.V reactor, L, and the capacitive load C.
3. The inductance of the reactor L is varied by varying its air gap and operating range is set in the ratio 10 : 1.
4. Capacitance C comprises of the capacitance of the test object, capacitance of the measuring voltage divider, capacitance of the high voltage bushing etc.
5. The Q-factor obtained in these circuits will be typically of the order of 50.

Advantages of series resonant circuit

1. It gives an output of pure sine wave.
2. Power requirements are less (5 to 10% of total kVA required).
3. No high-power arcing and heavy current surges occur if the test object fails, as resonance ceases at the failure of the test object.
4. Cascading is also possible for very high voltages.
5. Simple and compact test arrangement.
6. No repeated flashovers occur in case of partial failures of the test object and insulation recovery

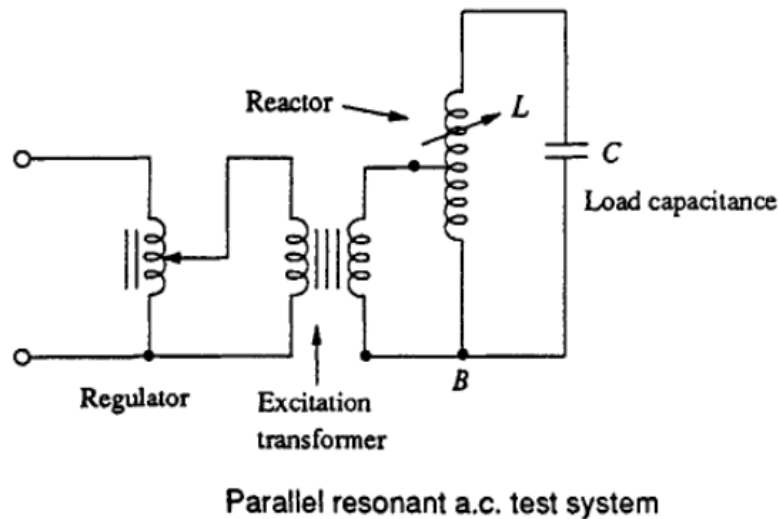
Disadvantages of series resonant circuit

1. Requirements of additional variable chokes capable of withstanding the full test voltage and the full current rating

2.2.3 Parallel Resonant Transformer

1. In the parallel resonant mode the high voltage reactor is connected as an auto-transformer and the circuit is connected as a parallel resonant circuit.
2. The advantage of the parallel resonant circuit is that more stable output voltage can be obtained along with a high rate of rise of test voltage.
3. Independent of the degree of tuning and the Q-factor.

4. Single unit resonant test systems are built for output voltages up to 500 kV, while cascaded units for outputs up to 3000 kV, 50/60 Hz are available.



Numerical on Parallel Resonant circuit

Example : A 100 kVA, 400 V/250 kV testing transformer has 8% leakage reactance and 2% resistance on 100 kVA base. A cable has to be tested at 500 kV using the above transformer as a resonant transformer at 50 Hz. If the charging current of the cable at 500 kV is 0.4 A, find the series inductance required. Assume 2% resistance for the inductor to be used and the connecting leads. Neglect dielectric loss of the cable. What will be the input voltage to the transformer ?

Solution

The maximum current that can be supplied by the testing transformer is

$$\frac{100 \times 10^3}{250 \times 10^3} 0.4 \text{ A}$$

$X_C =$ Reactance of the cable is

$$\frac{V_C}{I} = \frac{500 \times 10^3}{0.4} = 1250 \text{ k}\Omega$$

$X_L =$ Leakage reactance of the transformer is

$$\frac{\%X}{100} \times \frac{V}{I} = \frac{8}{100} \times \frac{250 \times 10^3}{0.4} = 50 \text{ k}\Omega$$

At resonance, $X_C = X_L$.

Hence, additional reactance needed

$$= 1250 - 50 = 1200 \text{ k}\Omega$$

Inductance of additional reactance (at 50 Hz frequency)

$$\frac{1200 \times 10^3}{2\pi \times 50} = 3820 \text{ H}$$

R = Total resistance in the circuit on 100 kVA base is $2\% + 2\% = 4\%$.

Hence, the ohmic value of the resistance

$$= \frac{4}{100} \times \frac{250 \times 10^3}{0.4} = 25 \text{ k}\Omega$$

Therefore, the excitation voltage E_2 on the secondary of the transformer

$$= I \times R$$

$$= 0.4 \times 25 \times 10^3$$

$$= 10 \times 10^3 \text{ V or } 10 \text{ kV}$$

The primary voltage or the supply voltage, E_1

$$= \frac{10 \times 10^3 \times 400}{250 \times 10^3}$$

$$= 16 \text{ V}$$

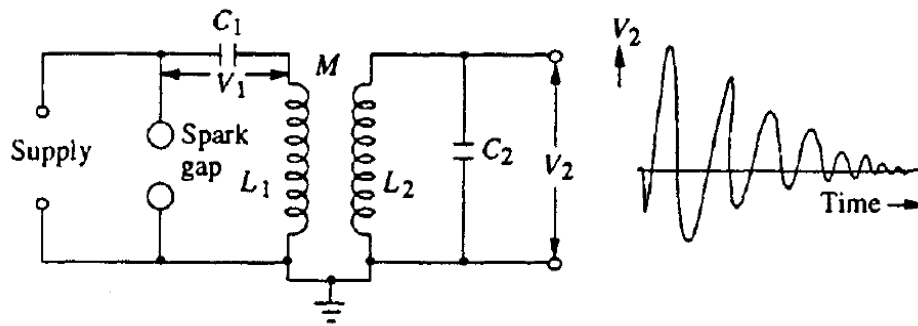
$$\text{Input kW} = \frac{16}{400} \times 100 = 4.0 \text{ kW}$$

2.2.4 Tesla coil

1. Tesla coil is an electrical resonant transformer circuit designed by inventor Nikola Tesla.
2. It is Used to generate or produce high voltage, low current & high frequency AC electricity.
3. High frequency transformer is required.
4. The commonly used high frequency resonant transformer is the Tesla coil.
5. Tesla coil is a doubly tuned resonant circuit.
6. The primary voltage rating is 10 kV and the secondary may be rated to as high as 500 to 1000 kV.
7. Output frequency range: 50kHz to 1 MHz.
8. Damped oscillations can be obtained by using Tesla Coil.

Applications:

1. X-ray generation, experiment in electrical Lighting etc



(a) Equivalent circuit

(b) Output waveform

1. The primary is fed from an AC supply through the condenser C1.
2. A spark gap G connected across the primary is triggered at the desired voltage V, which induces high self excitation in the secondary.
3. Spark gap G act as a switch of the circuit.
4. The primary and the secondary windings (L1 and L2) are wound on an insulated former with no core (air-cored) and are immersed in oil. The windings are tuned to a frequency of 10 to 100 kHz by means of the condensers C1 and C2.
5. The output voltage V is a function of the parameters LI, L2, C1, C2 and the mutual inductance M.
6. Usually, the winding resistances will be small and contribute only for damping of the oscillations.

$$V_2 = \frac{MV_1}{\sigma L_1 L_2 C_1} \frac{1}{\gamma_2^2 - \gamma_1^2} [\cos \gamma_1 t - \cos \gamma_2 t] \quad \text{Output Voltage}$$

$$V_2 = \frac{MV_1}{\sigma L_1 L_2 C_1} \frac{1}{\gamma_2^2 - \gamma_1^2} [\cos \gamma_1 t - \cos \gamma_2 t] \quad \text{Output Voltage}$$

Where

$$\sigma^2 = 1 - \frac{M^2}{L_1 L_2} = 1 - K^2 \quad \text{K = coefficient of coupling between the windings L1 and L2}$$

$$\gamma_{1,2} = \frac{\omega_1^2 + \omega_2^2}{2} \pm \sqrt{\left(\frac{\omega_1^2 + \omega_2^2}{2}\right)^2 - \omega_1^2 \omega_2^2 (1 - K^2)}$$

$$\omega_1 = \frac{1}{\sqrt{L_1 C_1}} \quad \text{and} \quad \omega_2 = \frac{1}{\sqrt{L_2 C_2}}$$

The *peak amplitude* of the secondary voltage V_2 can be expressed as

$$V_{2\max} = V_1 e \sqrt{\frac{L_2}{L_1}}$$

Where ,

$$e = \frac{2\sqrt{(1-\sigma)}}{\sqrt{(1+a)^2 - 4\sigma a}}$$

$$a = \frac{L_2 C_2}{L_1 C_1} = \frac{W_1^2}{W_2^2}$$

1. A more simplified analysis for the Tesla coil may be presented by considering that the energy stored in the primary circuit in the capacitance C_1 is transferred to C_2 via the magnetic coupling.
2. If W_1 is the energy stored in C_1 and W_2 is the energy transferred to C_2 and if the efficiency of the transformer is η , then

$$W_1 = \frac{1}{2} \eta C_1 V_1^2 = \left(\frac{1}{2} C_2 V_2^2\right)$$

$$V_2 = V_1 \sqrt{\eta \frac{C_1}{C_2}}$$

Advantages of Tesla coil

1. The absence of iron core in transformers and hence saving in cost and size.
2. pure sine wave output (Less wave form distortion).
3. Slow build-up of voltage over a few cycles and hence no damage due to switching surges
4. Uniform distribution of voltage across the winding coils due to subdivision of coil stack into a number of units.

2.3 Generation of Impulse Voltages

What is Impulse Voltage

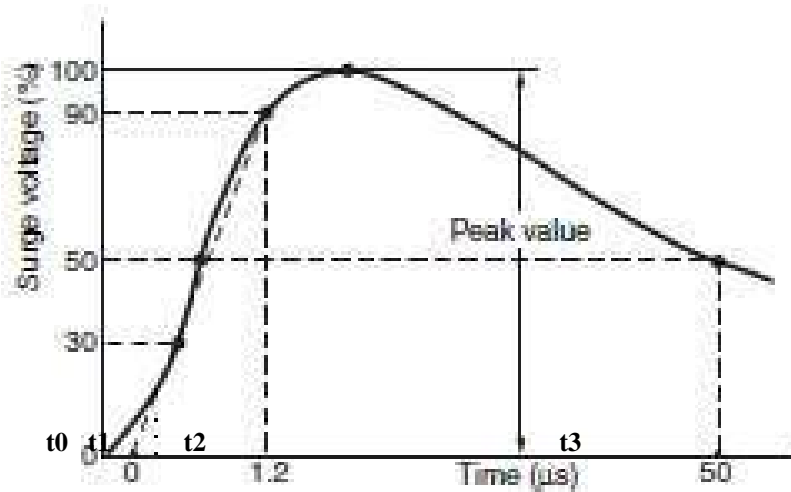
“Impulse voltage is a unidirectional voltage with no appreciable oscillation. It rises rapidly to a maximum value and falls more or less rapidly to zero.”

A unidirectional voltage that rapidly rises to a peak value and then drops to zero more or less rapidly. Also known as *pulse voltage*.

Why Impulse Voltage?

To study the effect of transient over voltages generated by lightning or switching operations on the system.

Representation of Impulse Wave



$$\text{Wave front} = 1.5 \cdot (t_2 - t_1)$$

$$\text{Wave tail} = t_3 - t_0$$

t2 is the time taken to reach 90% of peak value

t1 is the time taken to reach 10% of peak value

a) Impulse Voltage

1. Maximum value is called *peak value* of impulse voltage.
2. If an impulse voltage develops without causing flashover or puncture is called full impulse voltage.
3. Due to flash over or puncture sudden collapse of impulse voltage will occur and it is called as chopped impulse voltage.

b) Wave front & Wave tail

A full impulse voltage consists of both *wave front* and *wave tail*.

1. **Wave front**- Time taken by the wave to reach its maximum value starting from zero value.
 - Since it is difficult to identify the *wave front*, Wave front is considered as 1.5 times (t2-t1)
 - Where t2 is the time taken to reach 90% of peak value
 - t1 is the time taken to reach 10% of peak value
 - (t2-t1) is about 80% of wave front time
2. **Wave tail**- Time measured between the *nominal starting point t0* and the point on the wave tail where the voltage is 50% of peak value.
 - wave tail time (t3-t0)
 - Part of a signal-wave envelope (in time or distance) between the steady-state value (or crest) and the end of the envelope.

c) Standards for impulse voltage

Three standards

1. BSS & ISS standard
2. American Standard Association
3. IEC standard

1. BSS and ISS standard

- *Standard wave shape specified (1/50) microseconds wave.*

i.e a wave front of 1 micro second and wave tail of 50 micro seconds.

- Tolerance is not more than +50% or -50% on the duration of the wave front.
- 20% on the time to half value on the wave tail is allowed.
- *Complete specification of the wave is 100kV, (1/50) microseconds , where 100kV is the peak value of the wave*

2. American Standard Association

- *Wave shape recommended by American standard is 1.5/40 microseconds.*
- *Permissible variation 0.5 microseconds on the wave front and +10 or -10 microseconds for wave tail.*
- *The wave front time is taken as 1.67 times the time taken by the wave to rise from 30% to 90% of its peak value.*
- *Wave tail time is computed same as that of BSS and ISS standard*

3. IEC (International Electro technical Commission)

- *The standard impulse wave shape belonging to 1.2/50μs.*
- *Should withstand higher voltage (above 220kV).*

d) Important Definitions Related to Impulse Voltage (Types of impulse Voltage)**1. Chopped wave**

- *If an impulse voltage is applied to a piece of insulation a flash over or puncture occurs and sudden collapse of impulse voltage is called **chopped wave**.*
- *If the chopping takes place front part of the wave is called front chopped wave*

2. Impulse puncture voltage

- *Peak value of impulse voltage which cause the puncture of the material.*

3. Impulse flash over voltage

- *When impulse voltage applied to the insulating material flash over may or may not occur.*
- *If the **flashover** occurs more than 50% of number of applications, then it is called as **impulse flash over voltage**.*
- *Impulse flash over voltage depends polarity, duration of wave front & wave tail and nature of material.*

IMPULSE GENERATOR

2.3.1 Analysis of single stage impulse generator-expression for Output impulse voltage

“An **impulse generator** is an electrical apparatus which produces very short high-voltage or high-current surges”

It can be classified into two types

a) *Impulse voltage generators*

b) *Impulse current generators.*

Basic impulse generator

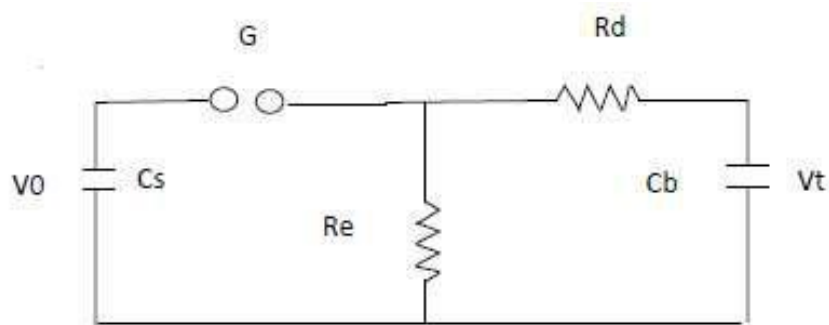


Fig. 2. Basic circuit of single stage impulse generator



a) Why impulse Generator

1. *Impulse generator produces high impulse voltage.*
2. High impulse voltages are used to test the *strength of electric power equipment* against lightning and switching surges.
3. *Steep-front impulse voltages* are sometimes used in *nuclear physics experiments*.

4. High impulse currents are needed for *tests* on equipment such as *lightning arresters*.
5. Fuse testing
6. Technical applications such as lasers, thermonuclear fusion, and plasma devices.

b) Basic Impulse Generator

1. An impulse generator essentially consists of a *capacitor* which is *charged to the required voltage* and *discharged through a circuit*.
2. The circuit parameters can be adjusted to give an impulse voltage of the desired shape.
3. C_s is charged from a dc source *until the spark gap G breaks down*.
4. The voltage is then impressed upon the object under test of capacitance C_b .
5. The *wave shaping resistors R_d and R_e control the front and tail* of the impulse voltage available across C_b respectively.
6. *c)Overall the wave shape* is determined by the *values of the generator capacitance (C_s) and the load capacitance (C_b), and the wave control resistances R_d and R_e* .
7. The output voltage waveform can be defined by

$$v(t) = \frac{V_0}{C_b R_d (\alpha - \beta)} (e^{-\alpha t} - e^{-\beta t})$$

Where, $v(t)$ instantaneous output voltage, V_0 DC charging voltage, α, β roots of the characteristics equation, which depends on the parameters of the generator. Where

$$\alpha = \frac{1}{R_d C_b}, \quad \beta = \frac{1}{R_e C_b}$$

c) Classification of Impulse Voltage Generator

1. Single Stage Impulse Generator
2. Multi Stage Impulse Generator

d) (Marx generator)

Single stage Impulse Generator

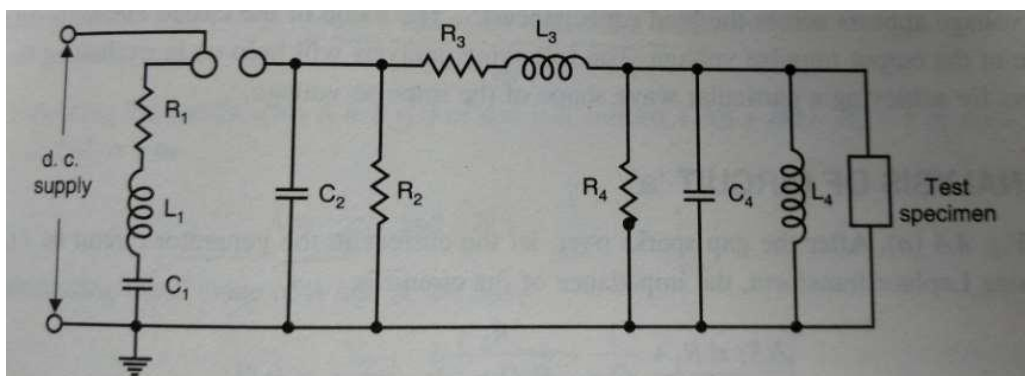


Fig: Single stage Impulse Generator Circuit

1. The *spark gap* act as voltage limiting & voltage sensing switch.
2. The apparatus which produces the *required voltages* is the **impulse generator**.
3. In high voltage engineering, an impulse voltage is normally a *unidirectional voltage* which rises quickly without appreciable oscillations, to a peak value and then falls less rapidly to zero.

Importance of each elements in impulse generator circuit

1. Capacitor (C1)-

- C1 is the capacitance of generator *charged from a dc source* to a suitable voltage.
- It will *discharge through the space gap*.
- If the generator is single stage C1 is enough.

In the case of *multistage impulse generator* group of capacitor connected in **parallel** and **discharged in series**.

2. Inductor (L1)

- It is used for the inductance of the generator.
- The leads of inductor is connecting to the generator.
- It consists of Small value.

3. Resistor (R1)

- Used for **Damping purpose**
- For **Output voltage / Output waveform control**.

4. L3 and R3

- These are external elements
- connected to the generator for the waveform control/shape

5. R2 and R4

- To Control the waveform duration -R4 serve as a potential divider .

6. C2 and C4

- Capacitance to the earth of high voltage components and leads.

7. C4

- Includes the capacitance of the test object -load capacitance

- Hold the voltage to produce required value of wave shape.

8. L4

- Inductance of test object
- Influence the waveform

9. Grounding

- One terminal of impulse generator is solidly grounded.
- The polarity of output voltage can be changed by changing the polarity of dc charging voltage.

Performance parameters of single stage impulse generator

1. Efficiency $\eta = \frac{1}{1 + C_2/C_1}$

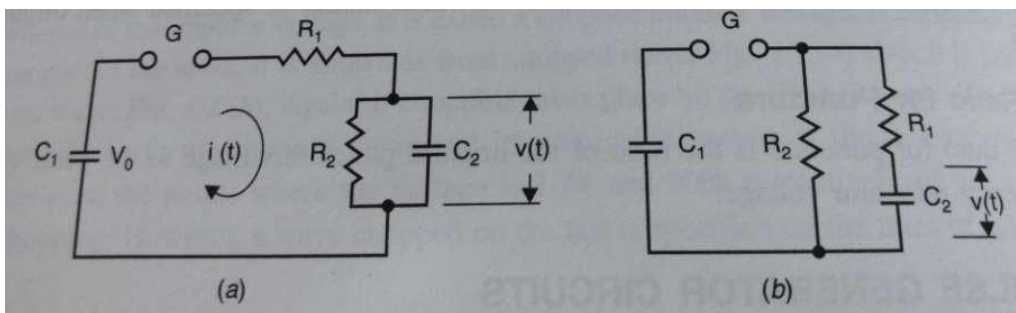
2. Impulse energy transformed during a discharge is given by

$$W = \frac{1}{2} C_1 * V_0^2$$

3. The minimum value of generator capacitance is given by

$$C_1 = \frac{MVA * 10^8}{Z * V^2}$$

Equivalent circuits of single stage Impulse Generator



- Evaluation & analysis is easy as compared to main circuit.

Note: Do refer text book of M S Naidu & V Kamaraju – page no 172 for more information

e) Drawbacks of single stage impulse generator

1. *Physical size* of the circuit elements are *very large*.
2. *Large size of sphere*.
3. *High dc charging voltage* is required.
4. *Suppression of corona is difficult*.
5. Switching of very high voltage with the spark gap is difficult.

Multistage Impulse Generator

2.3.2 Multistage impulse generator working of Marx impulse

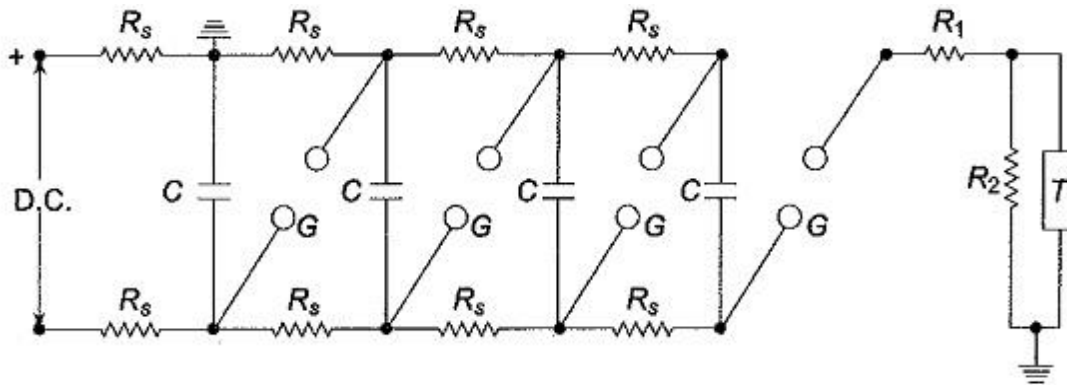
Introduction

- To obtain *higher* and *higher impulse voltage*.
- In 1923 *E. Marx* suggested a *multiplier circuit* which is *commonly used to obtain impulse voltage* with as *high a peak* value as possible for a given charging dc voltage.
- Depending upon the charging voltage available and output voltage required “*the number of identical impulse capacitors are charged in parallel and then discharged in series*”.
- Obtain total charging voltage multiplied with number of stages.

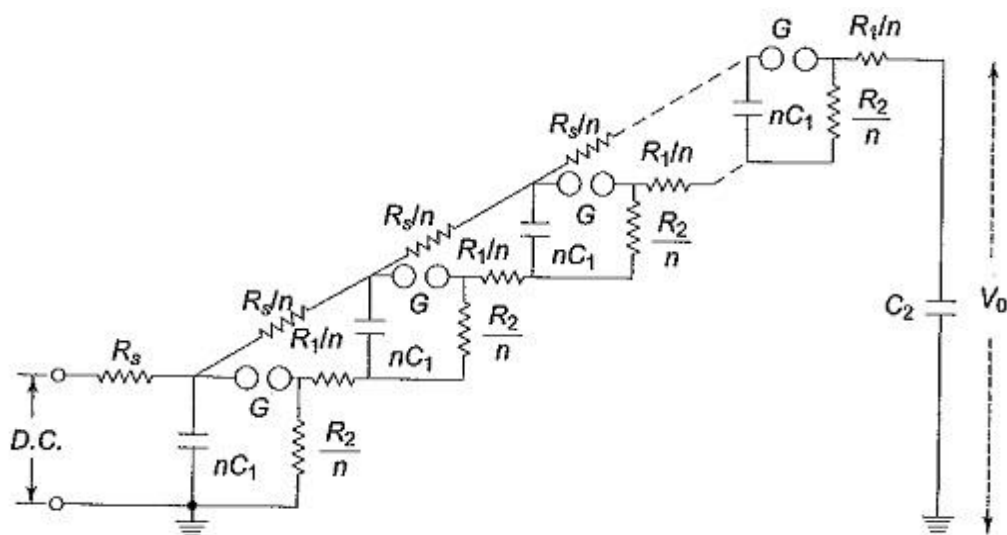
Why Multistage Impulse Generator?

A single capacitor C1 is may be used for voltages up to **200 kV**. Beyond this voltage, a single capacitor & charging unit may be too costly & the size becomes very large

Schematic Diagram of Multistage Impulse Generator



Schematic Diagram of Multistage Impulse Generator (Modified)



R_s is a charging resistance to limit the charging current.

1. The generator capacitance C is chosen such that the product of CR_s is about 10s to 1 min.
2. The gap spacing is chosen such that the breakdown voltage of the gap G is greater than the charging voltage V .
3. All the capacitance are charged to the voltage V in about 1 minute.
4. Charging time constant = CR_s (in seconds)
5. Discharging time constant = CR_1/n (in micro seconds), where n is the number of stages.



A **16 stage** Multistage Impulse Generator having a stage capacitance of **$0.280\mu F$** And maximum charging voltage **$300kV$** .

The height of the generator will be about **$15m$** .

$Area = 3.25m \times 3.00 m$

2.3.1.1 Construction of Multistage Impulse Generator

1. Require a *dc power supply* for *charging* the impulse capacitance *$C1$* of the generator.
2. Supply consists of *step up transformer* and *rectifier*.
3. The *value of resistor* should be *constant & never vary* with external factors.
4. *Non-inductive wire wound resistors* are commonly used.
5. *Resistors* which will be used for the construction for multistage impulse generator *flexible to replace*.
6. *Oil paper insulated capacitor* having high rate of discharge are normally employed and reason for *reduced size of capacitor*.
7. The *sphere gap* adjusted by a *remotely controlled motor* conjunction with indicator.
8. *Chimney* provided with *dust free and dry air*.
9. A *series protective resistance* should be included in this *earthing* device to *avoid too high discharge current*.
10. Charging resistors are fixed at sphere column.
11. Front and tail resistor fixed to the generator frame.
12. *All the leads and electrodes* should *dimensioned properly* to avoid *corona discharge*.

2.3.1.2 Components of a multistage impulse Generator

A Multistage impulse generator requires several components parts for Flexibility & production of the required wave shape.

1. DC Charging set

2. Charging Resistors

- Non inductive high value of resistance about *10 to 100k.Ω*
- Each resistance will be designed to have a maximum voltage *between 50 and 100kV*.

3. Generator Capacitors and spark gap

- Capacitor designed for several charging and discharging operations.
- Capacitors will be capable of having 10kA of current.
- Spark gaps will be usually spheres or hemispheres of 10 to 25 cm diameter.

4. Wave-shaping Resistors and Capacitors -Non inductive wound type -Capable of discharging 1000A current -50 to 100kV max. designed voltage

- Load capacitance will be 1 to 10nF

5. Triggering System

- Contains trigger spark gap to cause spark breakdown of the gaps.

6. Voltage Dividers

- Resistor type or damped capacitor type
- oscilloscope with recording arrangement are provided for measurement of voltage across test object

7. Gas insulated impulse generator

- Above 4MV impulse generator, tall & large space requirement
- 4.8MW- nearly 30m height
- N₂, compressed gas and SF₆ will provide proper insulation.

2.4 Triggering and Synchronization of the impulse Generator

Why triggering & synchronization?

- *Control for charging process* of impulse generator.
- To integrate the measuring devices.
- Chopping gap control.

- CRO is used for measuring and studying the effect of impulse wave on the performance of the insulation of the equipment.
- Impulse waves are of *shorter duration*.
- It is necessary that operation of the *generator* and the *oscillograph* should be *synchronized accurately*.
- *Time sweep circuit* is main part of *oscillograph*
- The *time sweep circuit* of the oscillograph should be initiated at the time slightly before the impulse wave reaches the deflecting plates.
- The *impulse generator drives both sweep and triggering circuits*.
- The *sweep circuit operating first* , triggering circuit works after 0.1 to 0.5 microseconds.

Triggering -3 Stages

1. *Fix the gap distance* between the spheres and increase the stage applied dc voltage till the flashover occurs.
2. *Set the gap distance* between the spheres large enough apply a desired voltage across them and then reduce the gap distance till flashover takes place.
3. *Fix both, the desired stage voltage and corresponding gap distance* within prescribed limits. Then apply the trigger pulse to the trigatron on the first stage.

Triggering and Synchronization of the impulse Generator

- *Two methods are available*
 1. Three electrode gap arrangement
 2. Trigatron gap

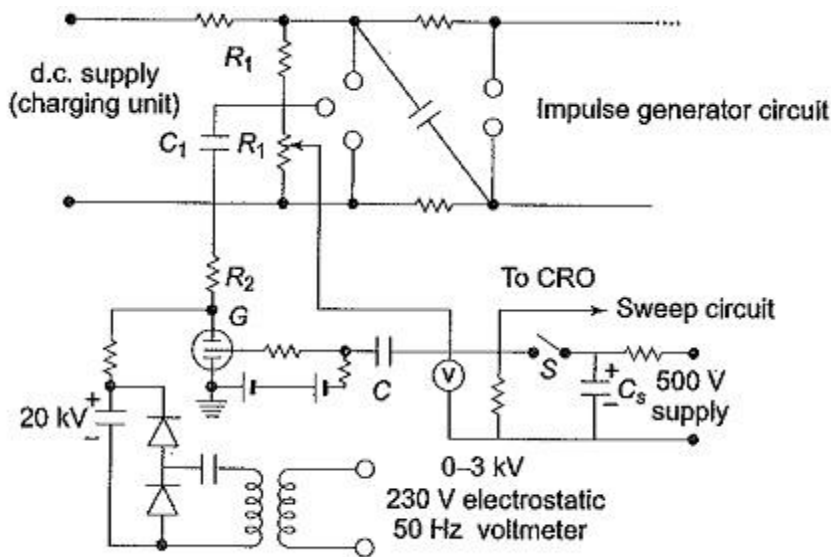
2.4.1 Triggering of impulse generator by three electrode gap arrangement

Triggering of impulse generator by

(i) Three electrode gap arrangement

1. '*Three electrode gap arrangement*' is one of the method for triggering and synchronization of impulse generator.
2. The *spacing between 2 spheres is adjusted* so that *two series gap are able to withstand charging voltage* of impulse generator.
3. *Central sphere* is called *control sphere*.
4. A *high resistance* is connected between the *outer sphere* and its *centre point* is connected to *control sphere*.

- The voltage between outer sphere is equally divided between two sphere gap



To test the dielectric breakdown strength of three sphere gap arrangement

- First *impulse generator* is to be *charged* to a voltage which is *slightly less than the breakdown voltage of the gap*.
- Apply an *impulse wave* of either polarity & peak voltage not less than $(1/5)$ th of charging voltage to the control sphere.
- Check whether the dielectric breakdown has occurred or not.

Operation of three sphere gap arrangement

- Two '*three sphere gap arrangement*' is included in the synchronization & triggering circuit

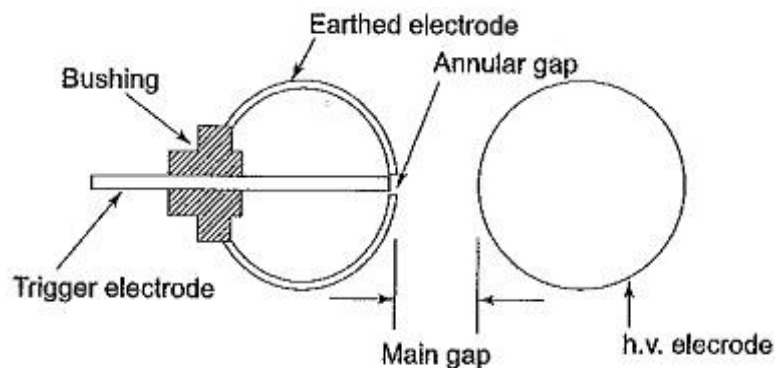
1. Three sphere gap arrangement'

- The switch 's' is closed which initiate the sweep circuit of the oscillograph.
- The same impulse is applied to the *thyatron tube*.
- The inherent time delay of thyatron ensure *sweep circuit operate first* before the starting of high impulse wave.
- We can be able to create further delay by using Capacitance-Resistance (R1C1) circuit.
- The tripping impulse is applied through capacitor C2.
- During charging period the voltage across thyatron is about +20kV.

2. Trigatron gap

1. A device, known as "*Trigatron*", is used to control the flash over at the spark gaps in order to get a desired magnitude of the output voltage repeatedly.
2. **Function-** used as 'First gap of impulse generator'
3. "*Trigatron*", consists essentially of three-electrodes.
4. **Three electrodes are**
 1. *High voltage electrode* is a sphere- indication of HV
 2. *Earthed electrode* is also a sphere. The spherical configuration gives homogeneous field.
 3. *Metal rod electrode/ Trigger electrode* be the third electrode

5.5 Diagram for "Trigatron spark gap"

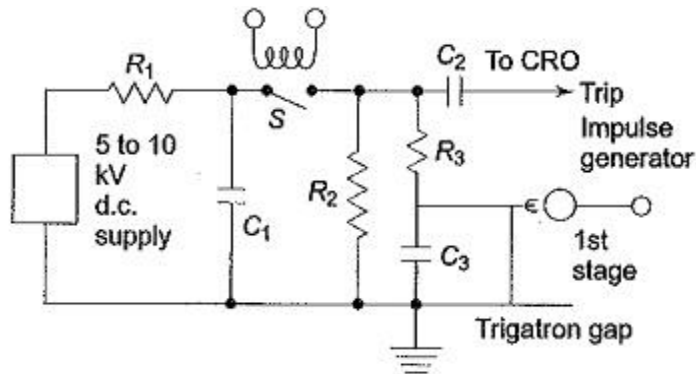


a) Construction of "Trigatron spark gap"

1. A small hole is drilled into earth electrode into which metal rod projects (trigger rod).
2. The annular gap between the rod and the surrounding hemisphere is 1 mm.
3. A glass tube is fitted over rod electrode.
4. The potential of metal electrode and earth electrodes are same.
5. Both are connected through a high resistance.

6. Tripping pulse or control pulse applied between metal and earth electrodes.
7. When the tripping pulse is applied, main field is distorted.
8. Reason for dielectric breakdown.

b) Tripping circuit of trigatron



(b) Tripping circuit using a trigatron

c) Operation of Tripping circuit of trigatron

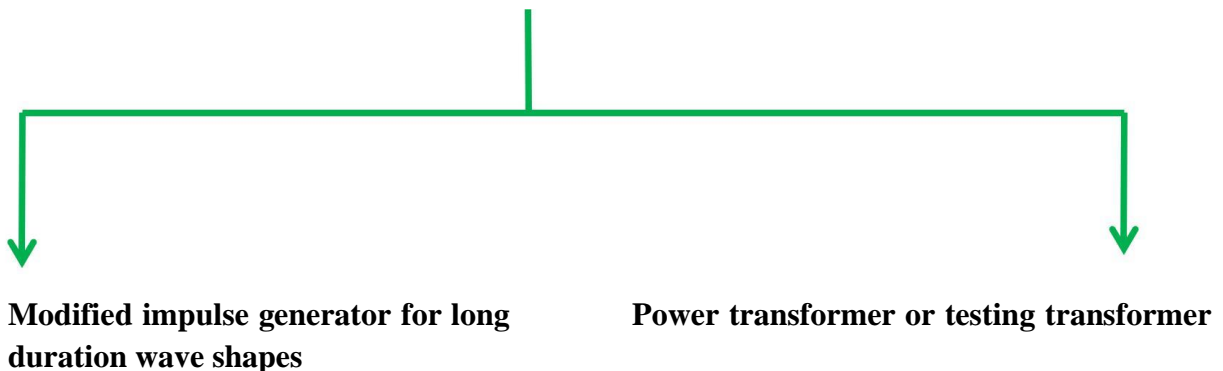
- The capacitor C_1 is charged through high resistance R_1
- Switch S is closed
- A pulse is applied to a sweep circuit of the oscillograph through the capacitor C_2
- Same time capacitor C_3 is charged
- Triggering pulse is applied through trigger electrode (metal rod electrode)
- The requisite delay in triggering the generator can be provide by R_3 and C_3
- The residual charge on the C_3 can discharged through R_3
- Now a day's laser is used for tripping the spark gap
- The trigatron also has a phase shifting circuit associate with the synchronization of initiation time with external Alternating voltage.
- Design is to prevent the overcharging of capacitor

- An *indicating device* shows whether the generator is going to fire properly or not.

2.4.1 Generation of switching surges/ switching impulse voltage

- *Switching surges* has an important role in the *design of insulation* for extra high voltage transmission line (EHV) & power systems.
- *Switching surge* is a *short duration transient voltage* produced in the system due to *sudden opening or closing of switch or circuit breaker*.
- Switching surges may be produced due to *arcing at faulty power systems*.
- The *transient voltage* may be oscillatory wave or damped oscillatory wave having *frequency of a few hundred Hz to a few kilo Hz*.
- Wave front time= 0.1 to 10ms
- Wave tail time ~ 1ms
- Switching surges contain higher energy than lightning impulse voltage.

- ***Types of circuit produced switching surges***



2.5 Impulse Current Generation

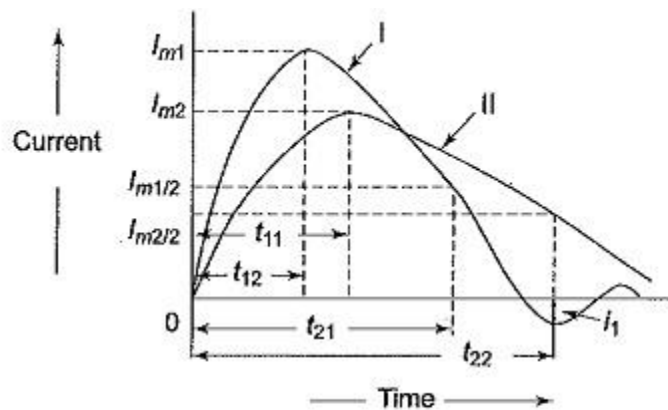
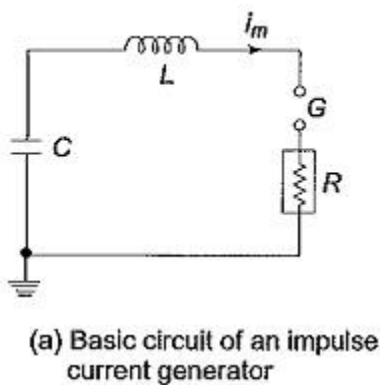
A *high impulse current generator* consists of *large number of capacitor* connected in *parallel* to a common discharge path. i.e by using '*capacitor bank*'.

- The generation of impulse current waveforms of high magnitude (nearly 100 KA) find applications like

- test work
- basic research on non-linear resistors -electric arc studies
- electric plasma state

a) Definition of impulse current waveforms

- The wave shapes used in testing surge diverters are (4/10 micro seconds-wave front) and (8/20 micro seconds –wave tail).
- Tolerance allowed in between +10% and -10%.
- Wave shapes are normally rectangular shape.

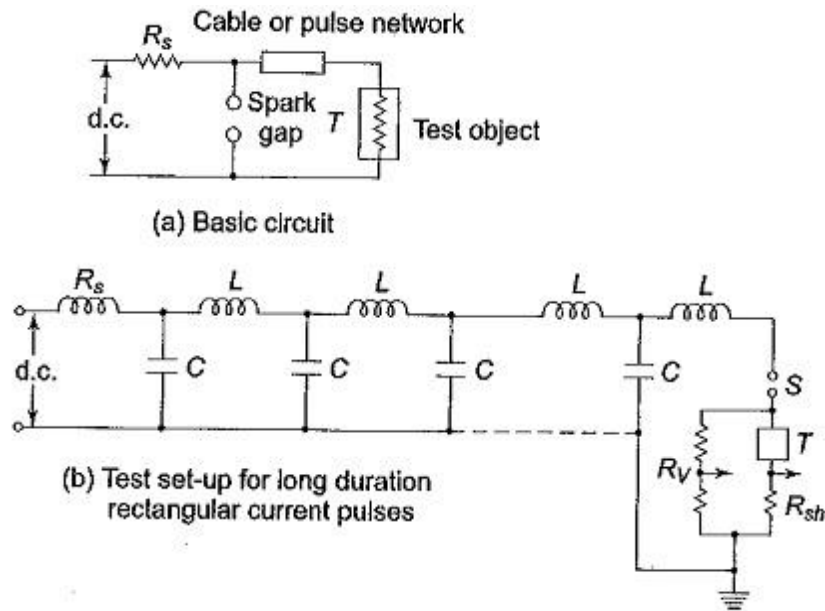


t_1 and t_{12} = time-to-front of waves I and II
 t_{21} and t_{22} = time-to-tail of waves I and II

I — damped oscillatory wave
 II — overdamped wave
 i_1 — overshoot

(b) Types of impulse current waveforms

b) Circuit producing impulse current wave



- *Number of capacitors* connected in parallel & discharged in parallel in the circuit.
- In order to minimize the value of inductance capacitance are subdivided into smaller units.

c) Components

1. *DC charging* unit giving variable voltage to capacitor bank.
2. Additional *air core inductor* having high current value.
3. Oscillograph- measurement purpose.
4. Triggering units & spark gap.

d) Generation of Rectangular Current Pulses

1. The generation of rectangular current pulse can be done by '*discharging a pulse network or cable previously charged*'
2. To produce a rectangular pulse a coaxial cable of surge impedance Z_0 is used.

Course Outcomes

At the end of the course the student will be able to:

CO-2: Apply the principles of generation of high voltage, currents and Impulse voltages.